


















The SOPHIE search for northern extrasolar planets

XIX. A system including a cold sub-Neptune potentially transiting a $V = 6.5$ star HD 88986[★]

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ABSTRACT

Transiting planets with orbital periods longer than 40 d are extremely rare among the 5000+ planets discovered so far. The lack of discoveries of this population poses a challenge to research into planetary demographics, formation, and evolution. Here, we present the detection and characterization of HD 88986 b, a potentially transiting sub-Neptune, possessing the longest orbital period among known transiting small planets ($<4 R_{\oplus}$) with a precise mass measurement ($\sigma_M/M > 25\%$). Additionally, we identified the presence of a massive companion in a wider orbit around HD 88986. To validate this discovery, we used a combination of more than 25 yr of extensive radial velocity (RV) measurements (441 SOPHIE data points, 31 ELODIE data points, and 34 HIRES data points), *Gaia* DR3 data, 21 yr of photometric observations with the automatic photoelectric telescope (APT), two sectors of TESS data, and a 7-day observation of CHEOPS. Our analysis reveals that HD 88986 b, based on two potential single transits on sector 21 and sector 48 which are both consistent with the predicted transit time from the RV model, is potentially transiting. The joint analysis of RV and photometric data show that HD 88986 b has a radius of $2.49 \pm 0.18 R_{\oplus}$, a mass of $17.2^{+4.0}_{-3.8} M_{\oplus}$, and it orbits every $146.05^{+0.43}_{-0.40}$ d around a subgiant HD 88986 which is one of the closest and brightest exoplanet host stars (G2V type, $R = 1.543 \pm 0.065 R_{\odot}$, $V = 6.47 \pm 0.01$ mag, distance = 33.37 ± 0.04 pc). The nature of the outer, massive companion is still to be confirmed; a joint analysis of RVs, HIPPARCOS, and *Gaia* astrometric data shows that with a 3σ confidence interval, its semi-major axis is between 16.7 and 38.8 au and its mass is between 68 and $284 M_{\text{Jup}}$. HD 88986 b's wide orbit suggests the planet did not undergo significant mass loss due to extreme-ultraviolet radiation from its host star. Therefore, it probably maintained its primordial composition, allowing us to probe its formation scenario. Furthermore, the cold nature of HD 88986 b (460 ± 8 K), thanks to its long orbital period, will open up exciting opportunities for future studies of cold atmosphere composition characterization. Moreover, the existence of a massive companion alongside HD 88986 b makes this system an interesting case study for understanding planetary formation and evolution.

Key words. planets and satellites: detection – techniques: photometric – techniques: radial velocities

1. Introduction

Among the 5000+¹ planets discovered so far (and many more candidates), transiting planets (~ 4000) have a considerable impact on our understanding of the formation and evolution of planetary systems. Such planets, when orbiting a bright host star that allows radial velocity (RV) follow-up, can be accurately characterized in terms of fundamental parameters such as mass and density, allowing for their internal structure to be modeled (e.g., Heidari et al. 2022; Delrez et al. 2021). Moreover, these objects provide us with a great opportunity to gather

information about the composition and temperature of their atmospheres by transmission and/or emission spectroscopy (e.g., Tabernero et al. 2020).

Among all the known transiting exoplanets with precise mass and radius measurements (Otegi et al. 2020), those with orbital periods exceeding 40 d are extremely rare, representing only $\sim 1\%$ of the total population (as of June 7, 2023). This scarcity poses a significant challenge to our understanding of planet demographics, formation, evolution, and the potential for habitability. The limited number of such long-period exoplanets has compelled many studies on exoplanet occurrence rates to focus primarily on planets with relatively short periods (e.g., Silburt et al. 2015; Petigura et al. 2013; Fulton et al. 2017). Moreover, Kopparapu et al. (2013) showed that the inner boundary of the habitable zone, encircling main-sequence stars with spectral types earlier than approximately M4 ($T_{\text{eff}} > 2800$ K), is

* Appendix D is available at the CDS via anonymous ftp to cdsarc.cds.unistra.fr (130.79.128.5) or via <https://cdsarc.cds.unistra.fr/viz-bin/cat/J/A+A/681/A55>

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¹ <https://exoplanetarchive.ipac.caltech.edu>

longer than ~ 11 d. This emphasizes the importance of exploring planetary systems with longer orbital periods in our pursuit of habitable planets. Additionally, new scientific exploration such as detecting exomoons has yet to be achieved. The importance of exomoon discovery is highlighted by our Moon’s influence on Earth’s spin dynamics (Li & Batygin 2014) as well as the prospective habitability of icy moons inside our own Solar System (Reynolds et al. 1983). The lack of successful exomoon discoveries could be linked to the dearth of long-period planets, as planets with longer orbital periods are more likely to harbor moons (Dobos et al. 2021). These examples highlight the importance of detecting and studying this “missing population”, thereby advancing our comprehension of exoplanet populations.

However, long-period transiting planets are particularly difficult to detect. The two primary methods used for detecting exoplanets, RV and transit photometry, each have their own challenges when it comes to detecting these elusive long-period planets. The RV method requires high-precision measurements over extended time spans to capture a full orbital period, while the transit method faces challenges due to both a lower transit probability and the limited baseline observations in most photometric surveys. These challenges are further compounded when dealing with smaller planets with a shallow transit depth and small RV semi-amplitude.

Here, we present the detection and characterization of a planetary system orbiting a $V = 6.5$ mag G2-type star: HD 88986 b, the longest-period transiting sub-Neptune among the known small planets ($< 4 R_{\oplus}$), accompanied by an outer massive companion. To accomplish this discovery, we employed a variety of observations, including photometric, spectroscopic, and astrometric techniques. The structure of this paper is organized as follows: Sect. 2 provides a description of the spectroscopic observations utilized in our analysis. In Sect. 3, the stellar properties of the host star are discussed. To identify the stellar rotational period, in Sect. 4 we present an analysis of various stellar activity indicators. In Sect. 5, we analyze RV data that led to the discovery of the sub-Neptune planet and a long-term curvature. In Sects. 6 and 7, we present the detection of a single transit event in TESS data sector 21 and perform a joint analysis, respectively. In Sect. 8, the result of our investigations into detecting HD 88986 b’s second transit event in additional photometric data is presented. Finally, in Sects. 9 and 10, we discuss the origin of the long-term trend and conclude on this system, respectively. The paper also includes appendices presenting updated and new procedures for spectroscopic extractions on SOPHIE data.

2. Spectroscopic observations

We have intensive spectroscopic observations of HD 88986 spanning a remarkable duration of 25 yr. These observations comprise a total of 506 data points obtained through the utilization of three high-resolution spectrographs: SOPHIE (Bouchy et al. 2013), HIRES (Vogt & Penrod 1988), and ELODIE (Baranne et al. 1996). The whole dataset is shown in Fig. 1. It displays a clear long-term curvature on a time scale of at least 25 yr, as well as other variations on shorter time scales.

2.1. High-resolution spectroscopy with SOPHIE

HD 88986 has been monitored by the SOPHIE high-precision spectrograph mounted on the 1.93-m telescope at the Haute-Provence Observatory (OHP, France). The observations were carried out as part of Recherche de Planètes Extrasolaires (RPE)

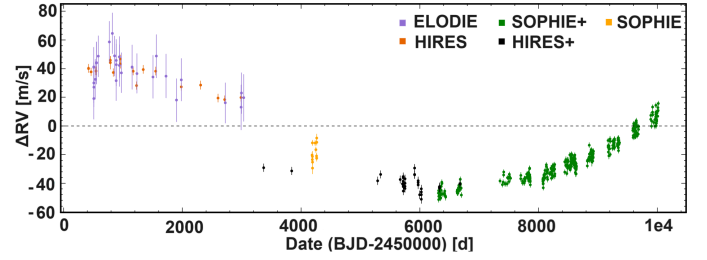


Fig. 1. Radial velocity measurements of HD 88986 from ELODIE, HIRES, HIRES+, SOPHIE and SOPHIE+.

program 1, also known as SP1, which is a high-precision program to search for Neptunes and Super-Earths orbiting bright stars in the solar neighborhood (Courcol et al. 2015; Hara et al. 2020; Heidari et al. 2022). Over a period of more than 15 yr, spanning from 2007 December 7th to 2023 March 12th, 441 high-resolution spectra were collected for this star (see Fig. 1). The observations were conducted in SOPHIE high resolution (HR) mode (resolving power of $\lambda/\Delta\lambda \approx 75\,000$ at 550 nm), with simultaneous thorium-argon (Th-Ar) or Fabry-Perot (FP) calibration light measurements. The latter allows us to track instrumental drift, ensuring precise and accurate RV measurements.

In June 2011, hexagonal fibers were installed in the SOPHIE spectrograph. This led to achieving an RV precision of $1\text{--}2\text{ m s}^{-1}$ but also about 50 m s^{-1} jump in the measured RVs of the standard stars (Bouchy et al. 2013). Hence, we separated the data before June 2011 (12 data points with the name SOPHIE) from the data after (429 data points with the name SOPHIE+). The exposure time was set for both data sets at 600–900 s to average the stellar oscillations, achieving a median signal-to-noise ratio (S/N) of 158 per pixel at 550 nm.

The RV was derived using the SOPHIE data reduction system (DRS, Bouchy et al. 2009). The DRS encompasses several crucial steps, including spectrum extraction, removal of telluric lines, correction for CCD charge transfer inefficiency (CTI), computation of the cross-correlation function (CCF) between the spectra and a binary mask, barycentric RV correction, and ultimately fitting Gaussian profiles to the CCFs to extract the RVs (Baranne et al. 1996; Pepe et al. 2002). We note that to extract HD 88986 RVs, we used a G2 mask. Additionally, prior to RV extraction, we corrected the spectra for the atmospheric dispersion effect (see Appendix A).

Once the RVs were extracted, we performed a correction for the nightly instrumental drift, which was measured through simultaneous calibration light observations. For this purpose, SOPHIE fiber A was dedicated to star observations, while fiber B was used to monitor a calibration lamp. In this configuration, sky background observations were not possible. Thus, it is crucial to identify and flag spectra contaminated by moonlight to ensure the accuracy of the RV analysis. By considering the phase and position of the Moon at the time of observation (see Appendix B for more details), we identified 31 spectra contaminated by the Moon. Consequently, we conservatively excluded these spectra from our analysis. We note that the inclusion or exclusion of these data points has no significant effect on our final results. Furthermore, we removed 1 data point that was identified as a 3σ RV outlier, along with an additional 17 measurements due to low signal-to-noise ratio ($S/N < 50$) and invalid calibration lamp flux. Consequently, a total of 50 data points were excluded from the SOPHIE+ measurements, and our final analysis incorporated

379 SOPHIE+ spectra, ensuring the reliability of our dataset for subsequent analysis.

SOPHIE experiences a long-term instrumental variation (Courcol et al. 2015), which is tracked by observing so-called “constant stars” every night. To account for this variation, following Courcol et al. (2015), we constructed a master time series using the RVs of these constant stars, which we then subtracted from the HD 88986 data. A detailed description of our update on the construction of the RV master constant time series can be found in Appendix C. The mean uncertainty of our final RV SOPHIE+ data is 1.2 m s^{-1} , with a root mean square (RMS) of 15.30 m s^{-1} . The final SOPHIE dataset is provided in Table D.1.

2.2. High-resolution spectroscopy with HIRES

The star was observed using the HIRES spectrograph from 1996 December 2nd to 2014 January 19th, spanning 17 yr during which 51 high-resolution spectra were obtained (see Fig. 1). Detailed information regarding data reduction and observation can be found in Butler et al. (2017). HIRES data experience a small jump of $1.5 \pm 0.1 \text{ m s}^{-1}$ resulting from a CCD change in August 2004, as well as a long-term drift ($\lesssim 1 \text{ m s}^{-1}$) and a small intra-night drift, as identified by Tal-Or et al. (2019). To account for these effects, we utilized the systematically corrected HIRES data obtained from the Vizier catalog access tool² following the methodology outlined in Tal-Or et al. (2019). The mean uncertainty of the HIRES data is 1.2 m s^{-1} , with a RMS of 11.1 m s^{-1} . To address any residual offsets from the CCD change in the HIRES data, we fit an offset between the data obtained before (HIRES) and after (HIRES+) the CCD change. The HIRES RVs are presented in Table D.2. We note that our moon contamination criteria (see Appendix B) were not applied to HIRES data since these data are only utilized to investigate the origin of the long-term curvature and are not intended for high-precision detection of the sub-Neptune.

2.3. High-resolution spectroscopy with ELODIE

ELODIE was a high-resolution spectrograph, mounted on the 1.93-m telescope at OHP, which was in particular used to discover the first exoplanet in 1995 (Mayor & Queloz 1995). HD 88986 was observed by ELODIE from 1997 February 28 to 2004 January 29, gathering 31 high-resolution spectra (see Fig. 1). The K0 numerical mask is used to extract the RVs (Baranne et al. 1996). The exposure time varied from 600 to 900 s, resulting in a mean uncertainty of 9.0 m s^{-1} and RMS of 13.0 m s^{-1} , which is close to the intrinsic stability of ELODIE. We note that 3 data points were removed due to their low S/N (< 50). They are listed in Table D.3. Similar to the HIRES data, the moon contamination criteria were not applied, as this data was not utilized for the detection of the sub-Neptune but to investigate the origin of the long-term curvature.

3. Stellar parameters

HD 88986 is a G2V star with a G magnitude of 6.3. To obtain the stellar atmospheric parameters, we co-added all SOPHIE+ spectra (428) after correcting for the RV variation of the star, barycentric Earth radial velocity, and background pollution due to the calibration lamp (Heidari 2022; Hobson 2019). This results in a high S/N per pixel spectrum of 3174 at 550 nm. Then we calculated the effective temperature (T_{eff}), metallicity ([Fe/H]), and

² <https://vizier.u-strasbg.fr/viz-bin/VizieR>

Table 1. Stellar properties of HD 88986.

Identifiers	TIC 1042868 HD 88986 HIP 50316 <i>Gaia</i> DR3 741184091114529792 2MASS J10162809+2840571	
Parameter	HD 88986	References
Astrometric properties		
Parallax (mas)	29.9864 ± 0.0205	<i>Gaia</i> DR3
AEN ε (mas)	0.135	<i>Gaia</i> EDR3
Significance of ε	20.6	<i>Gaia</i> EDR3
Distance (pc)	33.37 ± 0.04	<i>Gaia</i> DR3
α (h m s)	10:16:28.08	<i>Gaia</i> DR3
δ (d m s)	28:40:56.94	<i>Gaia</i> DR3
Photometric properties		
$B - V$	0.635 ± 0.006	HIP
V (mag)	6.47 ± 0.01	HIP
<i>Gaia</i> (mag)	6.315 ± 0.003	<i>Gaia</i> DR3
<i>Gaia</i> _{BP} (mag)	6.628 ± 0.003	<i>Gaia</i> DR3
<i>Gaia</i> _{RP} (mag)	5.822 ± 0.004	<i>Gaia</i> DR3
TESS (mag)	5.8706 ± 0.0061	TESS
J (mag)	5.247 ± 0.024	2MASS
H (mag)	4.946 ± 0.023	2MASS
K_s (mag)	4.884 ± 0.020	2MASS
W_1 (mag)	4.895 ± 0.239	WISE
W_2 (mag)	4.762 ± 0.085	WISE
W_3 (mag)	4.933 ± 0.014	WISE
W_4 (mag)	4.873 ± 0.029	WISE
Spectroscopic properties		
Spectral type	G2V	MK classification
$\log g$ (cm s^{-2})	4.16 ± 0.03	Sect. 3
ξ_t (km s^{-1})	1.11 ± 0.02	Sect. 3
$\log(R'_{\text{HK}})$	-5.04 ± 0.10	Sect. 4
$v \sin i$ (km s^{-1})	3.3 ± 1.0	SOPHIE DRS
[Fe/H]	0.06 ± 0.02	Sect. 3
T_{eff} (K)	5861 ± 17	Sect. 3
Bulk properties		
Mass (M_{\odot})	$1.25 \pm 0.05[0.06]^{(*)}$	SED Sect. 3
Radius (R_{\odot})	$1.543 \pm 0.010[0.065]^{(*)}$	SED Sect. 3
P_{rot} (d)	25_{-6}^{+8}	Sect. 4
Age (Gyr)	$7.9 \pm 1.3[1.58]^{(*)}$	Sect. 3

Notes. ^(*) Adopted the systematic uncertainty floor as suggested by Tayar et al. (2022) throughout this study.

surface gravity ($\log g$), using the procedure described in Santos et al. (2013) and Sousa et al. (2018). The resulting T_{eff} , [Fe/H], and $\log g$ together with other stellar parameters of HD 88986, are presented in Table 1.

We performed an analysis of the broadband spectral energy distribution (SED) of the star together with the *Gaia* EDR3 parallax (with no systematic offset applied; see, e.g., Stassun & Torres 2021), in order to determine an empirical measurement of the stellar radius, following the procedures described in

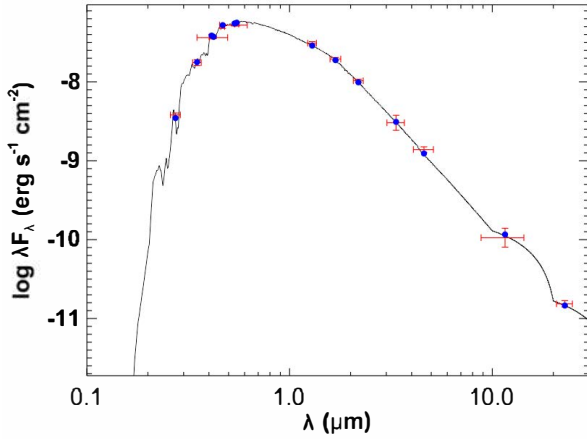


Fig. 2. Spectral energy distribution of HD 88986. Red symbols represent the observed photometric measurements, whereas the horizontal bars represent the effective width of the passband. Blue symbols are the model fluxes from the best-fit Kurucz atmosphere model (black).

Stassun & Torres (2016); Stassun et al. (2017); Stassun & Torres (2018). We obtained the $B_T V_T$ magnitudes from *Tycho-2* (Høg 2001), the JHK_S magnitudes from 2MASS (Cutri et al. 2003), the $W1 - W4$ magnitudes from WISE (Wright et al. 2010), the *uvby* Strömgren magnitudes from Paunzen (2015), and the $G_{BP} G_{RP}$ magnitudes from *Gaia* (Gaia Collaboration 2016, 2021). We also used the UV measurement at 274 nm from the *TDI* UV satellite (Thompson et al. 1978). Together, the available photometry spans the full stellar SED over the wavelength range 0.2–22 μm (see Fig. 2). Then, we performed a fit using Kurucz’s stellar atmosphere models with the T_{eff} , $\log g$, and $[\text{Fe}/\text{H}]$ adopted from the spectroscopic analysis. The remaining free parameter is the extinction A_V , which we fixed at zero due to the proximity of the system to Earth.

The resulting fit (Fig. 2) has a reduced χ^2 of 1.4. Integrating the model SED gives the bolometric flux at Earth, $F_{\text{bol}} = 7.28 \pm 0.17 \times 10^{-8} \text{ erg s}^{-1} \text{ cm}^{-2}$. Taking the F_{bol} and T_{eff} together with the *Gaia* parallax, gives the stellar radius, $R_{\star} = 1.543 \pm 0.010 R_{\odot}$, placing the star within the subgiant range (1.5–3 R_{\odot} ; Huber et al. 2017; Berger et al. 2018). In addition, we can estimate the stellar mass from the empirical relations of Torres et al. (2010), giving $M_{\star} = 1.19 \pm 0.07 M_{\odot}$, which is consistent with the value of $1.25 \pm 0.05 M_{\odot}$ determined empirically via R_{\star} and $\log g$. We acknowledge the possibility that our formal error budget for radius, mass, and stellar age could be underestimated, as suggested by Tayar et al. (2022). For stars such as HD 88986, the systematic uncertainty floor could rather be up to $\approx 4.2\%$ for radius, $\approx 5\%$ for mass, and $\approx 20\%$ for age. Hence, we conservatively adopt these relative uncertainties, reported in brackets in Table 1, to obtain more realistic stellar parameter errors throughout this study.

Finally, we can use the observed $\log R'_{\text{HK}}$ (see Sect. 4) to estimate the stellar age via empirical activity-age relations. We obtain an age of $\tau_{\star} = 7.9 \pm 1.3 \text{ Gyr}$ via the empirical relations of Mamajek & Hillenbrand (2008).

4. Stellar rotation and activity

To study the host star’s activity and rotational period, we used $\log R'_{\text{HK}}$, S-index, Na index, and CCF bisector measurements from the SOPHIE+ spectrograph, along with the S-index values from the HIRES and HIRES+ spectrographs. The bisector spans

are derived from the SOPHIE DRS using the method described by Queloz et al. (2001). We extracted the Na index as introduced in Da Silva et al. (2011). The HIRES and HIRES+ S-index values were acquired from Butler et al. (2017). For the extraction of $\log R'_{\text{HK}}$ and S-index from the SOPHIE+ spectra, we followed the procedure outlined by Noyes et al. (1984) and Boisse et al. (2010), respectively. The key step before deriving the $\log R'_{\text{HK}}$ and S-index is subtracting the background contamination light from the Th-Ar or FP calibration lamp from the stellar spectra. To correct this, we used the direct measurement method (see Appendix E).

To estimate the rotational period of the star, we summed 176 HD 88986 SOPHIE+ spectra which fulfilled two criteria. First, the spectra with $S/N > 50$ in the first (bluest, $\lambda \sim 3955 \text{ \AA}$) order of spectra where CaII H&K lines are located. Second, the spectra with minimal contamination due to the background light. This led to the value of $\log R'_{\text{HK}} = -5.04 \pm 0.10$. Furthermore, we investigated potential changes in magnetic activity over an approximately 11-yr SOPHIE+ observation span. For this purpose, the dataset was divided into three distinct observational seasons spanning from 2012 to 2023: 2012–2016, 2016–2019, and 2019–2023. We observed a gradual increase in the $\log R'_{\text{HK}}$ parameter, with values transitioning from -5.12 ± 0.10 during the initial subset to -5.05 ± 0.10 in the second subset, and ultimately stabilizing at -5.00 ± 0.10 in the final subset. All these values are in good agreement with the value of $\log R'_{\text{HK}} = -5.22$ and $\log R'_{\text{HK}} = -5.07$ reported by Radick et al. (2018) and Hall et al. (2007), respectively. Finally, we estimated a rotational period of 25_{-6}^{+8} d following Noyes et al. (1984), a value consistent with the Mamajek & Hillenbrand (2008) recipe, which yields $26.3 \pm 3.1 \text{ d}$.

We searched for rotational modulation in the Simple Aperture Photometric (SAP; see Twicken et al. 2010; Morris et al. 2020) TESS data (see Sects. 6 and 8.2 for details of the observations) using the Lomb-Scargle periodogram (Lomb 1976; Scargle 1982; VanderPlas 2018). No convincing signal was found. This was expected, given the star’s quiet nature and also the limited $\sim 27 \text{ d}$ observation window of TESS, which made the clear visibility of a 25 d signal difficult. We also note that additional photometric data from the T8 automatic photoelectric telescope (APT) did not show any photometric variability related to the stellar rotational period (see Sect. 9.1).

To constrain the stellar rotation, we conducted an analysis of the activity indicator periodogram using the Data and Analysis Center for Exoplanets (DACE; Delisle et al. 2016)³. For this analysis, we utilized the SOPHIE+ S-index to ensure comparability with the S-index measurements obtained from HIRES and HIRES+ instruments. We excluded a total of 68 S-index data points due to their dependency on S/N (< 30 in SOPHIE+ order 1, $\lambda \sim 3955 \text{ \AA}$) and significant contamination caused by the calibration lamp. Additionally, one data point was excluded due to its identification as a 5σ outlier. In a similar vein, 102 data points from the Na index were omitted due to their reliance on S/N (< 70 in SOPHIE+ order 30, $\lambda \sim 5931 \text{ \AA}$) and their susceptibility to contamination by the telluric lines. Figure 3 displays the periodogram of activity indicators. The HIRES and HIRES+ S-index measurements, along with the SOPHIE+ S-index, reveal periodic signals at 29.6 d (false alarm probability (FAP) $< 1\%$, Baluev 2008) and 31.5 d (FAP $< 10\%$), respectively. These results are consistent with the estimated rotational period of the star at 25_{-6}^{+8} d . Furthermore, there is an activity signal at 141.2 d in the

³ Available at <https://dace.unige.ch>

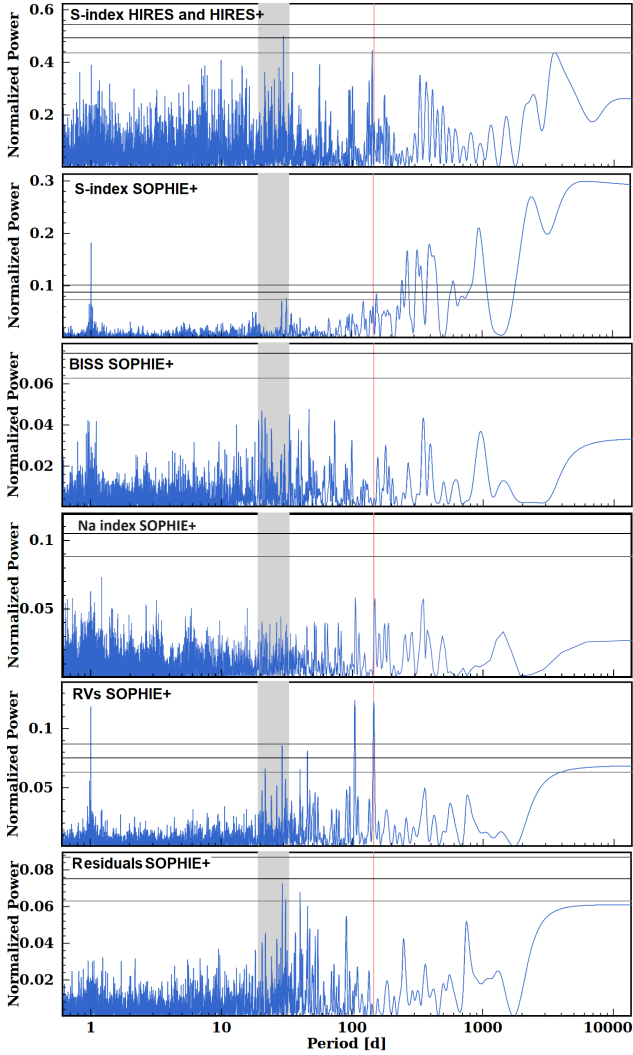


Fig. 3. Periodogram of RVs and activity indicators of HD 88986. From top to bottom: HIREs and HIREs+ S-index, SOPHIE+ S-index, bisector, RVs, and residuals of RVs after Keplerian fit on the 146.1 d. The vertical red line illustrates the planet candidates on 146.1 d, which have no corresponding peak in activity indicators. The vertical gray strip marks the estimated rotational period of the star. Also, the horizontal lines show the FAP level of 10, 1, and 0.1%, respectively (Baluev 2008).

periodogram of the HIREs and HIREs+ S-index, which will be further discussed in the following section.

5. Detection of the sub-Neptune HD 88986 b in the SOPHIE+ RVs

5.1. RV periodogram

To perform our RV periodogram analysis, we only used SOPHIE+ RV data because it contains an extensive number of data points (378), a long baseline, a higher RV accuracy, and superior sampling compared to other instruments. The analysis employed the default noise model in DACE, assuming an additional Gaussian white noise with nominal error bars of 1.5 m s^{-1} on the SOPHIE+ RVs. After removing the long-term curvature using a second-order polynomial model, the periodogram of SOPHIE+ RVs showed significant peaks at 104.8 and 146.1 d, falling below the analytical FAP (Baluev 2008) of 0.1%

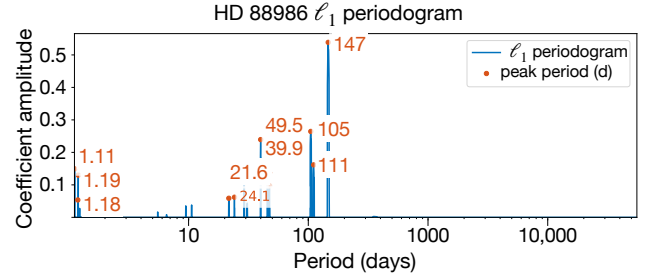


Fig. 4. ℓ_1 periodogram of SOPHIE+ data. The identified periods are shown in red.

(see Fig. 3, fourth panel). These two signals are yearly aliases of one another.

To determine the favored alias between two signals, we compute the ℓ_1 periodogram. This one takes in a frequency grid and an assumed covariance matrix of the noise as input. It aims to find a representation of the RV time series as a sum of a small number of sinusoids whose frequencies are in the input grid. It outputs a figure that has a similar aspect as a regular periodogram but with fewer peaks due to aliasing. The peaks can be assigned a FAP, whose interpretation is close to the FAP of a regular periodogram peak. The signals found to be statistically significant might vary from one noise model to another. To explore this aspect, as in Hara et al. (2020), we considered several candidate noise models based on the periodicities found in the ancillary indicators. We tried 1200 noise models, all Gaussian, such that the covariance is the sum of a white noise term of amplitude σ_W , a red noise term with Gaussian decay of amplitude σ_R and timescale τ_R , and a quasi-periodic component (Haywood et al. 2014) with amplitude σ_{QP} , timescale τ_{QP} and period P^* and harmonic complexity equal to 1. We tried all combinations with $\sigma_W, \sigma_R, \sigma_{QP} = 0, 0.3, 0.6, 0.9, 1.2, 1.5 \text{ m s}^{-1}$, $\tau_R = 0, 3, 6 \text{ day}$, $P^* = 29 \text{ d}$ and $\tau_{QP} = 20, 40, 60 \text{ d}$ or $P^* = 40 \text{ d}$ and $\tau_{QP} = 20, 50, 80 \text{ d}$. We ranked the models with cross-validation as well as Laplace approximation of the Bayesian evidence. We find that for the 20% highest ranked models, a peak with a period between 145 and 149 d consistently appears. The model with the highest Laplace approximation of the evidence is obtained with $\sigma_W = \sigma_{QP} = 1.2 \text{ m s}^{-1}$, $\sigma_R = 1.5 \text{ m s}^{-1}$, $\tau_R = 0 \text{ d}$, $\tau_{QP} = 20 \text{ d}$. The corresponding ℓ_1 periodogram is shown in Fig. 4. The highest peak appears at 146.5 d, which is compatible with the 146.1 d signal given the frequency resolution set by the timespan of observations. This signal presents a FAP of 2.45×10^{-6} , which is clearly statistically significant. We, therefore, conclude that the true signal is at 146 d, while the signal at 104.8 d represents its yearly aliases. Other signals appearing on the ℓ_1 periodogram are not statistically significant.

Subsequently, we performed a circular Keplerian fit (see Sects. 5.2 and 5.3) to remove the signal at 146.1 d and investigated the resulting RV residuals. The periodogram displayed two signals at 29.2 d and 40.0 d, with FAP values below 10% (see Fig. 3, bottom panel).

To conclude our analysis, we checked that the 146 d signal has a constant phase and amplitude following the methodology of Hara et al. (2022a). It simply consists of computing g the phase and amplitude of a signal at a given period with a moving time window. To perform this analysis, it is crucial to have realistic error bars. As visible in Fig. 3, the SOPHIE+ S-index exhibits low-frequency variations that are most likely due to a magnetic cycle. We expect a higher dispersion of RVs when S-index values are high (Borgniet et al. 2015; Meunier 2021;

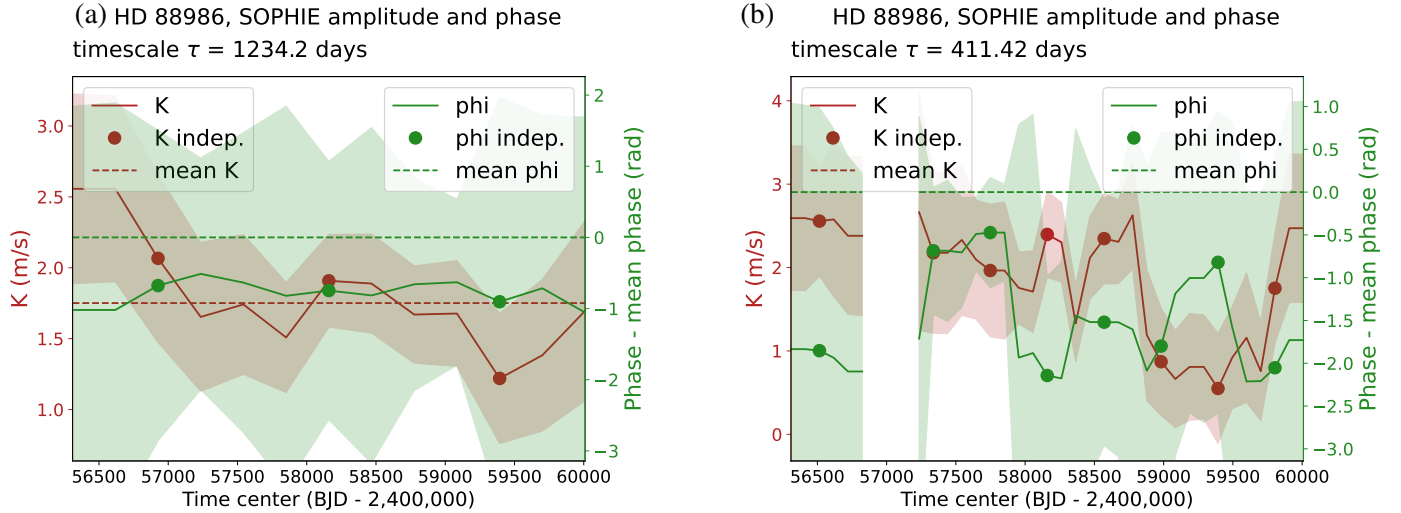


Fig. 5. Amplitude (red) and phase (green) of a 146.1 d signal as a function of time for different sizes of time windows. Solid lines correspond to estimate and shaded areas to $\pm 1 \sigma$ uncertainties. Denoting by T_{obs} the total time span of observations, a) and b) are obtained with windows of size $T_{\text{obs}}/3 = 1234.2$ d and $T_{\text{obs}}/9 = 411.42$ d, respectively.

Hara & Delisle 2023). Following Díaz et al. (2016), we added a white noise jitter term, as well as a jitter scaled with the value of the $\log R'_{\text{HK}}$, and fit those along with a polynomial line and the 146 d signal. We used those values to compute the amplitude and phase as a function of time, shown in Fig. 5. We here consider windows of size $T_{\text{obs}}/3 = 1211$ days and $T_{\text{obs}}/9 = 411$ days where T_{obs} is the total time span of observations. The most notable feature is the drop in amplitude in Fig. 5b at BJD 2 459 000–2 460 000. We performed the quantitative analysis presented in Hara et al. (2022a) and determined that the phase and amplitudes are consistent with being constant. The drop in amplitude is likely due to the fact that the epoch BJD 2 459 000–2 460 000 corresponds to an activity maximum, and it is possible that the activity pattern changes and masks the planetary signal in the corresponding observational seasons.

To summarize, both periodograms exhibit a strong periodicity of about 146 d in RVs, which falls within a different period than the estimated star’s rotation period (25^{+8}_{-6} d; see Sect. 4). Notably, the periodogram of the HIRES and HIRES+ S-index reveals an activity signal at 141.2 d, which differs from the RV signal by five days and has a relatively low strength (FAP $\sim 10\%$). None of the SOPHIE+ activity indicators showed a periodicity at 146.1 d. Moreover, no correlation was found between RV residuals after removing the trend and both S-index (Pearson’s coefficient $R = 0.03$) and bisector (Pearson’s coefficient $R = 0.13$). Furthermore, our analysis above demonstrates consistent phase and amplitude of the 146.1 d signal. Consequently, it is unlikely that RV periodicity at 146.1 d has an activity origin. Additionally, it is noteworthy that a survey encompassing all SOPHIE constant stars, as well as other stars observed by SOPHIE, did not reveal the same RV periodicity, confirming that the observed periodicity is not due to instrumental artifacts. Therefore, the RV signal at 146.1 d is likely to have a planetary origin. Throughout the rest of the paper, we attribute this periodicity to the planet HD 88986 b.

Furthermore, given the two periodic signals of 31.5 d in the SOPHIE+ S-index and 29.6 d in the HIRES and HIRES+ S-index, along with the estimated star rotation period (25^{+8}_{-6} d), the RV residuals signal at 29.2 d is likely the result of stellar rotational modulation. We take into account this signal in our analysis for the rest of the paper, testing three different

methods to model it (see below in Sect. 5.2). Finally, since the RV residuals signal at 40.0 d is statistically insignificant, further observations are required to determine whether this signal has an astrophysical origin or is simply noise.

We note that among the RVs presented in this paper, only those obtained with SOPHIE+ allow the low-amplitude signal of planet HD 88986 b to be detected. This is due both to the large number of measurements and to their high accuracy. ELODIE, SOPHIE, HIRES, and HIRES+ RVs do not assist here in the discovery of that planet. Therefore, to avoid any offsets or potential systematics among instruments, we only use the SOPHIE+ data in the fits of HD 88986 b presented below in the continuation of this section and Sect. 7. The other RVs datasets are only included in Sect. 9.2 for constraining the outer companion.

5.2. RV models

To adequately describe the data, we took into account several SOPHIE+ RV-only models and performed model comparisons. The RV analysis was carried out by juliet (Espinoza et al. 2019), which employs *radvel* (Fulton et al. 2018) to model RVs and *george* (Ambikasaran et al. 2015) and *celerite* (Foreman-Mackey et al. 2017) to model potential activity effects on the data through Gaussian process regression (GPs). For each tested model, juliet computes the Bayesian log evidence ($\ln Z$). If the Bayesian log-evidence difference ($\Delta \ln Z$) between a model and another exceeds two, it is moderately favored over the latter; a difference greater than five indicates strong favorability (Trotta 2008). The models are indistinguishable when the difference in Bayesian log evidence is $\Delta \ln Z \leq 2$. In this case, the model with the fewest free parameters would be chosen.

We defined our RV model as follows:

$$M(t) = K(t) + \epsilon(t) + \mu + Q(t^2) + A(t), \quad (1)$$

where $K(t)$ is the Keplerian model and the $\epsilon(t) \sim \mathcal{N}(0, \sigma(t)^2 + \sigma_w^2)$, is a normal distribution (\mathcal{N}) of white-Gaussian noise where $\sigma(t)$ is the uncertainty of each RV point at time t , and σ_w is a jitter term. Additionally, μ is a systematic RV offset of the instrument, and Q and A are defined as quadratic and linear terms, respectively, to model the long-term curvature. The model

Table 2. Different tested models on the SOPHIE+ RV-only data along with model comparisons with `juliet`.

Model	$\Delta \ln Z$	period (d)	K (m s ⁻¹)	T_c (BJD-2400000 d)
No planet	-97.0	–	–	–
No planet+EXP-GP	10.2	–	–	–
No planet+QP-GP	17.5	–	–	–
1Co	0	146.0 ± 0.5	1.7 ± 0.2	58 897 ± 3
1eccentricity-free	1.6	145.8 ^{+0.4} _{-0.3}	1.9 ± 0.3	58 884 ⁺⁸ ₋₇
1Co+sinusoidal	5.3	146.2 ± 0.4	1.6 ± 0.2	58 899 ± 3
1Co+EXP-GP	20.0	146.3 ± 0.6	1.6 ± 0.4	58 897 ⁺⁵ ₋₆
1Co+QP-GP	22.3	146.3 ± 0.6	1.7 ± 0.4	58 897 ± 6

Notes. K refers to the RV semi-amplitude and T_c is the time of mid-transit from RV fit. Additionally, in the model names, “Co” represents a circular orbit. The final choice model is indicated in bold.

is tested for both scenarios of the eccentricity-free and circular orbit (Co). To explore the possible effect of stellar activity on the planet’s parameters, we model the stellar activity in three different ways:

- a sinusoidal orbit;
- an exponential GP kernel (EXP-GP) with the form of $k_{i,j} = \sigma_{\text{GP}}^2 \exp(-|t_i - t_j|/T_{\text{GP}})$, where σ_{GP} is the amplitude of GP modulation, and T_{GP} presents the characteristic timescale (Ambikasaran et al. 2015);
- a quasi-periodic GP kernel (QP-GP, Foreman-Mackey et al. 2017) with the form of $\kappa_{i,j} = B_{\text{GP}}/(2 + C_{\text{GP}}) e^{(-|t_i - t_j|/L_{\text{GP}})} (\cos(2\pi|t_i - t_j|/P_{\text{rot;GP}}) + (1 + C_{\text{GP}}))$, where B_{GP} amplifies the kernel, C_{GP} is a constant scaling term, L_{GP} is a correlation time-scale component, and finally $P_{\text{rot;GP}}$ is the rotational modulation.

In addition to the models above, we also executed three no-planet models wherein we assumed the absence of any planetary signal in the RVs (i.e., in Eq. (1): $K(t) = 0$). Table 2 provides a summary of the results obtained from testing various models. Furthermore, Table F.1 presents the priors employed in the analysis, along with detailed descriptions of all parameters. Throughout this paper, we conducted `juliet` runs for each model using a consistent setup, employing a configuration with 3× number of free parameters as the number of walkers, executed 10 000 steps per walker, and discarded the initial 3000 steps as burn-in.

5.3. Detection of the sub-Neptune HD 88986 b

We set a uniform prior to the planetary period between 135 d and 155 d. For the mid-transit time, we applied a uniform prior defined by a time window of 146 d which is consistent with the planetary period duration. For the other parameters, we used fairly broad uniform priors. The results of the no-planet model as well as the circular and eccentric fits are shown in the Table 2. We note that this table includes T_c , the derived center time of the inferior conjunction, as a transit of this planet is reported below in Sect. 6. The results of the circular and eccentric models are consistent and both are statistically significant compared to the no-planet model ($\Delta \ln Z \geq 97$) which confirms a clear detection of the planetary signal. The eccentricity-free model, however, exhibits bimodality on the periastron argument ω . Given that the two models are statistically indistinguishable ($\Delta \ln Z \leq 2$), and their posterior distributions are consistent, we continued to model the HD 88986 b planet with a circular orbit as it has fewer free parameters.

The last three lines of Table 2 present the results of the fits adopting the three different models for the stellar activity (see Sect. 5.2). In the sinusoidal model, we employed a uniform prior for the activity period ranging from 25 to 35 d, as we detected a potential stellar signal at 29 d (see Sect. 4). Regarding the QP-GP hyperparameter, we imposed some constraints. On $P_{\text{rot;GP}}$, we used a Gaussian prior centered at 29 d with a standard deviation of 3 d. On the C_{GP} , we initially tried a wide range of Jeffreys priors from 10^{-20} to 100. The posterior distribution of C_{GP} reached the prior boundary at 10^{-20} , indicating that this parameter converged to zero. This result motivates us to set the C_{GP} to 10^{-20} , which is consistent with zero. We note that the models with fixed/unfixed C_{GP} are statistically indistinguishable ($\Delta \ln Z \leq 2$). Therefore, we fixed C_{GP} and continued using the QP-GP model with three free parameters. A broad uniform prior is taken into account for all remaining parameters of different models, as presented in Table F.1.

The results of the five different planet models reported in Table 2 are consistent. This strongly argues in favor of the detection of the planet HD 88986 b with those parameters. Notably, all planet models accounting for the potential activity signal are strongly favored statistically ($\Delta \ln Z \geq 5$) when compared to models that do not consider the stellar activity. Among these models, the planet models with simultaneous GP kernels (1Co+EXP-GP and 1Co+QP-GP) are strongly favored over the sinusoidal model (1Co+ sinusoidal). Additionally, the model incorporating the simultaneous QP-GP kernel displays moderate statistical favorability compared to the simultaneous EXP-GP kernel. We note that for the 1Co+sinusoidal model, we have a bimodality in the posterior distribution of the stellar rotation period at 29 d and a much smaller peak at about 31 d, which might be explained by differential stellar rotation.

In addition to the different planetary models and one no-planet model explored above, we extended our analysis to encompass two GP-only (EXP-GP and QP-GP) models (see Table 2). These models exhibit a higher statistical strength than those when considering the planet alone (1Co and 1eccentricity-free), suggesting that the presence of RV variabilities is primarily driven by dominant stellar activity signals rather than a planetary influence. However, a detailed examination outlined in Table 2 reveals a strong preference: models incorporating both the planet candida with the GP components are strongly favored ($\Delta \ln Z \geq \sim 5$) over GP-only models. This robust preference, the consistency of planet parameters across various models, and the detection of a strong periodicity in our periodogram analysis (refer to Sect. 5), coupled with the consistent phase and amplitude of the signal (refer to Sect. 5), ensures the credibility of our detection.

Finally, for the sake of completeness, we incorporated all RV data presented in this paper, with the exception of ELODIE, owing to its significantly larger error bars (approximately 8 times larger) in comparison to other datasets. This additional model aimed to assess the consistency of the remaining RV data with the results obtained from SOPHIE+ RVs. To account for the long-term curvature in the data, we applied a two-Keplerian model. Our analysis yielded consistent results (Period = 146.9 ± 0.3 d, $K = 1.7 \pm 0.2$ m s⁻¹, $T_c = 58 903 \pm 3$) when compared with other models listed in Table 2. After removing the second Keplerian orbit, the RV RMS values were 5.5 m s⁻¹, 5.6 m s⁻¹, 6.2 m s⁻¹, and 3.2 m s⁻¹ for HIRES, HIRES+, SOPHIE, and SOPHIE+ respectively. These RMS values, coupled with the limited number of available data points and sparse sampling of data from instruments other than SOPHIE+, indicate the challenges faced in detecting signals of such shallow amplitude in the other datasets beyond SOPHIE+. Additionally, this reaffirms the

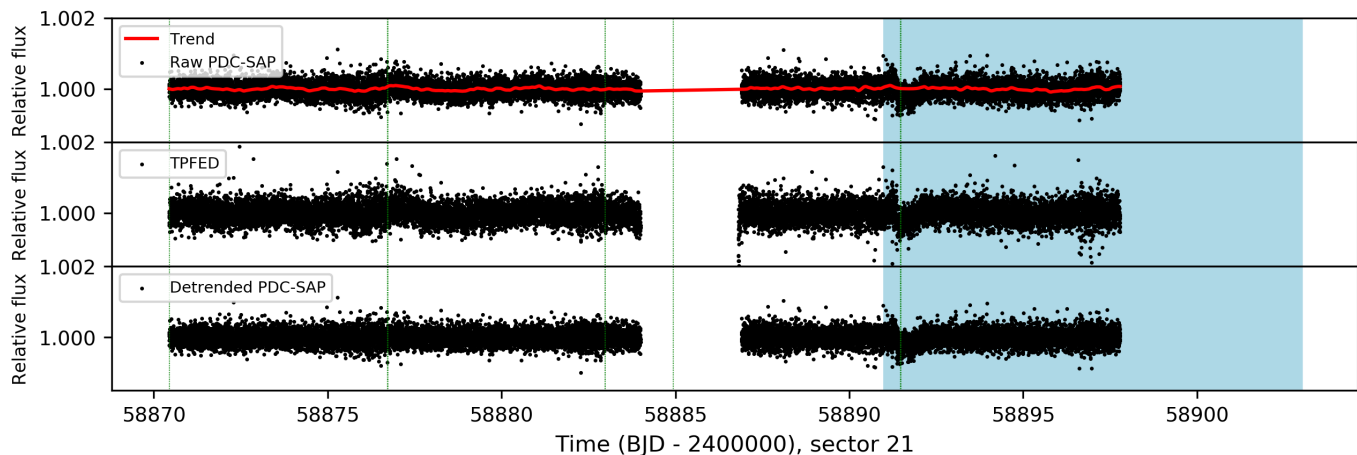


Fig. 6. TESS observation of HD 88986 in sector 21 in 2020 February. Top: normalized TESS PDC-SAP light curve of sector 21 (black dots) along with the best-fit trend (red curve) to the data. The green vertical lines represent the times of the spacecraft’s momentum dumps. Middle: normalized re-extracted light curve of sector 21 (black dots). See the text for more information. Bottom: final detrended light curve. The expected HD 88986 b transit event from SOPHIE+ RVs (Sect. 5.3), with 1 sigma uncertainties, is highlighted in blue, and a single transit event is found in the TESS photometric data within this region.

right selection of only SOPHIE+ data for presenting the detection and characterization of this low-mass planet, underscoring the accuracy of our results and ensuring the absence of additional instrumental offsets among the instruments. It is pertinent to highlight that satisfactory convergence was not achieved for certain parameters of the second Keplerian orbit, such as eccentricity and ω , as the orbit of this massive companion remains incomplete (see Sect. 9).

To conclude, the results of all investigated models agree within the error bars. Accordingly, we chose the 1Co+ QP-GP model on SOPHIE+ data as our final choice because it is strongly favored statistically over the model without GP and has moderate favorability compared to the Co+ EXP-GP model.

6. First transit detected in TESS sector 21 in February 2020

HD 88986 was observed in TESS sector 21⁴ with camera 1 in a 2-minute cadence from 2020 January 21 to 2020 February 18. The photometric data were produced by the Presearch Data Conditioning-Simple Aperture Photometry (PDC-SAP) pipeline (Stumpe et al. 2012, 2014; Smith et al. 2012), provided by the Science Processing Operations Center (SPOC; Jenkins et al. 2016) at NASA Ames Research Center. The normalized raw TESS photometric data are plotted in the top panel of Fig. 6.

TESS data from sector 21 revealed a potential single transit candidate with $T_c = 2\,458\,891.6$ (corresponding to 2020 February 12), a duration of about 16 h, and a depth of ~ 220 ppm. Remarkably, this T_c is in agreement, within uncertainty, with all the T_c values predicted above from the RV fits of HD 88986 b (Sect. 5.3, Table 2). We note that, neither the TESS SPOC nor Quick Look pipelines (QLP) detected this transit signature, as they require at least two transits to generate a Threshold Crossing Event (TCE) that would be vetted by the TESS Science Office.

To investigate whether that potential single, shallow transit in sector 21 is a false positive scenario, we performed a test by calculating the mean in-transit and mean out-of-transit flux, along

with the difference between them (see Fig. G.1). This approach allows us to examine the offset between the different image positions and the actual position of the target star, providing valuable insights into false positive scenarios. While interpreting the difference images from saturated stars like HD 88986 is particularly challenging, we observed that most of the energy in the transit feature is associated with the upper end of the bleed of the saturated pixels in the core of the stellar image. Therefore, it is likely that the transit feature is indeed associated with the host star.

Additionally, as Fig. 6 shows, a telescope reaction wheel momentum dump occurred during the transiting event (Fausnaugh et al. 2020). The sector 21 light curve seems to have been only minimally impacted by the other momentum dumps occurring within this sector. This suggests the robustness of the applied momentum dump correction. However, to ensure that the signal is not the cause of a pipeline’s imperfect momentum correction and produces an ingress-like feature, we re-extracted the light curve.

To do so, we use the TPFED/FFIED tool (hereafter TPFED) recently developed by Wilson et al. (2023) to conduct custom extractions of the TESS sector 21 data using the calibrated target pixel files (TPFs) with the default quality bitmask. In brief, we extracted target fluxes for a range of custom aperture masks created with radii of two to four pixels in steps of 0.1 pixels centered on the target. It should be noted that as the target does not fall in the exact center of a pixel increasing the aperture mask radius by 0.1 pixels can result in unique noncircular masks. All produced light curves were background-corrected after determining the sky level using custom background masks. We then detrended the data using two methods. Firstly, we conducted Principal Component Analyses (PCA) on the pixel values within our custom background masks to determine the scattered-light flux contribution to the light curves and then removed these systematics by using the five prime principal components as basis vectors in a linear model. Secondly, we corrected flux modulation due to spacecraft jitter by retrieving the co-trending basis vectors (CBVs), and two-second cadence engineering quaternion measurements for the cameras that observed HD 88986. Following the method used in Delrez et al. (2021), we computed the means and averages of the quaternions over the scientific observational cadences and subsequently used these

⁴ <https://heasarc.gsfc.nasa.gov/cgi-bin/tess/webtess/wtv.py>

vectors along with the CBVs to remove any flux trends. The final light curve is presented in the middle panel of Fig. 6, and the potential single transit is clearly seen within the dataset.

In a quest to further explore possible sources of instrumental noise that could impact the detection or shape of the potential, shallow single transit, we explored alternative methodologies following Rapetti et al. (in preparation). We used the adaptation of the technique Pixel Level Decorrelation (hereafter PLD; Deming et al. 2015; Luger et al. 2016, 2018) implemented in the PLDCorrector class of the community Python package Lightkurve⁵. This method employs (i) a spline polynomial fit to describe stellar variability, (ii) PCA eigenmodes to model the background light, and (iii) the PLD technique to account for pointing and mechanical effects. As an additional approach, we employed a version of PDC as adapted in the CBVCorrector class of Lightkurve, utilizing the CBV technique that the PDC method of the SPOC pipeline employs (hereafter we refer to this corrector as CBV).

Before applying the PLD, we added the background flux and errors estimated by the TESS SPOC pipeline back onto the SAP light curve. Flux level, fraction, and crowding adjustments are applied to the corrected light curves. To automatically optimize the selection of parameter values for the correctors, we evaluate the resulting light curve using the Savitsky-Golay Combined Differential Photometric Precision (sgCDPP) proxy algorithm (Gilliland et al. 2011; Van Cleve et al. 2016) implemented in Lightkurve, for durations of 30, 60, 120, 160, and 200 min (see the legend of Fig. G.2). For a grid of corrector parameter values (for further details on the parameters and the grid, see Rapetti et al., in prep.), we calculated the harmonic mean (HM) of these quantities and selected the corrected light curve that minimizes the HM. In addition, the final sgCDPP metrics can be compared to those obtained for the SPOC PDC-SAP corrected light curve (see Fig. G.2). For this comparison, we also calculated the over-fitting metric implemented in Lightkurve (see Fig. G.2) to measure the broad-band power spectrum via a Lomb-Scargle periodogram and assess the level of introduced noise in the corrected light curves.

In addition to the methods detailed above for extracting data from the 2-min TPFs, we extracted the full frame image (FFI) light curve from the TESS image using a strategy similar to Vanderburg et al. (2016). In particular, we created 20 different photometric apertures, 10 circular apertures, and 10 shaped like the TESS point spread function at the star location on the detector. We then calculated light curves from each aperture and corrected for systematics by performing a linear least-squares fit modeling on the light curve with time series the mean, standard deviation, kurtosis, and skew of the spacecraft quaternion measurements within each exposure (e.g., Vanderburg et al. 2019), the SPOC PDC CBVs, the background flux time series, and a basis spline to model slow variability. We performed the least-squares linear fit iteratively, removing outliers until convergence. Once the light curves were corrected for systematics, we corrected for dilution from other nearby stars and identified the one with the best photometric precision, which we used for our FFI analysis. The final resulting light curve is plotted in Fig. G.3.

The TESS light curves of sector 21, produced using different approaches, all find a feature where the potential single, shallow transit was identified (see Figs. 6, G.2 and G.3). Additionally, its mid-time always agrees with the predicted T_c reported in Sect. 5 for HD 88986 b, whatever the chosen RV model is (see Table 2). Furthermore, the feature exhibits fair similarity and

robustness across various tested approaches for correcting the instrumental variation in the TESS data. The consistent detection of this feature through various methodologies, combined with its robust nature, supports the fact that this feature is unlikely to be attributed to instrumental effects. However, the precise shape of the transit is not clearly discernible in the SAP data (as seen in the first panel of Fig. G.2). This lack of clarity is expected due to a momentum dump occurring at the time of the transit, in particular for such a shallow transit. Similar to other instances of momentum dumps observed in the SAP data, this event introduces instrumental variations. Additionally, the SAP data is not fully corrected for the scattered light that might affect the exact shape of the potential single transit. Given the robustness of the feature, as well as the fact that the observed T_c of the potential single transit agrees, within uncertainties, with the T_c obtained from all the RV-only models (see Sect. 5), it is likely that this feature corresponds to a single transit attributed to HD 88986 b.

We chose PDC-SAP data for our final analysis as all the newly extracted light curves are fairly consistent with the PDC-SAP light curve. We detrended the light curve using GP with an approximate Matern kernel introduced in Foreman-Mackey et al. (2017). The reason for this choice is that there is no evidence of existing quasi-periodic oscillations in the TESS light curves. Before applying this method to more accurately measure the planet's radii, we masked out the in-transit and immediately surrounding data points. The final detrended light curve is shown in Fig. 6 bottom panel, which we use for the rest of this work. We note that no additional signal was found by performing a Transit Least Squares (Hippke & Heller 2019) algorithm on this data.

Additionally, we searched for any potential light contamination caused by neighboring stars on the light curve of HD 88986. Within the aperture set by PDC-SAP, there is only one neighboring star. Because this star is one of the ~ 1 million new *Gaia* DR3 sources, its light contamination is not corrected by SPOC. This star has a magnitude of $G = 12.3$ ($\Delta G_{\text{mag}} = 6$ compared to HD 88986) and is located $1.4''$ west of HD 88986. There are no values for RP magnitude and renormalized unit weight error (RUWE), which is a measurement of the goodness of the star's astrometric solution. The poor behavior of this star could be due to blending with HD 88986. Because the *Gaia* RP bandpass is comparable to the TESS bandpass, one can assess the level of contamination using the *Gaia* RP fluxes of these stars. In our case, however, the lack of RP flux data for the neighbor star prevents us from estimating the contamination effect.

7. Joint analysis of SOPHIE+ and TESS sector 21

We performed a joint modeling of TESS photometric data of sector 21 and SOPHIE+ RVs using juliet. juliet, in addition to the packages mentioned above for RV modeling (see Sect. 5.2), employs batman (Kreidberg 2015) for transit fitting. Following the RV-only study in Sect. 5, we used the planet model with a simultaneous QP-GP model for modeling RVs in our joint modeling. Here, we tested both eccentricity free and zero models, as combining RV and transit data provides more constraints to fitting the orbital parameters including eccentricity and the argument of periastron. We employed the same priors for RV-related parameters, as detailed in Sect. 5, with the exception of T_c . For T_c , we set a Gaussian prior centered at 58 891.6 with a standard deviation of 5 d. To parameterize the limb darkening coefficient for TESS photometry, we applied a linear law through a parameter of q . This choice is motivated by the limited number of informative in-transit data points when modeling

⁵ <https://docs.lightkurve.org>

Table 3. Median values and 68% confidence interval of parameters for HD 88986 b based on the joint analysis of the photometric and RV data by *Juliet* (see Sect. 7 and Fig. 8).

Parameter (unit)	Posterior HD 88986 b
Stellar parameters:	
ρ_* (kg m ⁻³)	472 ⁺³⁸ ₋₃₅
Planet parameters	
P^* (d)	146.05 ^{+0.43} _{-0.40}
T_c (BJD-2 400 000)	58 891.690 ± 0.003
K (m s ⁻¹)	1.85 ± 0.34
e	0.24 ± 0.05
ω (°)	306 ⁺¹⁰ ₋₁₁
R_p/R_*	0.0148 ± 0.0004
b	0.21 ^{+0.17} _{-0.14}
a/R_*	81.1 ± 2.1
TESS instrumental parameters:	
M_{TESS} (ppm)	-0.0000001 ± 0.0000014
$\sigma_{\omega, \text{TESS}}$ (ppm)	143.4 ± 1.3
$q1$	0.27 ^{+0.17} _{-0.14}
SOPHIE+ instrumental parameters:	
$\sigma_{\text{SOPHIE+}}$ (m s ⁻¹)	2.09 ^{+0.16} _{-0.17}
$\mu_{\text{SOPHIE+}}$ (m s ⁻¹)	29 090.6 ± 0.4
Drift on SOPHIE+:	
A (m s ⁻¹)	0.0165 ± 0.0003
Q (m s ⁻¹)	0.0000039 ± 0.0000002
QP-GP on SOPHIE+:	
B_{GP} (m s ⁻¹)	4.0 ^{+1.1} _{-0.8}
C_{GP} (m s ⁻¹)	10 ⁻²⁰ (fixed)
P_{rot} (d)	30.0 ± 2.0
L_{GP} (d)	29 ⁺³⁷ ₋₁₈
Derived planet parameters:	
a (au)	0.58 ± 0.04
i (°)	89.9 ± 0.1
R_p (R_{\oplus})	2.49 ± 0.18
M_p (M_{\oplus})	17.2 ^{+4.0} _{-3.8}
ρ_p (g cm ⁻³)	6.1 ^{+3.3} _{-2.3}
T_{eq} (K)	460 ± 8

Notes. (*)See the refined period in Table 4.

single transit events (Sandford et al. 2019). We note that applying a quadratic limb-darkening law had no effect on our final results. Additionally, the results of the spectral analysis provided in Sect. 3 were used to set a Gaussian prior to the star density ρ_* . Finally, we added a jitter term of σ to TESS photometric data. Table H.1 shows all of the employed priors and the description of the parameters.

The joint modeling of TESS sector 21 and SOPHIE+ RVs with eccentricity-free and circular orbits yields consistent results. However, the eccentricity-free model exhibits strong statistical favorability ($\Delta \ln Z > 9$). Therefore, we present the resulting parameters of this model in Table 3 and depict its best-fit on combined photometry and RVs in Fig. 7. A corner plot of all parameters is included in Appendix J.1. We note that the

dilution factor was not taken into account in our analysis. This is due to the fact that when a wide uniform prior range of 0–1 is used, the dilution value tends to converge toward the lower edge of the prior 0. This outcome is unacceptable because there is only one faint nearby star in the TESS aperture, and it is approximately 6 mag fainter than the primary star in the G band (refer to Eq. (6) of Espinoza et al. 2019 for more details). Such behavior can be expected in transits with low S/Ns (Espinoza et al. 2019). Additionally, due to the unavailability of *Gaia* RP magnitude for the neighbor star, we were unable to estimate and constrain the dilution factor accurately. However, considering that the neighbor star is faint, we expect any contamination effect from it to be negligible.

Based on our final parameters, the transiting planet HD 88986 b is a sub-Neptune with a period of 146.05^{+0.43}_{-0.40} d. It exhibits an eccentricity of 0.23 ± 0.06, alongside a radius of 2.49 ± 0.18 R_{\oplus} and a mass of 17.2^{+4.0}_{-3.8} M_{\oplus} , corresponding to a high mean density of 6.1^{+3.3}_{-2.3} g cm⁻³. Additionally, the planet has an equilibrium temperature of 460 ± 8 K ($T_{\text{eq}} = T_* \sqrt{(R_p/2a)}$, Méndez & Rivera-Valentín 2017), making it a relatively cool planet.

8. Search for a second transit with additional photometric data

The analysis presented above in Sect. 7 predicts another transit of HD 88986 b should have occurred in 2022 February. We used CHEOPS and TESS sector 48 to attempt the detection of the second transit.

8.1. CHEOPS photometry

The CHEOPS spacecraft is a 30 cm ESA space telescope (Benz et al. 2021) that conducts ultra-high-precision photometry to characterize planets (Bonfanti et al. 2021; Delrez et al. 2021; Lacedelli et al. 2022) and their atmospheres (Lendl et al. 2020; Hooton et al. 2022), but it has also been used to aid in the discovery of new planets (Leleu et al. 2021; Osborn et al. 2022; Serrano et al. 2022; Wilson et al. 2022).

As derived in Sect. 7, the period of HD 88986 b is 146.05^{+0.43}_{-0.40} d. We predicted that the next transiting event would fall within the region of the TESS sector 48 which includes the gap between orbits. Therefore, to search for a second transit event, we obtained one visit of CHEOPS observation (PI: N. Heidari) spanning 167.4 h between 2022-02-08 and 2022-02-15 with an exposure time of 3.4 s. This allowed us to cover the transit period's uncertainty from joint analysis of RVs and sector 21 by $\sim 2\sigma$ and the TESS gap to be covered.

The data were processed with the latest version of the CHEOPS Data Reduction Pipeline (DRP v13; Hoyer et al. 2020) that conducts frame calibration, instrumental and environmental correction, and aperture photometry using predefined radii ($R = 22.5''$, $25.0''$, and $30.0''$) as well as a noise-optimized radius. The DRP-produced flux contamination was subtracted from the light curves. We retrieved the data and corresponding instrumental basis vectors and assessed the quality using the PYCHEOPS Python package (Maxted et al. 2022) and found that the DEFAULT aperture minimized the root mean square (RMS) noise. Therefore, we used this aperture for our further analysis. These are plotted in the upper panel of Fig. 8, on which the expected time of the transit, derived from the SOPHIE+ RVs and TESS sector 21 joint analysis (Sect. 7), is indicated in blue.

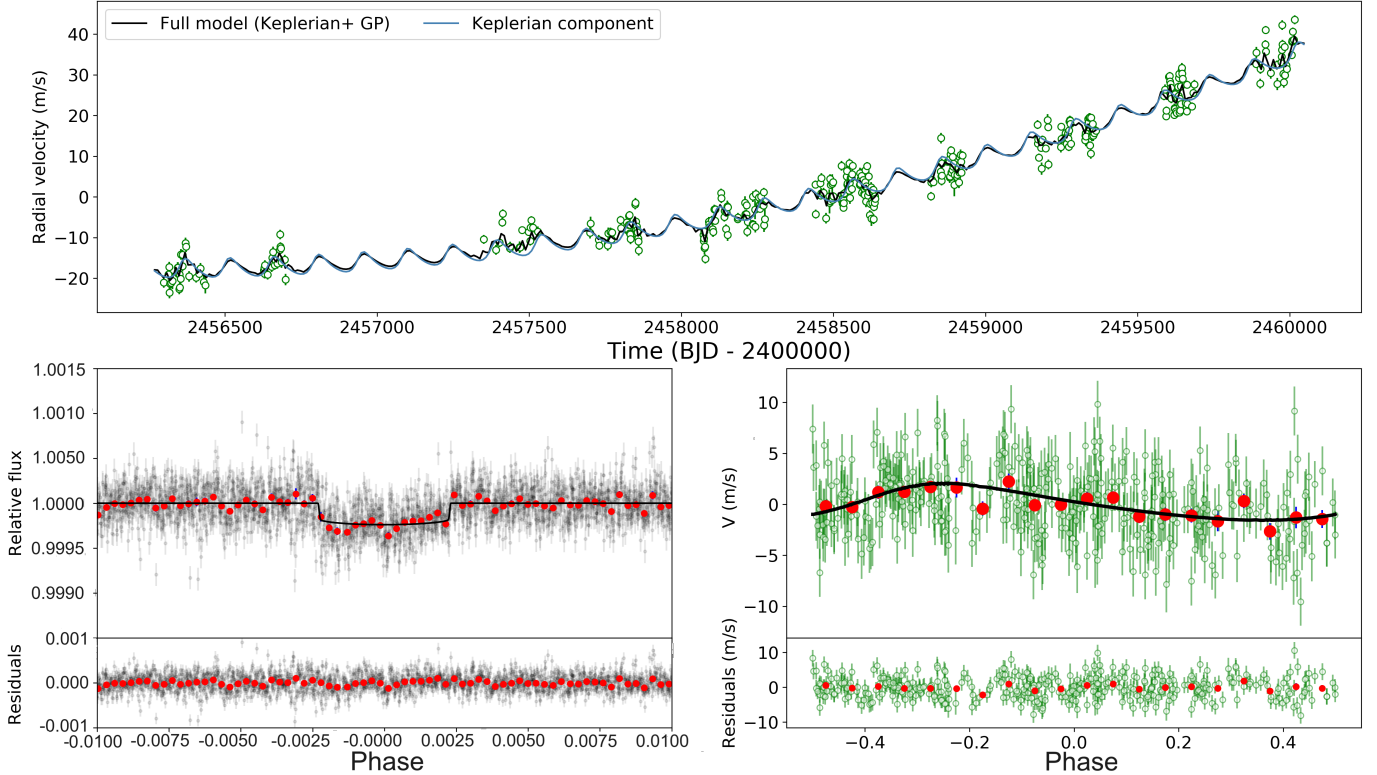


Fig. 7. Joint analysis of SOPHIE+ and TESS sector 21 observations of HD 88986 b. Top: SOPHIE+ data overplotted by the best-fit orbit model. Bottom-left: phase-folded TESS PDC-SAP photometric data of sector 21. The data are binned (red points) in 1 hour. The black line shows the best-fit transit model. Bottom-right: phase-folded SOPHIE+ RVs of HD 88986 b at the period of 146.05 d. The red points depict the binned data, utilizing a bin size of 0.05 in orbital phase units. The black line represents the best-fit orbit model.

In previous studies, it has been noted that environmental effects (i.e., spacecraft temperature and illumination) and the presence of nearby contaminants can induce flux modulation in light curves (Morris et al. 2021; Maxted et al. 2022; Wilson et al. 2022). In order to correct for these effects and search for the smallest transit signals in our transit search analysis, we conduct a principal component analysis on the auto-correlation function of the CHEOPS frames using the methodology detailed in Wilson et al. (2022). The process has been shown to monitor PSF shape changes, and so any effects that alter the CHEOPS PSF, such as environmental and contamination effects, are measured by this tool and can be removed by using the produced principal components as the basis vectors in a linear model detrending. Further examples of applications of this tool can be seen in Hoyer et al. (2022); Ehrenreich et al. (2023); Hawthorn et al. (2023).

To assess the existence of a transiting body with the CHEOPS observations, we conduct a statistical analysis using a newly developed tool Wilson et al. (2023). In brief, we use the PSF-based PCA components produced following (Wilson et al. 2022) above in combination with the instrumental basis vectors to construct a linear noise model that is fit simultaneously with either a 0 or 1 planet transit model that allows us to compute the True and False Inclusion Probabilities (TIP and FIP; Hara et al. 2022b) for the presence of transit in the data. These are calculated using the Bayes Evidences and posterior distributions of the 0 and 1 planet fits. For this study, we conduct this analysis twice: one with a period prior constrained by the transit model from the RV data and the second time with no period prior. For both cases and for all transit T_0 values within the CHEOPS dataset, we find FIP ~ 1 , which statistically means that there is no transit in the lightcurve.

This non-detection by CHEOPS leads to two potential conclusions: (1) the rejection of the presumed transit event in TESS sector 21 as a spurious feature, or (2) the transit might be occurring at a time that deviates more than $\sim 2\sigma$ away from our predicted ephemeris. We note that although the CHEOPS data did not reveal any transit features, this observation was valuable in covering the gap in TESS sector 48 data (see Sect. 8.2 and Fig. 8), substantially contributing to the refinement of the planet’s period.

8.2. TESS photometry sector 48

TESS conducted a second observation of this star with a cadence of 2 minutes, spanning from 2022 January 28 to February 26. The PDC-SAP data provided by SPOC from this observation is depicted in Fig. 8 (second panel). Remarkably proximate to the 3σ anticipated transit region, as determined through the joint modeling of RVs and TESS sector 21 data, a second potential transit-like feature with a T_c of about $\sim 59\,628.8$ and a period of 147.4 d from the first transit is observed in the figure. We note that it was particularly lucky to cover two transits of that long-period planet with TESS, as only two sectors of TESS covered that star.

Similar to the first potential transit in sector 21, we tested the mean in-transit and mean out-of-transit flux, along with the difference between them (see Fig. G.1). This test confirmed that the feature in sector 48 is likely related to the host star. However, in contrast to sector 21 with a standard deviation of $\sigma = 204.4$ ppm, TESS sector 48 displays a substantial dispersion with $\sigma = 635.8$ ppm. This noticeable difference might be linked to the

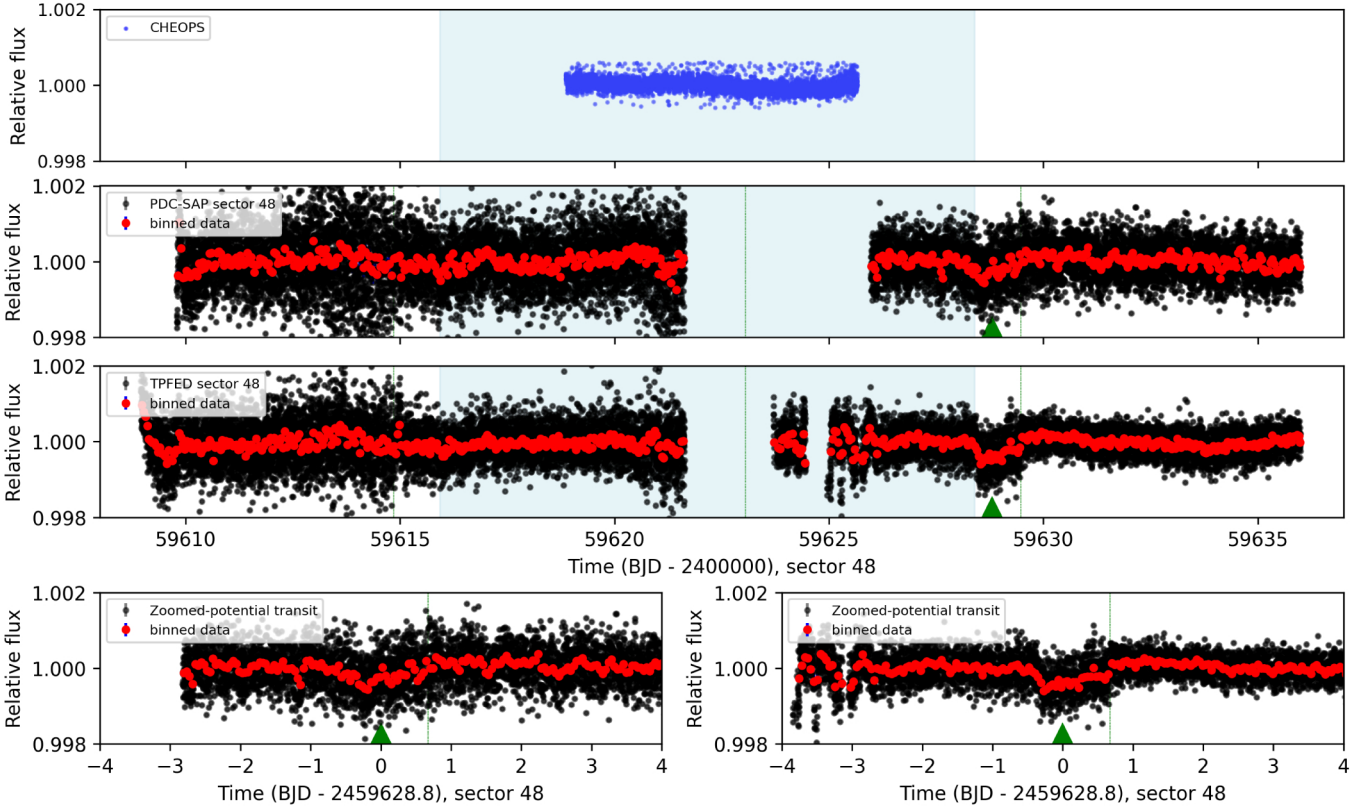


Fig. 8. CHEOPS and TESS observations of HD 88986 in 2022 February. The predicted time of HD 88986 b’s second transit event, based on the best-fit model of combining RVs and the photometric light curve of sector 21 (see Sect. 7), is highlighted in blue. Top: CHEOPS photometric data. Second: TESS (black dots) PDC-SAP light curve of sector 48. The TESS data are binned (red points) in 1-hour increments. The potential transit-like feature is marked by a green triangle. The vertical dashed, green lines are the spacecraft momentum dumps. Third: re-extracted TESS light curve (see the text for more explanation). Bottom: zoomed on the potential transit event of HD 88986 b on PDC-SAP (left) and re-extracted (right) data. As the plot indicates, the two light curves are noticeably different. As a result, we did not include those data in our joint analysis presented in Sect. 7.

presence of residual systematics that may have persisted even after the SPOC correction.

Therefore, following the methodology outlined in Sect. 6 using the TPFED tool, we conducted a customized extraction of TESS sector 48. The photometric results obtained from this approach are presented in Fig. 8 (third panel), with the transit-like feature zoomed in for better visualization (fourth panel). While the resulting custom extraction of the TESS light curve for sector 21 was fairly similar to the SPOC light curve, they are noticeably different for sector 48 (fourth panels).

To further explore the potential source of instrumental noises, similar to sector 21, we also extracted the light curve using PLD and CBV approaches from 2-min TPFs cadence, along with the FFI data (see Sect. 6 for more information about the methods). The resulting extracted data (see Figs. G.2 and G.3) following these methods also confirmed the noticeable difference between PDC-SAP data and the independently extracted light curves. Moreover, the variations within the transit further complicate our understanding of the TESS photometric data in sector 48, leading to its exclusion from our analysis. Additionally, we note that by the inclusion of PDC-SAP data of sector 48 in our joint modeling, the final results remain consistent compared to our model with only RVs and sector 21 in Sect. 7.

Figure G.4 shows the phase-folded TESS PDC-SAP and FFI data for sectors 21 and 48 corresponding to the 147.4 d period. We note that the FFI light curve is detrended by the

Table 4. Possible solution for HD 88986 b’s period.

Models	HD 88986 b’s period
RVs-only	146.3 ± 0.6
RVs+ sector 21	146.1 ± 0.4
RVs+ sector 21+ sector 48	147.4 ± 0.1

spline approach using the Wotan package (Hippke et al. 2019). While the consistency between the two potential transits in the PDC-SAP data remains uncertain, the two transits exhibit good consistency within the FFI data, particularly concerning transit depth and duration.

In Table 4, we summarize all the possible period solutions for HD 88986 b, including the periods obtained through the final choice of the RV-only model (see Sect. 5.2), combined RVs with TESS sector 21 (see Sect. 7), and combined RVs with both TESS sector 21 and 48. The orbital period derived from RV data combined with two potential transits agrees (at 3σ) with the period calculated using RVs and single transit in sector 21, and also agrees (at 2σ) with the RV-only period. One could expect an even better agreement; possible persistent instrumental effects not perfectly taken into account in our models might be the cause. This agreement between all period solutions, arguing here for an actual detection of a transit of HD 88986 b. Still, the noise

in sector 48 light curve and the differences between reduction methods keep us prudent about the transit detection in sector 48, which we chose not to include in our final fit (Sect. 7). Conducting follow-up photometric observations for this system, with the goal of identifying HD 88986 b's second transit event, would strongly confirm that the planet is transiting while also providing a much better constraint on the planet's period.

9. Constraining a long-term companion

In this section, we examined different scenarios to determine the origin of long-term curvature seen in the RVs in addition to HD 88986 b. Stellar activity or a wide-orbit companion are two possibilities. To explore them, we used long-term photometric data obtained with the T8 APT, the combined RVs from ELODIE, HIRES, and SOPHIE instruments, as well as astrometric data from *Gaia* and HIPPARCOS.

9.1. APT photometric observations

To characterize the origin of long-term curvature observed in RVs (see Fig. 1), we used 1335 photometric observations of HD 88986 covering 21 observing seasons from 1995–1996 to 2019–2020, except the four observing seasons 2015–16 through 2018–19, during which the star was not observed. The observations were acquired with the T8 0.80 m APT at Fairborn Observatory in southern Arizona. The T8 APT is equipped with a two-channel photometer that uses two EMI 9124QB bi-alkali photomultiplier tubes to measure the stellar brightness simultaneously in the Strömgren *b* and *y* passbands.

The observations are made differentially with respect to three nearby comparison stars. We measured the difference in brightness between our program star HD 88986 (star d) and the comparison stars (stars a: HD 89557 ($G = 7.3$ mag, G8 III), b: HD 87667 ($G = 7.3$, F5), and c: HD 88476 ($G = 6.6$, G8 III)) and created differential magnitudes in the following six combinations: d-a, d-b, d-c, c-a, c-b, and b-a. Intercomparison of these six light curves shows that the comparison star a (HD 89557) is the only one that appears to be constant to the limit of our precision, so we present our results as differential magnitudes in the sense star d minus star a, which we designate as d-a.

To improve the photometric precision of the individual nightly observations, we combined the differential *b* and *y* magnitudes into a single $(b+y)/2$ passband. The precision of a single differential observation with T8, as measured from pairs of constant comparison stars, typically ranges between 0.001 mag and 0.0015 mag on good nights. The T8 APT is described in Henry (1999), where further details of the telescope, precision photometer, and observing and data reduction procedures can be found.

Figure 9 plots the 1335 nightly observations in the $(b+y)/2$ passband photometry from d-a obtained across the 21 observing seasons as small filled circles. The mean of all the nightly observations, -1.16492 mag, is plotted as the dashed line in the figure. The standard deviation of the nightly observations from their mean is 0.00118 mag, consistent with the precision of the measurements. The 21 seasonal means of these data are plotted as large filled circles. The standard deviations of the individual seasonal means are roughly the size of the plot symbols. The standard deviation of the 21 seasonal means from the mean of the seasonal means is 0.00028 mag, indicating that there is no long-term variability in HD 88986 to the limit of our photometric precision.

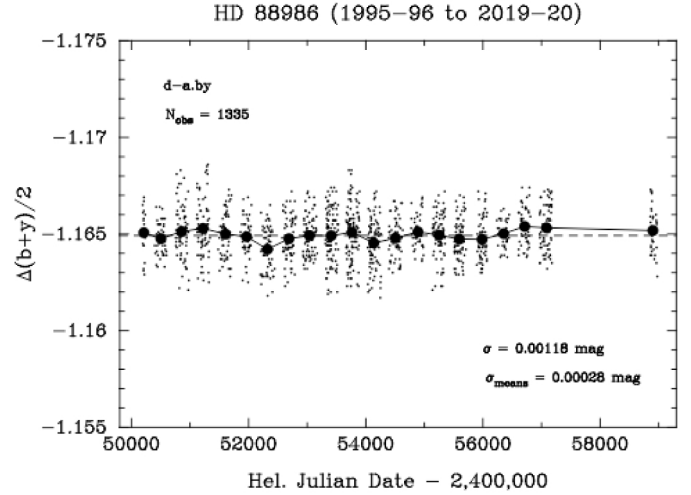


Fig. 9. Nightly Strömgren $(b+y)/2$ band photometry of HD 88986 from 21 observing seasons from 1995–96 to 2020–21 (small filled circles) scatter about their mean (dashed line) with a standard deviation of 0.00118 mag. Seasonal means from the 21 seasons (large filled circles) scatter about their mean with a standard deviation of 0.00028 mag. No significant variations nor periodicities are detected.

Table L.1 summarizes observations in the $(b+y)/2$ passband photometry from d-a. The standard deviations of the nightly observations for each observing season indicate little or no short-term variability within each observing season. Frequency analysis of each individual observing season using the method of Vaníček (1971) confirms the lack of any periodic variability. Henry et al. (2022) show extensive examples of this method of period analysis.

In a study conducted by Lovis et al. (2011), the activity cycles of 311 FGK stars were analyzed. It shows that RV semi-amplitudes can be induced up to approximately 25 m s^{-1} by the stellar long-period activity. However, in the case of HD 88986, the long-period RV semi-amplitude is at least about 40 m s^{-1} (see the SOPHIE+ RVs in Fig. 7), and also as stated in this section, there is no evidence of long-term photometric variability up to the limits of our precision. This suggests that the origin of this long-term curvature is likely unrelated to stellar activity and instead points toward the presence of a third body in the system.

9.2. Combining RV and HIPPARCOS/*Gaia* astrometry data

In order to improve the characterization of the outer massive companion, we modeled simultaneously the available RV and absolute astrometry data. The use of an MCMC algorithm enables us to explore the different solutions for each orbital parameter and for the companion mass compatible with the data. This algorithm, introduced by Philipot et al. (2023), is used to fit Keplerian orbits based on the emcee 3.0 (Foreman-Mackey et al. 2013) and HTOF (Brandt et al. 2021a) packages. The likelihood computation is similar to that of the ORVARA code (Brandt et al. 2021b).

We considered the ELODIE, SOPHIE, SOPHIE+, HIRES, and HIRES+ RV data, presented previously, coupled with the proper motion and position values calculated in the HIPPARCOS-*Gaia* Catalog of Accelerations (Brandt 2021) from HIPPARCOS (Perryman et al. 1997; van Leeuwen 2007) and *Gaia* data release 3 (DR3; Gaia Collaboration 2016, 2021) measurements. For the fit, we considered a Gaussian prior for the stellar mass and parallax, based on the values published

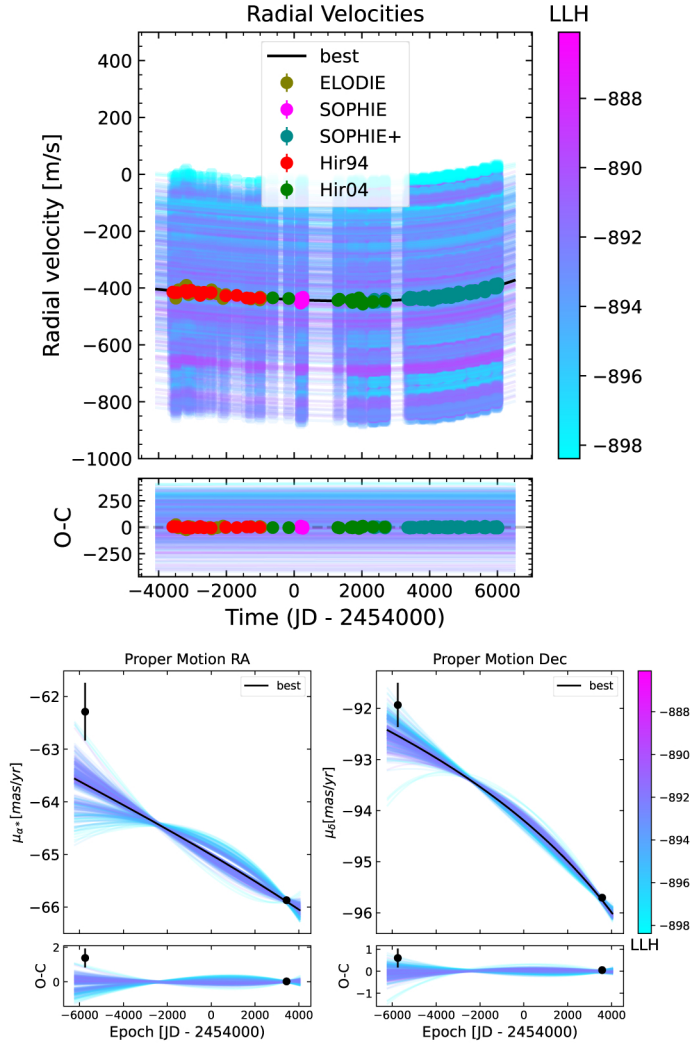


Fig. 10. Orbital fits for HD 88986 outer massive companion. Top: fit of the HD 88986 RV data points. Bottom: fit of the HD 88986 proper motion measurements in right ascension (left) and declination (right). The black points correspond to the HIPPARCOS and *Gaia* EDR3 data points. In each plot, the black curve corresponds to the best fit. The color bar indicates the log-likelihood corresponding to the different fits plotted.

by Kervella et al. (2022), and a $\sin(I)$ prior for the orbital inclination. For the semi-major axis (a), the companion mass, the eccentricity, the longitude of the ascending node, the argument of periastron, the periastron passage time, and the jitter, we set uniform priors. In addition, as we use RV data from different instruments, we added an instrument offset for each dataset, also with uniform priors.

As the mass of HD 88986 b is low and its orbital period much smaller than the HIPPARCOS and *Gaia* DR3 observation windows (1227 and 1038 d, respectively), the proper motion variation of HD 88986 induced by the planet HD 88986 b is negligible. We have therefore only fitted the orbit of the outer massive companion (Fig. 10). However, as the RV data covers only a small part of the RV variation due to the outer companion, the star's RV remains poorly constrained and a wide range of solutions is compatible with the data, with similar likelihood values. We thus obtain an interval, with a confidence index of 3σ , between 16.7 and 38.8 au for the semi-major axis, 16 and 169° for the orbital inclination, and 68 and $284 M_{\text{Jup}}$ for the true mass

Table 5. Median values and 68% confidence interval for parameters of the outer companion of HD 88986 based on the joint analysis of the HIPPARCOS/*Gaia* astrometric and RV data.

Parameter (unit)	The outer companion posteriors
Stellar parameters	
M_* (M_\odot)	$1.20^{+0.07}_{-0.06}$
Parallax (mas)	30.025 ± 0.023
σ_* (m s^{-1})	$3.3^{+0.2}_{-0.1}$
The outer companion parameters	
P (yr)	116^{+40}_{-34}
T_c (BJD-2 400 000 d)	$65\,000 \pm 2000$
a (au)	$26.2^{+6.4}_{-5.5}$
$\sqrt{e} \cos \omega$	$0.47^{+0.16}_{-0.24}$
$\sqrt{e} \sin \omega$	$-0.47^{+0.13}_{-0.10}$
e	0.46 ± 0.13
ω ($^\circ$)	$314.9^{+14.4}_{-21.4}$
I ($^\circ$)	$54.5^{+21.3}_{-18.8}$ or $135.5^{+18.4}_{-19.4}$
Ω ($^\circ$)	$29.1^{+8.5}_{-3.6}$
M_c (M_{Jup})	145^{+73}_{-48}
Instrumental parameters:	
μ_{ELODIE} (m s^{-1})	$29\,220^{+180}_{-110}$
μ_{SOPHIE} (m s^{-1})	$29\,320^{+180}_{-110}$
$\mu_{\text{SOPHIE+}}$ (m s^{-1})	$29\,320^{+180}_{-110}$
μ_{HIRES} (m s^{-1})	240^{+180}_{-110}
$\mu_{\text{HIRES+}}$ (m s^{-1})	240^{+180}_{-110}

of the companion (Table 5). Nevertheless, these results suggest that the outer massive companion is likely a brown dwarf or a low-mass star.

As previously mentioned, there is a *Gaia* DR3 source situated 1.4 arcseconds west of HD 88986. Considering HD 88986's parallax value for this source, its semi-major axis deviates by approximately 3.2σ from the resulting semi-major axis of the massive companion (see Table 5). Given the compatibility of the results with a wide range of solutions, it remains uncertain whether this source is the cause of the observed acceleration. Notably, this *Gaia* source lacks parallax information, raising the possibility that it might be a projected neighbor, unrelated to HD 88986.

9.3. Other constraints from *Gaia* astrometric excess noise

We used the *Gaia* data simulator from the *gaston* code first developed for the *Gaia* DR1 (Kiefer et al. 2019, 2021; Kiefer 2019) to test whether astrometric excess noises (AEN, hereafter) from the *Gaia* DR3 could lead to complementary mass constraints on the outer companion of HD 88986 at the orbital period found by coupling to the proper motions of HIPPARCOS and *Gaia*. The AEN is a measurement of supplementary motion, beyond proper motion and parallax, in the astrometric data of a source. The AEN is obtained from the RMS of residuals after fitting out the RA–Dec position, proper motion, and parallax to the simulated astrometric *Gaia* measurements by the approximate formula (see also Kiefer et al. 2019

Table 6. Resulting constraints on the orbital inclination and mass of companion “c”, and on the predicted photocenter semi-major axis of HD 88986, using the AEN from *Gaia* DR3.

Parameter	1σ	3σ limits
I_c (deg)	33^{+33}_{-18}	>2.7
M_c (M_{jup})	180^{+220}_{-80}	<810
a_{phot} (mas)	91^{+107}_{-47}	<440

and references therein):

$$\sigma_{\text{AL}}^2 + \sigma_{\text{attitude}}^2 + \text{AEN}_{\text{DR3}}^2 = \frac{\sum_j R_j^2}{N - 5} \quad (2)$$

where R_j are the N along-scan (AL) angle residuals of the astrometric fit; σ_{AL} is the typical AL angle measurement noise; σ_{attitude} is the spacecraft attitude excess noise, and AEN_{DR3} is the AEN. The AL angle measurement noise has a value of $\sigma_{\text{AL}} = 0.05$ mas for targets with a G -magnitude of 6.3 (Fig. A.1 from Lindegren et al. 2021), and the typical attitude noise in the DR3 is $\sigma_{\text{attitude}} = 0.076$ mas (Lindegren et al. 2021).

HD 88986 has a magnitude of $G_{\text{mag}} \sim 6.3$ and a color Gb–Gr of ~ 0.8 . In the *Gaia*-DR3 catalog, the typical AEN of single stars at that magnitude and color for sources fitted with five parameters, as HD 88986, is 0.14 mas. This nonzero AEN is present for nearly all single stars and is due to a systematic jitter, including instrumental and global modelization noises, that is accounted for in the formal errors used to calculate the χ^2 (Lindegren et al. 2021). The AEN of HD 88986 is $\epsilon_{\text{DR3}} = 0.135$ mas. The *Gaia* DR3 astrometry of this target is thus compatible with a single star without a companion, but it also allows deriving an upper-limit constraint on the mass of the RV-detected companion, given a range of possible orbital periods.

We follow the method from Kiefer et al. (2019, 2021), using the code *gaston* adapted to the (E)DR3. The general principle of the method is the same as with the DR1. Fixing P , $m \sin i$, e , ω and T_0 within their priors derived from combined RVs in Table 5, we run several simulations of *Gaia* measurements of the target along a model of the orbital motion of the system due to the outer massive companion and derive simulated values of AEN that we compare with the actual AEN_{DR3} .

We sample orbital inclination uniformly between 0 and 90° by an MCMC routine based on the *emcee* code (Foreman-Mackey et al. 2013) and thoroughly explained in Kiefer et al. (2019, 2021). The orbital inclination changes the amplitude of the astrometric motion due to a different mass of the companion determined from $M = m \sin i / \sin i$ and thus changes the value of the AEN allowing us to match a range of orbital inclinations to the observed AEN.

Noises, epochs, scan angles, and the number of measurements used in the simulations are updated with respect to the new data reduction of DR3 (Gaia Collaboration 2021). An epoch is a date when the star is transiting the *Gaia* field of view; several measurements, typically 9, are performed during a single transit. Those epochs can be found for any target in the *Gaia* Observation Forecast Tool (or GOST⁶). We add in our simulated model a jitter of 0.16 mas, allowing us to reproduce a median AEN of 0.14 mas for single sources at $G = 6.3$ and Gb–Gr = 0.8. It is

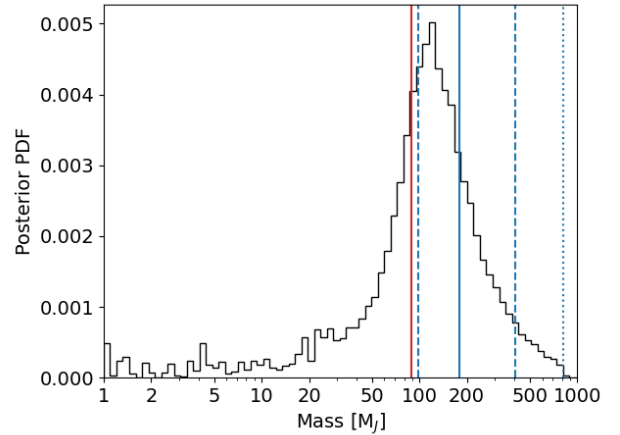


Fig. 11. Illustration of HD 88986 outer companion analysis using *Gaia* DR3 analysis showing the companion mass posterior distribution running *gaston*. The dotted line shows the 3σ upper-limit, the dashed lines show the 1σ confidence interval, the solid blue line is the median mass, and the solid red line shows the RV $m \sin i$.

modeled as a Gaussian noise changing every epoch of observation. The spacecraft attitude noise is also added to the model as a systematic Gaussian dispersion that changes every observation epoch with a standard deviation of 0.076 mas. A Gaussian measurement noise of $\sigma_{\text{AL}} = 0.05$ mas is added to each of the N_{AL} astrometric measurements performed at a given epoch.

Table 6 summarises the results of AEN fitting for this star. Fig. 11 shows the relation between AEN and inclination in the simulations and plots the posterior distribution of companion mass. The posterior distribution on mass gives an upper limit on the mass of the companion below $810 M_{\text{jup}}$ at 3σ . This result agrees with the one presented in Sect. 9.2. Finally, we adopted the results from Sect. 9.2 as it provides a higher level of precision in the mass and orbital inclination of the outer massive companion.

10. Discussion and conclusion

We discovered and have characterized HD 88986 b, a sub-Neptune in orbit around a subgiant star, which stands as one of the nearest and brightest ($V = 6.47$ mag) exoplanet host stars (see Fig. 12 top right). Our analysis indicates that this planet is transiting, based on two potential single transit detections in TESS sectors 21 and 48, both of which are consistent with the anticipated transit time from the RV model. By combining data from SOPHIE+ RV measurements and TESS sector 21 photometric data, we determined the following parameters for HD 88986 b: a period of $P_p = 146.05^{+0.43}_{-0.40}$ d, a mass of $M_p = 17.2^{+4.0}_{-3.8} M_{\oplus}$, and a radius of $R_p = 2.49 \pm 0.18 R_{\oplus}$, resulting in a high mean density of $\rho_p = 6.1^{+3.3}_{-2.3} \text{ g cm}^{-3}$. The two-layer theoretical composition model developed by Zeng et al. (2016) indicates that the planet is composed predominantly of rock, accounting for approximately 75% of its mass, while water makes up the remaining 25% (Fig. 12 bottom left). Additional photometric observations of the system targeting another transit event of HD 88986 b are needed. Such observations would provide a strong confirmation of the planet’s transiting nature and yield better estimates for its period and radius.

Additionally, we identified a clear long-term curvature in the RV caused by the presence of a massive companion in the system. The nature of this companion has yet to be confirmed. A

⁶ <https://gaia.esac.esa.int/gost/index.jsp>

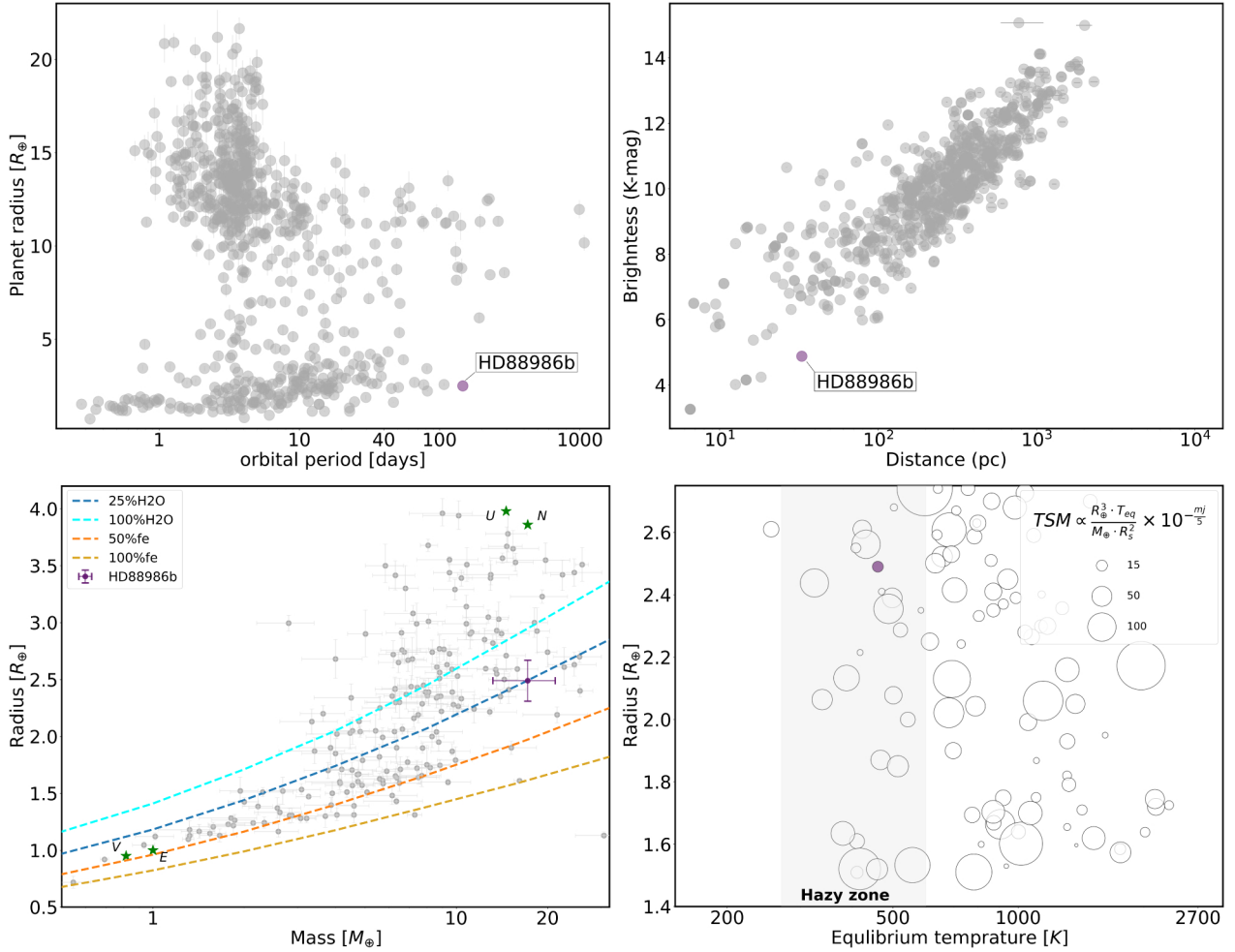


Fig. 12. Position of HD 88986 b and its host star among known transiting exoplanetary systems, with precise planet mass and radius measurements ($\sigma M/M = 25\%$ and $\sigma R/R = 8\%$, Otegi et al. 2020) from the NASA Exoplanet Data Archive (June 7, 2023). Top left: radius-period diagram of exoplanets. Top right: brightness in the K band versus distance of the exoplanet host star for the same planets. Bottom left: mass-radius diagrams of small planets ($R_p < 4 R_{\oplus}$). The colored curves are the two-layer theoretical composition models of Zeng et al. (2016). Bottom right: equilibrium temperature-radius diagram of planets within the radius range of $1.5 R_{\oplus}$ to $2.75 R_{\oplus}$ with each planet’s size scaled according to the propositional TSM introduced by Kempton et al. (2018). The gray area is the proposed hazy atmosphere zone by Yu et al. (2021). The purple mark indicates HD 88986 b. These planets possess either a known equilibrium temperature or information about the radius and temperature of their host star to estimate their temperature ($T_{eq} \sim T_* \sqrt{(R_p/2a)}$, Méndez & Rivera-Valentín 2017). These figures highlight the unique position of the HD 88986 system.

joint analysis of RV, HIPPARCOS, and *Gaia* astrometric data shows that with a 3σ confidence interval, its semi-major axis is between 16.7 and 38.8 au and its mass is between 68 and $284 M_{Jup}$. SOPHIE+ observations are being conducted to disclose the nature of this massive companion, and in particular better constrain its period and eccentricity. Furthermore, given its extensive semi-major axis, this outer massive companion presents an opportunity for being directly imaged, aiming to provide a more precise characterization of its orbit and mass. This study can be facilitated using the current generation of high-contrast imaging instruments, such as SPHERE.

The top-left panel of Fig. 12 highlights the unique position of HD 88986 b in the radius-period diagram among other known planets from the NASA Exoplanet Data Archive⁷ (as of June 7, 2023) with precise mass and radius measurements ($\sigma M/M = 25\%$ and $\sigma R/R = 8\%$, Otegi et al. 2020). Notably, HD 88986 b

has the longest orbital period among the discovered small transiting planets ($R_p < 4 R_{\oplus}$). This wide orbit suggests that the planet did not undergo significant mass loss due to extreme-ultraviolet radiation, and hence it probably retains its primordial composition (Kubyskhina & Fossati 2022). Consequently, HD 88986 b is an excellent candidate for investigating the planet’s internal structure and formation conditions.

The bottom-right panel of Fig. 12 compares the equilibrium temperatures of HD 88986 b with those of other known small planets possessing a precise mass and radius (Otegi et al. 2020). HD 88986 b, thanks to its long orbital period, is a cold planet ($T_{eq} = 460 \pm 8$ K). The study of atmospheric characteristics of cold planets (≤ 500 K) transiting bright hosts is extremely limited by the lack of such planets. In terms of atmospheric chemistry, colder atmospheres may contain disequilibrium chemistry that is useful for understanding atmospheric physics (Fortney et al. 2020). Remarkably, HD 88986 b’s equilibrium temperature places it within the proposed hazy atmosphere zone, ranging between 270 and 600 K, as suggested by Yu et al. (2021).

⁷ <https://exoplanetarchive.ipac.caltech.edu/>

This intriguing positioning opens up exciting opportunities for studying the haze layer and atmospheric composition above it (Kawashima et al. 2019). Hence, for the bottom-right panel of Fig. 12, we examined the proportional transmission spectroscopy metric ($TSM \propto \left(\frac{T_{eq} \times R_p^3}{M_p \times R_s^2}\right) \times 10^{-m_J/5}$) introduced by Kempton et al. (2018) and scaled the size of each planet accordingly. This metric considers the planet's equilibrium temperature T_{eq} , radius R_p , mass M_p , host star radius R_s , and host star magnitude in the J band m_J . We selected a radius bin of $1.5 R_{\oplus}$ to $2.75 R_{\oplus}$ based on Kempton et al. (2018)'s assumption that planets within the same size bin share similar atmospheric compositions. We exclusively employed the proportional TSM because the constant scale factor in Kempton et al. (2018)'s TSM is intended for stars with $m_J > 9$, while HD 88986 has a magnitude of $m_J = 5.2$ mag. HD 88986 b ranked 19th in comparison with proportional TSM S/N of only 24 planets detected in the hazy atmosphere zone (see Fig. 12 bottom-right panel). This relatively low rank is to some extent compensated for by the exceptionally long duration of the transit (16 h). Therefore, HD 88986 b's unique characteristics, such as being a cold exoplanet orbiting a bright star at a distance of 33 pc, make it a good target for atmospheric characterization studies of cold planets residing in the hazy zone.

Furthermore, with a mass of $M_p = 17.2^{+4.0}_{-3.8} M_{\oplus}$, HD 88986 b surpasses the critical mass threshold of $\sim 10 M_{\oplus}$ required for envelope accretion (Johnson et al. 2010). This indicates that it likely formed similarly to the cores of giant planets in our Solar System. However, HD 88986 b failed to accumulate much gas during its formation process. One possible scenario is that HD 88986 b formed at a late stage in the protoplanetary disk when there was little gas present during core assembly (Lee & Chiang 2016). Moreover, according to the minimum mass solar nebular model, it is unlikely for such a massive planet to form in situ at its current location, situated 0.6 au from its host star (Schlichting 2014). Instead, it likely formed farther away and subsequently migrated inward over time, potentially influenced by interactions with the detected massive companion in the system. However, to gain a comprehensive understanding of the HD 88986 planetary system, additional photometric and spectroscopic observations are required.

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Appendix A: Atmospheric dispersion correction

Atmospheric dispersion can introduce a slope in the spectral continuum, leading to a shift in the mean RV values of the observed targets (Pepe & Lovis 2008; Wehbe et al. 2020). In order to achieve a higher RV precision necessary for detecting low-mass planets, it is imperative to consider the impact of atmospheric dispersion. To address this effect in SOPHIE, we implemented a correction method based on the HARPS⁸ and ESPRESSO DRS (Modigliani et al. 2019). This correction involves scaling the target spectrum to match its flux distribution with that of a template. Specifically, we multiplied the target spectrum by the flux ratio between the target spectrum and the template. The template is constructed from a high S/N spectrum of a standard star with the same spectral type, acquired at low air mass conditions. Through the application of this method, the flux distributions of star spectra always have the same distribution, thereby minimizing the influence of atmospheric conditions on the computation of the CCF.

The method described herein yielded an enhancement in the precision of SOPHIE RV measurements by 8 cm s^{-1} when applied to the high-precision RV measurements from the SOPHIE SP1 star catalog (which comprises 96 stars that have more than 10 observations). This improvement equates to 7% of the mean error bar of 1.2 m s^{-1} associated with these stars. With the application of this method to the full width at half maximum (FWHM) of the same set of stars, we observed a substantial precision enhancement of 15 m s^{-1} on the FWHM. Notably, this enhancement is nearly five times greater than the average error bars of 2.8 m s^{-1} for the FWHM of these stars. This correction has been incorporated into the SOPHIE DRS and will be used in future planet detections conducted by the SOPHIE instrument. Moreover, the correction method is applied to all SOPHIE RV constant stars (4 super constant stars in addition to ~ 26 other stars with low RV dispersion), resulting in the creation of a more robust RV master constant time series (see Appendix C).

Appendix B: Moon contaminated spectra

To effectively detect and characterize planets through the RV method, it is imperative to meticulously manage systematic noise sources and eliminate any outliers. One such source of outliers in RV data sets is the spectra contaminated by Moonlight (e.g., Hébrard et al. 2008; Santerne et al. 2011). The Moon's reflected light can cause spectral contamination, leading to potential masking of the planet's signals or presenting systematic errors in the properties of the detected planets. Therefore, it is crucial to carefully identify and exclude any contamination by the lunar light from our data sets.

To achieve this, we developed a recipe that can identify Moon-polluted spectra for star observations made through the simultaneous calibration lamp, where no sky observation is available. This is achieved by taking into account the phase and position of the Moon at the time of observation, using two empirical criteria.

The first criterion considers whether moonlight contributes significantly to the target spectrum. This can be assumed when either: 1. the Moon phase is more than 68% at the time of observation and the sky-level is above the mean of the sky-level of all observations, 2. or when the separation between the target and Moon is less than 30° . We note that the sky-level is a criterion for estimating sky background light (see Bijaoui (1980); Ji et al. (2018)). In SOPHIE, it is calculated using SOPHIE DRS and is available in each FITS file spectrum header.

The second criterion we utilized in our study takes into account the proximity of the targets' RV to the Moon's RV. The Barycentric Earth radial velocity (BERV) at the time of observation and in the direction of the target is within approximately 1 km s^{-1} of Moon RVs (Díaz et al. 2012). Therefore, it is reasonable to consider it as a Moon RV. If the BERV is close to the target radial velocity, with $|RV_{\text{target}} - \text{BERV}| < 2 * \text{FWHM}$, then a spectrum can be considered moonlight polluted.

To test these empirical criteria, we used observations of three stars with simultaneously recorded sky observations where recorded sky spectra were available. Over a total of 59 spectra, 13 data were Moon contaminated. Our criteria allowed us to successfully detect 8 of these contaminated spectra but also flagged three uncontaminated data. So we conclude our criteria are conservative.

Overall, our recipe provides a useful tool for identifying suspected Moon-polluted spectra in RV observations made through simultaneous calibration lamps. This can help improve data quality and ensure accurate scientific results. In the case of HD 88986, following these criteria, we identified 31 spectra that were suspected to be contaminated by moonlight. These data conservatively were discarded from our analysis. We note that including or excluding these data had no significant effects on our final results within the uncertainties, showing our criteria indeed are conservative.

Appendix C: Update on constructing RV master constant timeseries

To monitor long-term instrumental variations, we have been conducting nightly observations of a few constant stars using SOPHIE since 2012. These constant stars include four super constant stars and approximately 25 additional stars with low RV dispersion ($\sigma < 3.5 \text{ m s}^{-1}$). Then, following the method outlined in Courcol et al. (2015), we create a master constant time series and subtract it from the RVs of each star. However, our latest analysis suggests that one of our constant stars, HD185144, exhibits activity over an extended period (see Fig. C.1). This activity could potentially affect our master constant time series and consequently impact the RVs of other stars.

We note that this star's activity cycle was already known thanks to HIRES data (Isaacson & Fischer 2010). SOPHIE later confirmed this when we built the first master constant correction in 2015 (Courcol et al. 2015). At that time, we estimated the semi-amplitude of the signal to be less than 1.5 m s^{-1} , which was negligible given the spectrograph's precision. With more data points in 2023, the effect is estimated to have a semi-amplitude of $2.7 \pm 0.1 \text{ m s}^{-1}$. Given SOPHIE's improved RV precision, it has become necessary to correct the impact of HD185144's stellar activity on its RVs. Since this star is one of the most frequently observed

⁸ <http://www.eso.org/sci/facilities/lasilla/instruments/harps/doc/index.html>

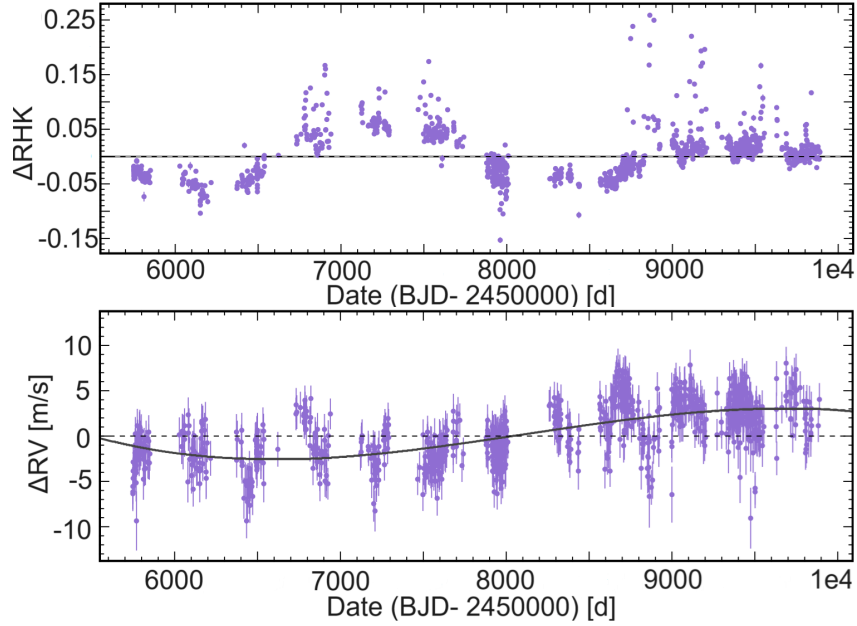


Fig. C.1. $\log R'_{\text{HK}}$ (*top*) and RVs (*bottom*) of constant star HD185144. The best fit of a third-order polynomial model (black line *bottom*) is overplotted to the stellar long-period activity.

constant stars by SOPHIE with more than 1100 data points, removing the RVs of this star from our master constant time series is not an option.

To correct this stellar activity, we utilized a four-step approach. Firstly, we corrected the HD185144 RVs for SOPHIE instrumental variations. To accomplish this, we subtracted the master constant time series, derived from SOPHIE constant stars excluding HD185144, from the RV of HD185144. Next, we fit a third-order polynomial model on the HD185144 RV time series to determine its activity phase (see Fig. C.1 bottom). Subsequently, we subtracted the same polynomial model from the raw RVs of HD185144 (prior to master constant correction). Finally, we used these corrected RVs to construct the final master constant time series along with other stars.

Appendix D: RVs

Table D.1: SOPHIE RVs for HD 88986. We note that a value of 999.0 indicates invalid data on the corresponding date.

BJD (-2400000 d)	RV (km s ⁻¹)	σ_{RV} (km s ⁻¹)	BIS (km s ⁻¹)	S-index	$\sigma_{S-index}$	Na	σ_{Na}
SOPHIE:							
54185.43116	29.0727	0.0013					
54189.45774	29.0698	0.0016					
54190.42612	29.0813	0.0014					
54190.43296	29.0717	0.0035					
54192.48075	29.0680	0.0013					
54192.48729	29.0638	0.0039					
54236.34361	29.0812	0.0014					
54249.39304	29.0765	0.0015					
54260.37481	29.0721	0.0016					
54262.37490	29.0707	0.0017					
54263.36789	29.0847	0.0025					
54264.36478	29.0817	0.0017					
SOPHIE+:							
56298.72054	29.07	0.001	-0.0041	0.1759	0.0007	0.521	0.007
56313.59596	29.072	0.001	-0.0042	0.1709	0.0007	0.518	0.007
56316.56759	29.073	0.001	-0.0023	0.1676	0.0007	0.528	0.008
56317.68241	29.067	0.001	-0.004	0.1769	0.0012	0.525	0.01
56319.61938	29.069	0.001	-0.0072	0.1703	0.0011	0.53	0.01
56322.59358	29.069	0.001	-0.0053	0.1739	0.0008	0.516	0.008
56327.48507	29.07	0.002	-0.0071	999.0	999.0	0.522	0.018
56344.58229	29.073	0.001	-0.0013	0.1737	0.0008	0.521	0.008

Table D.1: –continued from previous page

BJD (-2400000 d)	RV (km s ⁻¹)	σ_{RV} (km s ⁻¹)	BIS (km s ⁻¹)	S-index	$\sigma_{S-index}$	Na	σ_{Na}
56345.50874	29.073	0.001	-0.0026	0.1739	0.001	0.528	0.009
56346.50675	29.072	0.001	-0.0	0.1731	0.0007	0.525	0.007
56349.46062	29.068	0.001	-0.0043	0.1693	0.0007	0.525	0.008
56350.49421	29.072	0.001	-0.0017	0.1667	0.0005	0.526	0.006
56351.59704	29.068	0.001	0.0018	0.1712	0.0007	0.521	0.007
56354.44695	29.07	0.001	-0.0012	0.1647	0.0004	0.514	0.005
56355.52704	29.076	0.001	0.0006	0.171	0.0007	0.519	0.007
56360.42506	29.076	0.001	-0.0001	0.1657	0.0004	0.52	0.005
56360.51722	29.074	0.001	-0.0029	0.1751	0.0006	0.519	0.007
56370.50959	29.079	0.001	-0.0061	0.1709	0.0008	0.526	0.008
56372.49076	29.078	0.001	-0.0019	0.1677	0.0008	0.527	0.009
56382.36446	29.071	0.001	-0.0054	0.1694	0.0009	0.518	0.009
56405.33846	29.071	0.001	-0.0023	0.1722	0.0006	999.0	999.0
56415.36788	29.072	0.002	-0.0067	0.1747	0.0015	999.0	999.0
56419.4127	29.073	0.001	-0.0017	0.1707	0.0007	999.0	999.0
56430.35736	29.07	0.002	0.005	0.1739	0.0017	999.0	999.0
56435.37259	29.069	0.002	0.0059	999.0	999.0	999.0	999.0
56627.71815	29.072	0.001	-0.0004	0.1761	0.0007	0.533	0.007
56629.7066	29.073	0.001	0.0034	0.1658	0.0006	0.525	0.007
56630.6626	29.072	0.001	0.0001	0.1669	0.0006	0.525	0.006
56631.68114	29.074	0.001	-0.0025	0.1707	0.0007	0.526	0.008
56640.58001	29.071	0.001	-0.0006	0.17	0.0009	0.523	0.008
56653.67292	29.073	0.001	0.0025	0.1769	0.001	0.523	0.009
56655.67739	29.076	0.001	-0.0039	0.1681	0.0009	0.518	0.008
56656.65089	29.075	0.001	-0.0055	0.1694	0.001	0.525	0.009
56657.63896	29.077	0.001	-0.0024	0.1717	0.001	0.516	0.01
56663.55861	29.074	0.001	-0.0012	0.1792	0.0008	0.515	0.008
56665.69581	29.075	0.001	0.0001	0.1684	0.0008	0.514	0.008
56672.62532	29.074	0.001	-0.0033	0.1706	0.0011	0.527	0.01
56680.49332	29.078	0.001	-0.0049	0.1673	0.0006	0.522	0.007
56681.54471	29.081	0.001	-0.0042	0.1749	0.001	0.518	0.009
56682.61116	29.078	0.001	-0.0012	0.1736	0.0007	0.529	0.007
56683.56202	29.078	0.001	-0.0058	0.1958	0.0014	0.522	0.011
56685.45394	29.074	0.001	-0.0031	0.1815	0.0016	0.528	0.013
56696.41786	29.075	0.001	-0.0011	0.1747	0.0007	0.523	0.007
56699.61383	29.07	0.001	-0.0019	0.1781	0.0012	0.521	0.01
57350.70123	29.08	0.001	-0.0014	999.0	999.0	0.524	0.009
57390.64252	29.078	0.001	-0.0034	0.1661	0.001	0.52	0.01
57402.57042	29.079	0.001	0.0022	0.1683	0.001	0.521	0.009
57411.45305	29.084	0.001	-0.0022	0.1812	0.0011	0.522	0.009
57413.56732	29.086	0.001	-0.0049	0.1688	0.001	0.516	0.009
57436.56638	29.078	0.001	-0.0	0.1652	0.001	0.522	0.009
57437.64439	29.078	0.001	-0.0026	0.1912	0.0017	0.52	0.011
57468.4337	29.078	0.001	-0.0003	999.0	999.0	0.505	0.013
57470.53201	29.078	0.001	0.0011	0.1812	0.0016	0.521	0.01
57476.412	29.082	0.001	-0.003	0.1676	0.0006	0.524	0.007
57498.40682	29.082	0.001	-0.0006	0.1677	0.0006	999.0	999.0
57503.40866	29.08	0.001	-0.005	0.1687	0.001	999.0	999.0
57504.43547	29.083	0.001	-0.0055	0.1802	0.0014	999.0	999.0
57507.38017	29.085	0.001	-0.0005	0.1688	0.0009	999.0	999.0
57512.4085	29.083	0.001	0.0056	0.1609	0.0016	999.0	999.0
57528.33925	29.082	0.001	-0.002	0.1675	0.0014	999.0	999.0
57699.67587	29.082	0.001	-0.0013	0.1793	0.0011	0.523	0.01
57701.63228	29.084	0.002	-0.0009	999.0	999.0	0.522	0.015
57728.6449	29.08	0.001	-0.0002	0.1704	0.0004	0.521	0.006
57730.6722	29.079	0.001	-0.0019	0.1725	0.0005	0.526	0.007
57757.69077	29.079	0.001	-0.0017	0.1758	0.001	0.522	0.01
57758.5679	29.079	0.001	-0.0029	0.1795	0.0012	0.529	0.011
57759.52851	29.082	0.001	-0.0001	0.1793	0.0013	0.524	0.012
57766.64339	29.082	0.001	0.0009	0.1733	0.0007	0.519	0.008
57770.67824	29.08	0.001	-0.0025	0.1797	0.001	0.526	0.01

Table D.1: –continued from previous page

BJD (-2400000 d)	RV (km s ⁻¹)	σ_{RV} (km s ⁻¹)	BIS (km s ⁻¹)	S-index	$\sigma_{S-index}$	Na	σ_{Na}
57771.63633	29.082	0.001	-0.0023	0.1758	0.0007	0.526	0.008
57772.53428	29.082	0.001	-0.0012	0.1738	0.0005	0.527	0.006
57800.52831	29.085	0.001	0.0007	0.1718	0.0005	0.516	0.006
57801.52514	29.083	0.001	0.0021	0.1733	0.0006	0.526	0.007
57820.5185	29.084	0.001	0.004	0.1773	0.0013	0.527	0.012
57821.46905	29.082	0.001	-0.0001	0.172	0.0008	0.516	0.009
57823.50327	29.083	0.001	-0.0002	0.1706	0.0006	0.522	0.007
57826.55084	29.084	0.001	0.0014	0.1831	0.0009	0.514	0.008
57827.4408	29.086	0.001	-0.0014	0.1709	0.0005	0.508	0.006
57829.50094	29.086	0.001	0.0009	0.1731	0.0005	0.524	0.006
57830.47692	29.082	0.001	-0.0018	0.1725	0.0007	0.523	0.008
57831.48271	29.084	0.002	0.0045	999.0	999.0	0.512	0.014
57832.46256	29.081	0.001	0.0009	0.1662	0.0006	0.519	0.007
57833.47721	29.08	0.001	0.0045	0.1682	0.0012	0.515	0.011
57848.41243	29.089	0.001	-0.0026	0.1752	0.0009	999.0	999.0
57849.36053	29.089	0.001	0.0019	0.1889	0.001	999.0	999.0
57850.416	29.082	0.001	0.0018	0.1717	0.0005	999.0	999.0
57851.41507	29.084	0.001	0.0014	0.1703	0.0005	999.0	999.0
57852.42093	29.082	0.001	0.0004	0.1734	0.0006	999.0	999.0
57853.46839	29.083	0.001	-0.0017	0.1746	0.0006	999.0	999.0
57854.45925	29.081	0.001	0.0001	0.1723	0.0008	999.0	999.0
57855.44274	29.082	0.001	-0.0026	0.1731	0.0005	999.0	999.0
57856.36935	29.082	0.001	-0.0019	0.1722	0.0008	999.0	999.0
57858.36212	29.08	0.001	-0.0016	0.1696	0.0007	999.0	999.0
57859.3784	29.08	0.001	-0.0013	0.1724	0.0009	999.0	999.0
57860.40603	29.077	0.001	-0.0005	0.1727	0.0012	999.0	999.0
58072.69214	29.081	0.001	-0.0007	999.0	999.0	0.525	0.008
58073.61653	29.08	0.001	-0.0027	999.0	999.0	0.524	0.007
58074.69324	29.08	0.001	0.0014	999.0	999.0	0.524	0.009
58075.67984	29.082	0.001	-0.0027	999.0	999.0	0.525	0.009
58076.67888	29.078	0.002	-0.0096	999.0	999.0	0.508	0.015
58077.70279	29.078	0.001	-0.0023	999.0	999.0	0.525	0.01
58078.70137	29.075	0.001	-0.0051	999.0	999.0	0.526	0.01
58090.72611	29.084	0.001	0.0002	999.0	999.0	0.525	0.01
58091.68905	29.084	0.001	-0.0011	999.0	999.0	0.524	0.009
58093.62615	29.083	0.001	0.0016	999.0	999.0	0.524	0.007
58100.68476	29.085	0.001	-0.0007	999.0	999.0	0.528	0.009
58102.70122	29.083	0.002	-0.0034	999.0	999.0	0.486	0.016
58104.64993	29.082	0.001	0.0011	999.0	999.0	0.525	0.011
58108.69417	29.088	0.001	-0.0026	999.0	999.0	0.521	0.009
58110.70972	29.085	0.001	0.0028	999.0	999.0	0.525	0.008
58111.62003	29.088	0.001	0.0024	999.0	999.0	0.523	0.007
58130.60025	29.092	0.001	-0.0036	0.1649	0.0008	0.525	0.008
58131.66504	29.09	0.001	-0.0011	0.161	0.0011	0.503	0.009
58141.61493	29.086	0.001	0.0048	0.1638	0.0009	0.513	0.009
58142.5731	29.087	0.001	0.0003	0.1675	0.0005	0.522	0.006
58146.57834	29.083	0.001	0.0	0.1651	0.0008	0.525	0.008
58147.54992	29.087	0.001	0.0005	0.1634	0.0009	0.495	0.008
58148.5671	29.087	0.001	0.0021	0.1636	0.001	0.522	0.01
58151.67525	29.088	0.001	-0.0058	0.1557	0.0018	0.526	0.013
58152.626	29.081	0.002	-0.0048	0.1493	0.002	0.525	0.015
58153.56616	29.088	0.001	0.0016	0.1621	0.0014	0.525	0.012
58185.49837	29.085	0.001	0.0025	0.1661	0.0007	0.529	0.008
58186.47613	29.086	0.001	0.0018	0.1672	0.0008	0.519	0.008
58209.54029	29.089	0.002	-0.0035	999.0	999.0	999.0	999.0
58210.44872	29.086	0.001	-0.0005	0.17	0.0006	999.0	999.0
58213.54147	29.086	0.001	0.0009	999.0	999.0	999.0	999.0
58214.39055	29.088	0.001	0.0004	0.1676	0.0006	999.0	999.0
58215.45449	29.085	0.001	-0.003	0.1674	0.0011	999.0	999.0
58216.45408	29.082	0.001	-0.0002	0.165	0.0011	999.0	999.0
58218.47574	29.084	0.002	-0.0085	999.0	999.0	999.0	999.0

Table D.1: – continued from previous page

BJD (-2400000 d)	RV (km s ⁻¹)	σ_{RV} (km s ⁻¹)	BIS (km s ⁻¹)	S-index	$\sigma_{S-index}$	Na	σ_{Na}
58234.37191	29.084	0.001	-0.0024	0.1684	0.0007	999.0	999.0
58235.44114	29.091	0.001	-0.0005	0.1707	0.0015	999.0	999.0
58236.38366	29.084	0.001	-0.0035	0.1733	0.0008	999.0	999.0
58242.46149	29.087	0.002	0.0037	999.0	999.0	999.0	999.0
58243.4582	29.083	0.001	0.0004	999.0	999.0	999.0	999.0
58245.36182	29.091	0.001	-0.0011	0.1736	0.0011	999.0	999.0
58255.40949	29.09	0.001	0.0	0.1766	0.0013	999.0	999.0
58257.39281	29.089	0.001	0.0039	0.1773	0.0008	999.0	999.0
58258.37469	29.088	0.001	-0.0016	0.1732	0.0008	999.0	999.0
58262.35981	29.091	0.001	-0.0016	0.1706	0.0007	999.0	999.0
58263.35275	29.089	0.001	-0.002	0.1729	0.0008	999.0	999.0
58264.35148	29.089	0.001	0.0003	0.1723	0.0018	999.0	999.0
58270.34924	29.088	0.001	-0.0018	0.1716	0.0006	999.0	999.0
58271.35578	29.092	0.001	-0.0042	0.1714	0.001	999.0	999.0
58272.34719	29.084	0.002	-0.0026	999.0	999.0	999.0	999.0
58274.38435	29.085	0.003	-0.0218	999.0	999.0	999.0	999.0
58440.66644	29.094	0.001	0.0009	0.1704	0.0008	0.526	0.008
58441.63117	29.086	0.001	-0.0025	0.1672	0.001	0.523	0.009
58456.70082	29.094	0.001	0.004	0.1691	0.0008	0.515	0.009
58457.72054	29.091	0.001	0.0012	0.1673	0.0005	0.52	0.006
58459.65022	29.091	0.001	-0.0035	0.1502	0.0013	0.513	0.012
58460.67423	29.095	0.001	-0.0035	0.1588	0.0012	0.51	0.01
58467.67996	29.092	0.001	-0.0031	0.1644	0.0011	0.53	0.01
58475.70316	29.085	0.001	-0.0029	0.1599	0.0013	0.519	0.011
58486.64971	29.091	0.002	0.001	999.0	999.0	0.521	0.017
58487.69909	29.089	0.003	0.0024	999.0	999.0	999.0	999.0
58488.69742	29.095	0.001	0.0051	0.1672	0.001	0.529	0.01
58489.70608	29.09	0.002	0.0028	0.1606	0.0019	0.527	0.014
58490.67879	29.094	0.001	-0.002	0.1692	0.0006	0.527	0.007
58496.63178	29.094	0.002	-0.0059	999.0	999.0	999.0	999.0
58497.61321	29.09	0.001	0.0023	0.1681	0.0014	0.516	0.012
58498.66066	29.094	0.001	0.0002	0.1667	0.0013	0.528	0.011
58499.59632	29.091	0.001	0.0017	0.1701	0.0006	0.526	0.007
58526.57706	29.098	0.001	0.0008	0.1725	0.0011	0.533	0.011
58527.54347	29.09	0.001	0.0006	0.1721	0.0012	0.527	0.011
58528.50643	29.091	0.001	0.0025	0.1712	0.0005	0.527	0.006
58529.5612	29.09	0.001	0.001	0.1712	0.0005	0.522	0.006
58530.5159	29.089	0.001	0.0004	0.1718	0.0006	0.526	0.007
58531.59703	29.09	0.001	-0.0016	0.1696	0.0005	0.53	0.006
58532.53022	29.088	0.001	-0.0036	0.17	0.0008	0.521	0.008
58533.4996	29.089	0.001	-0.003	0.1696	0.0007	0.526	0.007
58534.50645	29.091	0.001	-0.0008	0.1702	0.0007	0.527	0.008
58535.59314	29.091	0.001	-0.0023	0.171	0.001	0.521	0.009
58543.57619	29.096	0.001	0.0017	0.1692	0.001	0.525	0.009
58544.51305	29.097	0.001	-0.0024	0.1706	0.0011	0.528	0.01
58545.4534	29.094	0.001	-0.0008	0.1707	0.0011	0.522	0.01
58546.37522	29.094	0.001	0.0014	0.1728	0.0006	0.526	0.006
58548.37912	29.093	0.001	-0.0014	0.1662	0.0009	0.52	0.009
58550.39724	29.093	0.001	0.0003	0.1691	0.0017	0.522	0.013
58551.42881	29.092	0.001	0.0005	0.1702	0.0007	0.524	0.008
58552.40384	29.099	0.001	-0.0004	0.1689	0.0009	0.519	0.009
58553.41709	29.094	0.001	-0.0061	0.1676	0.0008	0.525	0.009
58554.49277	29.09	0.002	-0.001	999.0	999.0	0.524	0.014
58556.44137	29.095	0.001	0.0004	0.1689	0.0009	0.526	0.009
58557.48776	29.095	0.001	0.0006	0.1676	0.0007	0.518	0.008
58559.44023	29.095	0.001	0.0006	0.1693	0.0007	0.527	0.008
58560.51233	29.092	0.001	-0.0027	0.1706	0.0012	0.529	0.011
58561.43576	29.096	0.001	0.0005	0.1728	0.0009	0.522	0.009
58563.51862	29.098	0.001	-0.0005	0.1745	0.0008	0.529	0.008
58586.3874	29.094	0.001	0.0043	0.1703	0.0009	999.0	999.0
58587.40305	29.096	0.001	0.0017	0.1676	0.0013	999.0	999.0

Table D.1: – continued from previous page

BJD (-2400000 d)	RV (km s ⁻¹)	σ_{RV} (km s ⁻¹)	BIS (km s ⁻¹)	S-index	$\sigma_{S-index}$	Na	σ_{Na}
58588.37817	29.094	0.001	-0.0019	0.1749	0.0017	999.0	999.0
58590.4154	29.095	0.001	-0.0001	0.169	0.0004	999.0	999.0
58591.34231	29.095	0.001	0.0027	0.1631	0.0012	999.0	999.0
58592.45683	29.096	0.002	-0.0032	999.0	999.0	999.0	999.0
58593.42747	29.092	0.001	0.0006	0.1745	0.0008	999.0	999.0
58598.49199	29.095	0.003	-0.002	999.0	999.0	999.0	999.0
58600.48275	29.091	0.001	-0.0043	999.0	999.0	999.0	999.0
58601.42492	29.093	0.001	-0.0005	0.1736	0.0012	999.0	999.0
58602.32023	29.091	0.001	-0.0008	0.1715	0.001	999.0	999.0
58603.34279	29.093	0.001	-0.0003	0.1727	0.0009	999.0	999.0
58604.36121	29.094	0.001	-0.0023	0.1736	0.0006	999.0	999.0
58605.37671	29.097	0.001	-0.0013	0.1786	0.0009	999.0	999.0
58606.38135	29.093	0.001	-0.0018	0.1775	0.001	999.0	999.0
58607.37926	29.089	0.001	0.0054	0.176	0.0016	999.0	999.0
58608.39479	29.093	0.001	-0.0009	0.1739	0.0012	999.0	999.0
58610.38085	29.098	0.001	0.0005	0.1761	0.0007	999.0	999.0
58613.41864	29.091	0.002	-0.006	999.0	999.0	999.0	999.0
58616.33982	29.096	0.001	-0.0001	0.1745	0.0013	999.0	999.0
58617.33881	29.092	0.001	-0.0012	0.1719	0.0006	999.0	999.0
58619.4107	29.086	0.001	-0.0036	0.1778	0.0012	999.0	999.0
58620.38094	29.089	0.001	0.0032	0.1739	0.0009	999.0	999.0
58624.41277	29.093	0.001	-0.0002	999.0	999.0	999.0	999.0
58625.39701	29.085	0.002	0.0102	999.0	999.0	999.0	999.0
58626.36614	29.09	0.001	0.0019	0.1777	0.0007	999.0	999.0
58627.37623	29.089	0.001	0.0022	0.18	0.0011	999.0	999.0
58630.37143	29.092	0.001	0.0002	0.1747	0.0008	999.0	999.0
58631.35476	29.092	0.001	0.0002	0.172	0.0013	999.0	999.0
58632.35378	29.085	0.001	-0.0019	0.1656	0.0013	999.0	999.0
58633.35156	29.088	0.001	-0.0037	0.169	0.001	999.0	999.0
58634.34584	29.09	0.001	0.0031	0.1734	0.0007	999.0	999.0
58635.34845	29.089	0.001	-0.0007	0.1727	0.0008	999.0	999.0
58636.36255	29.091	0.001	-0.0017	0.1777	0.001	999.0	999.0
58637.35109	29.09	0.001	-0.0007	0.174	0.0008	999.0	999.0
58820.63063	29.091	0.001	-0.003	0.1801	0.0011	0.516	0.009
58821.60302	29.094	0.001	-0.0038	0.1796	0.0013	0.512	0.01
58824.67421	29.095	0.001	0.0003	0.1764	0.0007	0.52	0.007
58828.61484	29.094	0.001	0.0015	0.1735	0.0007	0.53	0.008
58852.6337	29.097	0.002	0.0044	999.0	999.0	0.527	0.017
58853.55459	29.105	0.001	0.0028	0.189	0.0016	0.524	0.013
58854.58145	29.096	0.001	-0.0021	0.1818	0.0007	0.525	0.008
58855.57747	29.094	0.001	-0.0005	0.1844	0.0009	0.53	0.009
58856.6402	29.099	0.001	0.0013	0.185	0.0011	0.514	0.01
58856.73025	29.096	0.001	0.0001	0.1882	0.0014	0.518	0.011
58875.6166	29.099	0.001	-0.0043	0.1808	0.0006	0.525	0.006
58877.61726	29.099	0.001	-0.0014	0.1804	0.0008	0.515	0.008
58881.59325	29.099	0.001	0.0011	0.1845	0.0009	0.512	0.008
58882.53817	29.095	0.001	-0.0039	0.193	0.0016	0.512	0.012
58883.54223	29.096	0.001	-0.0011	0.1874	0.0011	0.521	0.01
58884.46423	29.1	0.001	-0.0048	0.1967	0.0018	0.527	0.014
58885.38578	29.101	0.002	-0.0014	999.0	999.0	0.517	0.019
58886.50785	29.102	0.001	0.0004	0.1805	0.0006	0.535	0.007
58887.45579	29.097	0.001	-0.0026	0.1833	0.0011	0.524	0.011
58888.50882	29.096	0.001	-0.0002	0.1791	0.0005	0.524	0.005
58891.56505	29.097	0.001	0.0004	0.1891	0.0013	0.52	0.011
58892.55219	29.1	0.001	-0.0005	0.1843	0.0007	0.532	0.008
58893.5583	29.098	0.001	0.0028	0.191	0.0013	0.524	0.011
58894.48852	29.099	0.001	-0.0009	0.18	0.0007	0.524	0.008
58897.58099	29.094	0.003	-0.0036	999.0	999.0	999.0	999.0
58898.50343	29.096	0.001	0.0014	0.185	0.001	999.0	999.0
58906.53712	29.095	0.001	0.001	0.1838	0.0013	0.518	0.011
58907.50513	29.096	0.001	0.0035	0.1838	0.0013	0.526	0.011

Table D.1: – continued from previous page

BJD (-2400000 d)	RV (km s ⁻¹)	σ_{RV} (km s ⁻¹)	BIS (km s ⁻¹)	S-index	$\sigma_{S-index}$	Na	σ_{Na}
58911.46747	29.098	0.001	0.0016	0.1893	0.0015	0.527	0.012
58912.49592	29.094	0.001	0.0019	0.187	0.0017	0.526	0.014
58913.4537	29.097	0.001	0.0052	0.1752	0.001	0.52	0.01
58914.41822	29.1	0.001	0.0015	0.1894	0.0014	0.519	0.012
58916.42498	29.099	0.001	-0.0002	0.1903	0.0013	0.535	0.012
58918.44042	29.101	0.001	0.0024	0.1933	0.0016	0.527	0.013
58919.48435	29.099	0.002	0.0003	999.0	999.0	0.474	0.012
58920.43465	29.096	0.001	0.0004	0.18	0.0007	0.522	0.008
58924.46581	29.101	0.001	0.0001	0.1776	0.0009	0.528	0.009
59170.59242	29.108	0.001	-0.0077	0.2018	0.0013	0.518	0.009
59171.67277	29.104	0.001	-0.0012	0.1707	0.0005	0.524	0.006
59172.59053	29.105	0.001	-0.0036	0.2086	0.0011	0.515	0.006
59175.67902	29.1	0.001	-0.0027	0.1753	0.0007	0.519	0.008
59182.69165	29.103	0.001	0.0006	0.172	0.0005	0.516	0.006
59183.6644	29.104	0.001	-0.0018	0.1798	0.0006	0.523	0.007
59184.66932	29.098	0.002	0.001	0.1895	0.0018	0.513	0.014
59186.62898	29.105	0.001	-0.0007	0.1748	0.0007	0.526	0.008
59197.73091	29.102	0.001	-0.001	999.0	999.0	0.524	0.007
59203.65678	29.109	0.002	-0.0044	0.1674	0.0019	0.514	0.015
59205.62881	29.108	0.001	0.0043	0.1709	0.0006	0.518	0.007
59206.6322	29.098	0.001	-0.0025	0.1701	0.0011	0.516	0.011
59247.50061	29.103	0.001	-0.001	0.1749	0.0014	999.0	999.0
59248.63037	29.108	0.001	-0.001	0.174	0.0006	0.516	0.007
59249.56861	29.105	0.001	-0.003	999.0	999.0	0.518	0.01
59263.47458	29.106	0.001	-0.002	0.1724	0.0006	0.526	0.007
59265.54794	29.105	0.001	-0.0031	0.176	0.0009	0.525	0.009
59266.41158	29.104	0.001	0.0002	0.1763	0.0008	0.526	0.008
59267.37249	29.106	0.002	-0.0034	999.0	999.0	0.52	0.02
59269.38117	29.105	0.001	0.0014	0.1739	0.0007	0.525	0.008
59271.4168	29.106	0.001	0.0011	0.1725	0.0005	0.53	0.007
59272.37643	29.105	0.001	0.0042	0.1777	0.0009	0.525	0.009
59273.50018	29.103	0.001	0.0036	0.1775	0.0009	0.522	0.008
59274.52433	29.107	0.001	-0.0007	0.1729	0.0005	0.527	0.007
59275.53869	29.109	0.001	-0.0002	0.1728	0.0006	0.526	0.007
59277.48064	29.109	0.001	-0.0001	0.1775	0.0009	0.522	0.009
59278.45468	29.109	0.001	-0.0007	0.1737	0.0008	0.523	0.008
59279.43298	29.108	0.001	0.0007	0.175	0.0006	0.524	0.007
59280.4677	29.104	0.001	-0.0049	0.1808	0.0012	0.517	0.01
59327.42527	29.104	0.001	-0.0025	0.1785	0.0009	999.0	999.0
59328.43132	29.106	0.001	-0.0037	0.1742	0.0007	999.0	999.0
59329.37507	29.106	0.001	-0.0012	0.1727	0.0006	999.0	999.0
59330.42242	29.105	0.002	-0.0119	999.0	999.0	999.0	999.0
59336.36732	29.108	0.001	0.0007	0.1743	0.0011	999.0	999.0
59337.39674	29.11	0.001	0.0027	0.1788	0.0009	999.0	999.0
59339.38104	29.109	0.001	0.0026	0.1717	0.0008	999.0	999.0
59340.36174	29.11	0.001	0.0012	0.1725	0.0007	999.0	999.0
59342.33408	29.11	0.001	0.0017	0.1732	0.0007	999.0	999.0
59343.35287	29.103	0.001	-0.0023	0.1718	0.0006	999.0	999.0
59346.36233	29.101	0.001	-0.0025	0.1721	0.0012	999.0	999.0
59347.33788	29.11	0.001	-0.0001	0.1705	0.0006	999.0	999.0
59349.34036	29.106	0.001	-0.0041	0.1816	0.0013	999.0	999.0
59351.4423	29.107	0.002	-0.0066	999.0	999.0	999.0	999.0
59351.45289	29.107	0.002	0.0035	999.0	999.0	999.0	999.0
59352.34585	29.108	0.001	-0.0014	0.1771	0.0009	999.0	999.0
59354.35096	29.106	0.001	-0.001	0.1764	0.0014	999.0	999.0
59355.35012	29.107	0.002	-0.0035	999.0	999.0	999.0	999.0
59357.37102	29.106	0.001	-0.0012	999.0	999.0	999.0	999.0
59363.3513	29.107	0.001	0.0004	0.1755	0.001	999.0	999.0
59586.50556	29.115	0.001	-0.0067	0.186	0.0008	0.53	0.008
59590.52159	29.117	0.001	-0.0015	0.19	0.0013	0.504	0.011
59593.4655	29.11	0.001	-0.0032	0.1857	0.0007	0.529	0.007

Table D.1: – continued from previous page

BJD (-2400000 d)	RV (km s ⁻¹)	σ_{RV} (km s ⁻¹)	BIS (km s ⁻¹)	S-index	$\sigma_{S-index}$	Na	σ_{Na}
59594.5332	29.112	0.001	-0.0003	0.1765	0.0006	0.53	0.007
59602.6255	29.12	0.001	-0.0001	0.1818	0.0006	0.526	0.007
59605.44167	29.12	0.001	0.0011	0.1895	0.0008	0.527	0.008
59606.47317	29.119	0.001	-0.0017	0.185	0.0009	0.521	0.008
59607.57129	29.118	0.001	0.0046	0.1907	0.0009	0.528	0.009
59608.67797	29.116	0.001	-0.0013	0.1938	0.0012	0.521	0.01
59609.60292	29.117	0.001	0.0011	0.1878	0.001	0.525	0.009
59610.51254	29.115	0.001	0.0021	0.1853	0.0008	0.523	0.009
59620.52934	29.111	0.001	-0.0019	0.1789	0.0007	0.523	0.008
59621.56096	29.112	0.001	-0.0011	0.1847	0.001	0.513	0.009
59622.47061	29.112	0.001	-0.0006	0.1833	0.0008	0.522	0.008
59623.53538	29.116	0.001	-0.0011	0.1872	0.001	0.525	0.01
59625.55919	29.112	0.001	-0.0029	0.1812	0.0008	0.52	0.008
59628.46108	29.111	0.001	-0.0024	0.1871	0.0012	0.519	0.011
59630.49989	29.115	0.001	-0.0012	0.1978	0.0015	0.526	0.012
59633.41679	29.118	0.001	-0.0023	0.1834	0.0008	0.529	0.008
59634.56414	29.115	0.001	0.0021	0.178	0.0008	0.525	0.008
59635.48433	29.12	0.001	-0.0003	0.1852	0.001	0.523	0.01
59636.55304	29.121	0.001	0.0003	0.1847	0.0009	0.528	0.009
59637.57302	29.111	0.001	0.0009	0.181	0.0008	0.526	0.008
59638.51495	29.115	0.001	0.002	0.1796	0.0009	0.506	0.008
59639.54117	29.113	0.001	0.0006	0.1851	0.001	0.525	0.01
59640.4762	29.112	0.001	-0.0016	0.1914	0.0013	0.525	0.011
59641.56528	29.118	0.001	0.0018	0.1905	0.0009	0.524	0.008
59642.51285	29.113	0.001	-0.0019	0.1843	0.0008	0.522	0.008
59644.46157	29.122	0.001	0.0049	0.1885	0.0013	0.523	0.01
59645.56396	29.122	0.001	0.0024	0.2027	0.0015	0.509	0.01
59646.45423	29.121	0.001	0.0013	0.1883	0.0009	0.527	0.009
59648.51781	29.12	0.001	0.0021	0.1851	0.0006	0.525	0.007
59658.43432	29.114	0.001	-0.0043	0.1906	0.001	0.526	0.01
59660.5041	29.113	0.001	0.0004	0.1848	0.001	0.528	0.009
59661.43835	29.112	0.001	0.0012	0.1801	0.0008	0.532	0.008
59662.40771	29.118	0.001	0.0017	0.1786	0.0006	0.525	0.007
59663.4597	29.113	0.001	-0.0003	0.1785	0.0006	0.528	0.007
59678.33034	29.113	0.001	-0.0036	0.1757	0.0005	999.0	999.0
59683.40842	29.116	0.001	0.0003	0.1769	0.0006	999.0	999.0
59686.49836	29.118	0.001	0.0032	0.2257	0.0017	999.0	999.0
59889.7015	29.123	0.001	0.0008	0.1778	0.0006	0.518	0.007
59890.67476	29.126	0.001	0.0012	999.0	999.0	0.521	0.014
59902.69906	29.118	0.001	-0.0017	0.1811	0.0011	0.524	0.01
59903.66273	29.122	0.001	0.0032	0.185	0.0011	0.523	0.01
59919.63625	29.128	0.001	-0.0002	0.1802	0.0008	0.527	0.009
59920.64785	29.132	0.001	-0.0011	0.1769	0.0007	0.52	0.008
59921.57429	29.126	0.001	0.0026	0.181	0.0009	0.526	0.008
59937.67352	29.121	0.001	-0.0072	0.1894	0.0015	0.51	0.012
59958.60953	29.123	0.001	-0.0013	0.1789	0.0009	0.528	0.009
59959.57843	29.118	0.002	-0.0036	999.0	999.0	0.506	0.014
59972.57361	29.124	0.001	0.0028	0.1877	0.0009	0.527	0.009
59973.54181	29.125	0.001	-0.001	0.1816	0.0007	0.521	0.008
59974.51399	29.127	0.001	-0.0011	0.178	0.0006	0.529	0.007
59975.61481	29.133	0.001	0.0006	0.1797	0.0012	0.524	0.011
59976.53289	29.128	0.001	-0.0018	0.1851	0.0011	0.515	0.01
59978.45779	29.121	0.001	-0.0021	0.1819	0.0008	0.527	0.008
59980.4728	29.119	0.001	0.0011	0.179	0.0014	0.529	0.012
59983.48087	29.127	0.001	-0.0004	0.1876	0.0012	0.529	0.011
59984.62393	29.12	0.001	-0.0009	0.1786	0.0008	0.527	0.008
59988.46075	29.123	0.001	-0.0013	999.0	999.0	0.524	0.006
59990.5449	29.122	0.001	-0.0003	999.0	999.0	0.527	0.006
60006.45527	29.125	0.001	0.0014	0.1775	0.0006	0.526	0.007
60007.43307	29.129	0.001	0.0012	0.178	0.0006	0.529	0.007
60008.49984	29.129	0.001	-0.0003	0.1798	0.0007	0.534	0.008

Table D.1: – continued from previous page

BJD (-2400000 d)	RV (km s ⁻¹)	σ_{RV} (km s ⁻¹)	BIS (km s ⁻¹)	S-index	$\sigma_{S-index}$	Na	σ_{Na}
60009.54012	29.129	0.001	0.0006	0.1808	0.0007	0.53	0.007
60010.53674	29.131	0.001	0.0025	0.1809	0.0007	0.528	0.008
60013.52425	29.129	0.001	-0.0012	0.1891	0.0013	0.508	0.011
60016.39097	29.134	0.001	-0.002	0.186	0.001	0.524	0.009

Table D.2: HIRES RVs for HD88986

BJD (-2400000 d)	RV (m s ⁻¹)	σ_{RV} (m s ⁻¹)	S-index
HIRES:			
50420.10946	22.494	1.643	0.1382
50463.00185	20.158	1.406	0.1397
50545.86786	20.750	1.560	0.1422
50787.06992	26.429	3.740	0.1542
50787.07411	28.104	1.608	0.1521
50838.01219	19.714	1.467	0.1527
50954.80494	29.031	1.550	0.1540
50955.75722	25.449	1.522	0.1510
51171.99838	20.624	1.395	0.1508
51229.00435	10.522	1.389	0.1529
51341.82219	21.790	1.538	0.1604
51551.06319	20.628	1.536	0.1382
51982.00707	9.603	1.384	0.1272
52308.02544	10.857	1.870	0.1273
52601.15939	1.742	1.715	0.1373
52712.96215	0.661	1.464	0.1309
52988.06928	2.112	1.521	0.1224
HIRES+:			
53370.00523	8.157	1.533	0.1336
53841.88252	5.906	1.406	0.1361
55289.71865	-1.037	1.585	0.1270
55339.84111	3.448	1.336	0.1425
55669.86880	-0.145	1.349	0.1300
55707.73738	-3.202	1.436	0.1382
55719.83472	1.936	1.365	0.1346
55719.83589	-1.386	1.374	0.1379
55720.79264	1.047	1.365	0.1410
55720.79490	-3.926	1.315	0.1405
55721.81729	-8.243	1.434	0.1409
55721.81885	-5.055	1.434	0.1436
55721.82031	-4.837	1.285	0.1427
55749.77312	-6.456	1.447	0.1434
55749.77472	-4.918	1.348	0.1487
55750.76293	0.377	1.447	0.1403
55750.76616	-2.757	1.536	0.1417
55912.09590	7.933	1.321	0.1332
55912.09693	3.431	1.350	0.1327
55912.09794	3.180	1.400	0.1307
55971.91094	-2.303	1.531	0.1245
55971.91211	-3.924	1.473	0.1274
55971.91332	-1.016	1.531	0.1264
55997.01689	-10.852	1.618	0.1317
56024.88359	-8.907	1.289	0.1367
56024.88929	-14.024	1.346	0.1373
56024.89104	-10.796	1.289	0.1362
56024.89298	-6.688	1.221	0.1371
56329.97966	-5.863	1.541	0.1314
56329.98069	-6.265	1.472	0.1343
56329.98178	-5.186	1.561	0.1368
56676.89512	-3.038	1.427	0.1370
56676.89610	-3.379	1.465	0.1361

Table D.3: ELODIE RVs for HD 88986

BJD (-2 400 000 d)	RV (m s ⁻¹)	σ_{RV} (m s ⁻¹)
50508.4203	29009.240546	7.201594
50509.5491	28987.240514	7.943309
50509.56	28998.240514	7.467904
50510.5337	28995.240487	7.111546
50533.4545	29000.739841	7.351913
50554.435	29012.139250	8.299547
50554.4436	29012.139250	8.843668
50584.3377	29016.838409	8.021465
50770.7146	29026.833161	7.937892
50821.6156	29032.831728	7.838441
50858.5533	29017.030688	7.324449
50885.4545	28999.829930	7.506361
50886.4527	29013.829902	8.826301
50887.4928	29010.829873	8.564956
50939.3686	29016.328412	7.989163
50939.3776	29010.328412	8.438047
50973.345	29005.327455	7.360800
51153.7066	29009.222377	9.974239
51235.5637	29004.820072	7.097413
51505.6993	29002.412466	9.181249
51562.5653	29016.910865	9.396184
51725.365	29003.006281	9.713716
51901.6319	28986.201318	9.321223
51982.4489	29000.399042	8.947926
52723.4565	28984.278178	7.554854
52989.6915	28981.170682	10.367050
52995.6586	28991.170514	7.902043
53033.6212	28987.869445	11.367766

Appendix E: Background contamination of the calibration lamp from the SOPHIE spectra

The combined analysis of RVs and activity indicators plays a crucial role in determining the origin of a signal. To do so, having accurate activity indicators is essential for effectively interpreting the data. In CCD spectrograph images, the recorded light from fibers A and B in a spectral order are located close to each other (e.g., within approximately 17 pixels for SOPHIE). This proximity introduces a small but non-negligible amount of light diffusion, primarily caused by the calibration lamp's light from fiber B to fiber A (Lovis et al. 2011). Consequently, before deriving the activity indexes such as $\log R'_{HK}$ and $H\alpha$, it becomes imperative to subtract the background light originating from the diffuse light emitted by either the Th-Ar or FP calibration lamp present in the star spectrum.

To address this contamination issue, the SOPHIE DRS employs various methods, depending on the calibration lamps used. In the case of the Th-Ar lamp, a background is estimated from the flux of fiber B in the same spectral order by fitting a polynomial function on local minima (Boisse et al. 2010). On the other hand, for the FP lamp, which has been installed since semester 2017B, the background is directly measured using a Dark-FP frame, that is, illumination of fiber B with the FP calibration lamp while keeping fiber A completely dark (Hobson 2019; Lovis et al. 2011). However, as more years of observations were conducted, it became evident that there was a noticeable discrepancy in the data obtained from the two calibration lamps. This discrepancy can be attributed to the utilization of different background correction methods and likely over-estimation of background contamination in the method used in Th-Ar data. In order to rectify this issue, we employed a direct measuring method (Hobson 2019; Lovis et al. 2011) for both calibration lamps. By implementing this approach, we successfully corrected this discrepancy and significantly improved the consistency between data sets obtained using different calibration lamps. This method has been implemented into the SOPHIE DRS and will be utilized in forthcoming SOPHIE planet publications. We applied this method to the SOPHIE spectra prior to deriving the $H\alpha$ and $\log R'_{HK}$ (or S-index) activity indices for HD 88986. We note that we did not use the $H\alpha$ activity indexes in our final analysis due to its high contamination by the telluric.

Appendix F: Priors on HD88986 b for RV-only model

Table F.1: Priors and description of parameters used within `juliet` to model RVs of HD88986 in Sect. 5.2.

Parameter	prior	description
Planet parameters		
P (d)	$\mathcal{U}(135, 155)$	Period of the HD88986 b
$T_c - 2400000$ (d)	$\mathcal{U}(58850, 58850 + 146)$	Center of the transit time for HD88986 b
K (m s^{-1})	$\mathcal{U}(0, 10)$	RV semi-amplitude for HD88986 b
e	$\mathcal{U}(0, 1)$ or 0 (fixed)	Eccentricity
ω ($^\circ$)	$\mathcal{U}(0, 360)$ or 90 (fixed)	Argument of periastron
Telescope Parameters:		
$\sigma_{\text{SOPHIE+}}$ (m s^{-1})	$\mathcal{U}(1e - 3, 100.)$	RV jitter
$\text{mu}_{\text{SOPHIE+}}$ (m s^{-1})	$\log \mathcal{U}(28995, 29196)$	Instrumental offset
Drift on SOPHIE+:		
A (m s^{-1})	$\mathcal{U}(-5, 5)$	Linear RV drift
Q (m s^{-1})	$\mathcal{U}(-5, 5)$	Quadratic RV drift
QP-GP on SOPHIE+:		
B_{GP} (m s^{-1})	$\mathcal{J}(10^{-5}, 100)$	Amplitude of the GP kernel
C_{GP} (m s^{-1})	10^{-20} (fixed)	Constant scaling term of the GP kernel
P_{rot} (d)	$\mathcal{N}(29, 3)$	Rotation period of the GP kernel
L_{GP} (d)	$\mathcal{J}(10^{-20}, 300)$	Correlation time-scale of the GP kernel
EXP-GP on SOPHIE+:		
T_{GP}	$\log \mathcal{U}(1e - 13, 100.)$	Length-scale of the GP kernel
σ_{GP} (m s^{-1})	$\log \mathcal{U}(1e - 13, 100.0)$	Amplitude of the GP kernel
sinusoidal on SOPHIE+:		
P (d)	$\mathcal{U}(25, 35)$	Period for the additional sinusoid
K (m s^{-1})	$\mathcal{U}(58870, 58870 + 30)$	RV semi-amplitude for the additional sinusoid
$T_c - 2400000$ (d)	$\mathcal{U}(0, 10)$	Center of the transit time for additional sinusoid

Notes. The prior labels of \mathcal{N} , \mathcal{U} , $\log \mathcal{U}$ indicate normal, uniform, and uniform logarithms of distributions.

Appendix G: False positive tests

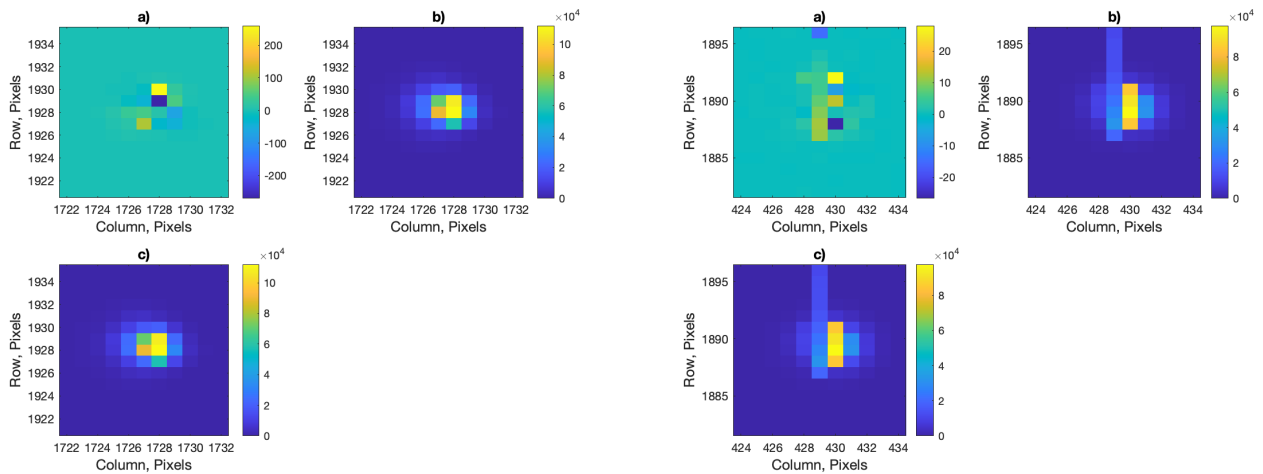


Fig. G.1. Centroid analysis for HD88986. Difference images (panels a) for the potential transits in sector 21 (left) and sector 48 (right), along with the mean out-of-transit image (panel b) and the mean in-transit image (panel c). The difference images are obtained by subtracting the mean in-transit image from the mean out-of-transit image and ideally appear as an isolated stellar image of the host star. We note that in sector 48, the host star is located just beside a bad column. While interpreting the difference images from saturated stars such as HD88986 is particularly challenging, we observed that most of the energy in the transit feature is associated with the upper end of the bleed of the saturated pixels in the core of the stellar image. Thus, the transit features are likely associated with the host star in both sectors.

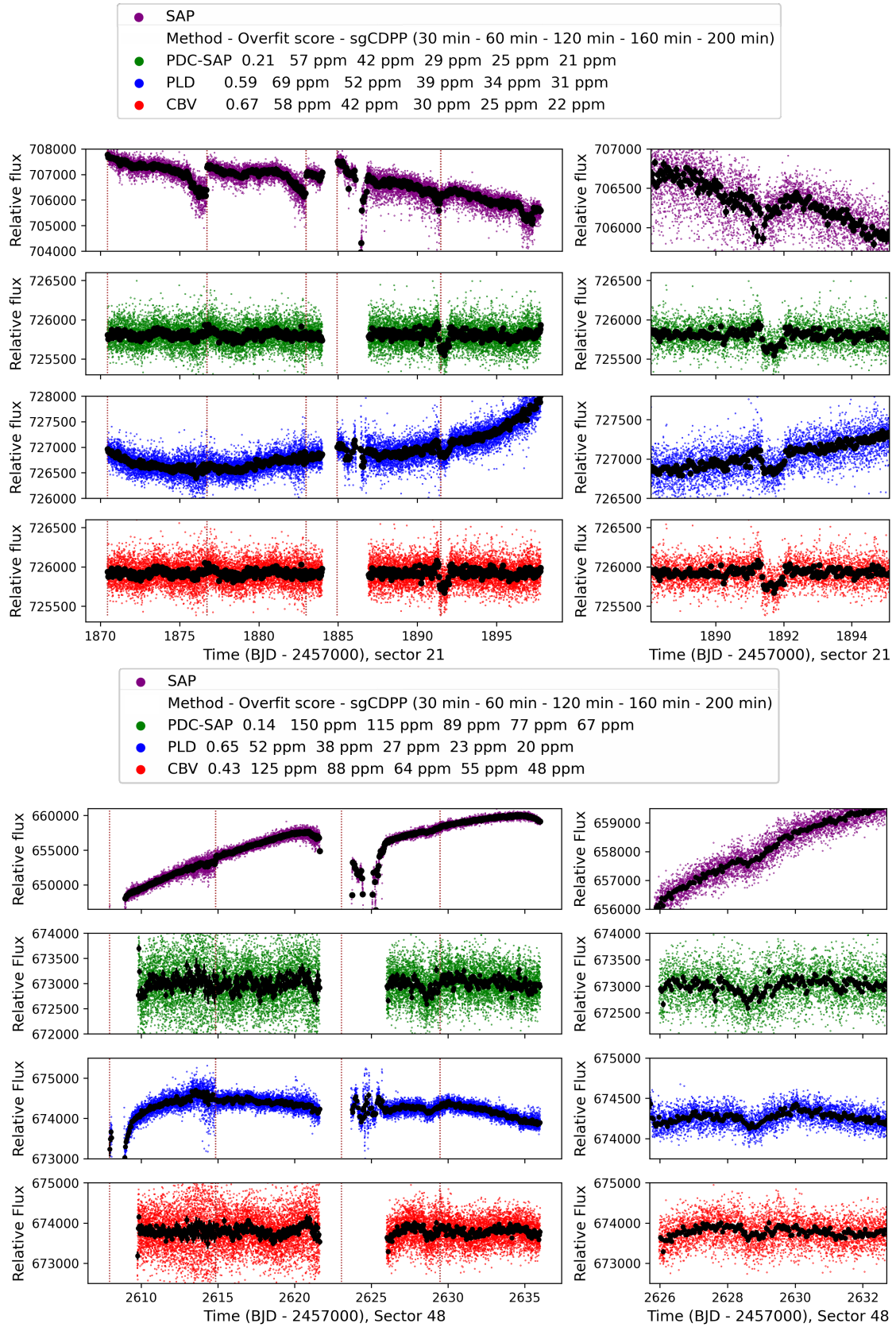


Fig. G.2. TESS light curves reproduced using PLD and CBV approaches (*left panels*) and zoomed in the potential single transits (*right panels*) for sector 21 (*top*) and sector 48 (*bottom*). The SAP and PDC-SAP data are also plotted to provide a reference for comparison. The data are binned (black points) in 1 hour. The legend includes an overfitting score and the sgCDPP metric to facilitate an assessment of the different light curves. The brown vertical lines are the telescope momentum dumps.

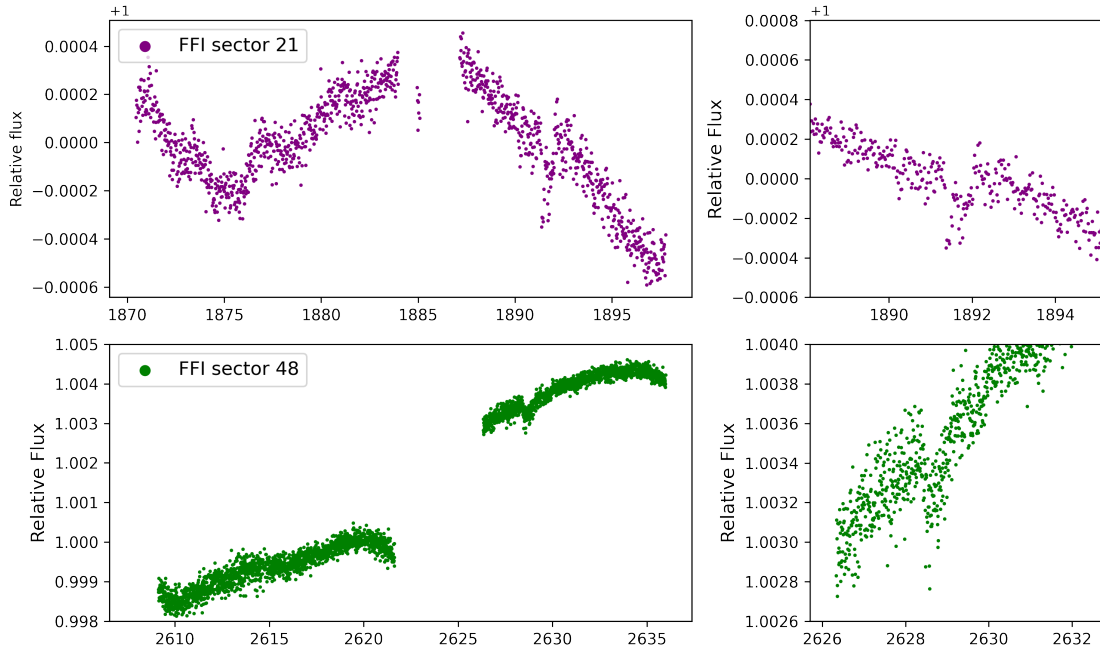


Fig. G.3. TESS data extracted from FFI for sector 21 (*top*) and sector 48 (*bottom*). The data are zoomed in on the potential single transits in the right panels.

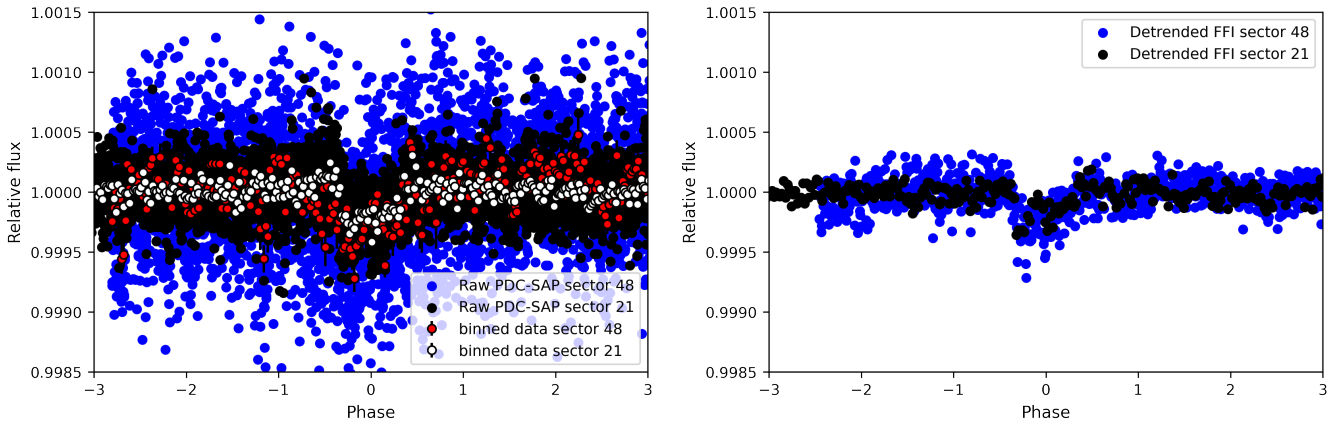


Fig. G.4. Raw PDC-SAP (*left*) and detrended FFI (*right*) phase-folded data from sector 21 and sector 48 with a period of 147.4 d. The PDC-SAP data were binned in 30 minutes to ensure compatibility with the FFI data.

Appendix H: Priors on joint modeling of RV and photometric data

Table H.1: Priors for the joint modeling of RV and photometric data with `juliet` in Sect. 7

Parameter	prior	description
Stellar parameters:		
ρ_* (kg/m ³)	$\mathcal{N}(479.768, 40)$	Stellar density
Planet parameters		
P (d)	$\mathcal{U}(135, 155)$	Period of HD88986 b
$T_c - 2400000$ (d)	$\mathcal{N}(2458891.6, 5)$	Center of the transit time for HD88986 b
K (m s ⁻¹)	$\mathcal{U}(0, 10)$	RV semi-amplitude for HD88986 b
e	$\mathcal{U}(0, 0.9)$	Eccentricity
ω (°)	$\mathcal{U}(0, 360)$	Argument of periastron
b	$\mathcal{U}(0, 1)$	Transit impact parameter
R_p/R_*	$\mathcal{U}(0, 1)$	Planet-to-star radius ratio
Drift on SHOPHIE+:		
A (m s ⁻¹)	$\mathcal{U}(-5, 5)$	Linear RV drift
Q (m s ⁻¹)	$\mathcal{U}(-5, 5)$	Quadratic RV drift
QP-GP on SOPHIE+:		
B_{GP} (m s ⁻¹)	$\mathcal{J}(10^{-5}, 100)$	Amplitude of the GP kernel
C_{GP} (m s ⁻¹)	10^{-20} (fixed)	Constant scaling term of the GP kernel
P_{rot} (d)	$\mathcal{N}(29, 3)$	Rotation period of the GP kernel
L_{GP} (d)	$\mathcal{J}(10^{-20}, 300)$	Correlation time-scale of the GP kernel
SOPHIE instrumental Parameters:		
$\sigma_{SOPHIE+}$ (m s ⁻¹)	$\log \mathcal{U}(1e - 3, 100.)$	RV jitter
$\mu_{SOPHIE+}$ (m s ⁻¹)	$\mathcal{U}(28995, 29196)$	Instrumental offset
TESS instrumental parameters:		
D_{TESS}	1.0 (fixed)	Dilution factor
M_{TESS}	$\mathcal{N}(0., 1)$	Relative flux offset
σ_{TESS}	$\log \mathcal{U}(0.1, 1000.)$	Extra jitter term
q	$\mathcal{U}(0, 1)$	Linear limb-darkening

Notes. The prior labels of \mathcal{N} , \mathcal{U} , $\log \mathcal{U}$ indicate normal, uniform, and uniform logarithms of distributions.

Appendix I: Priors on joint modeling of RV and Hipparcos/Gaia astrometric data

Table I.1: Priors for the joint modeling of RV and Hipparcos/Gaia astrometric data.

Parameter	prior	description
Stellar parameters:		
M_* (M_\odot)	$\mathcal{N}(1.2, 0.06)$	Stellar mass
Parallax (mas)	$\mathcal{N}(30.025, 0.023)$	Stellar parallax
σ_* (m s ⁻¹)	$\mathcal{U}(0, 10)$	Stellar jitter
Planet parameters		
a (au)	$\mathcal{U}(1, 100)$	Semi-major axis of HD88986 c
e	$\mathcal{U}(0, 0.99)$	Eccentricity
ω (°)	$\mathcal{U}(0, 360)$	Argument of periastron
I (°)	$\sin(0, 180)$	Orbital inclination
Ω (°)	$\mathcal{U}(0, 360)$	Longitude of ascending node
M_c (M_{Jup})	$\mathcal{U}(1, 500)$	Mass of HD88986 c
SOPHIE instrumental Parameters:		
μ_{ELODIE} (m s ⁻¹)	$\mathcal{U}(28000, 30000)$	ELODIE offset
μ_{SOPHIE} (m s ⁻¹)	$\mathcal{U}(28000, 30000)$	SOPHIE offset
$\mu_{SOPHIE+}$ (m s ⁻¹)	$\mathcal{U}(28000, 30000)$	SOPHIE+ offset
μ_{HIRES} (m s ⁻¹)	$\mathcal{U}(-1000, 1000)$	HIRES offset
μ_{HIRES+} (m s ⁻¹)	$\mathcal{U}(-1000, 1000)$	HIRES+ offset

Notes. The prior labels of \mathcal{N} , \mathcal{U} , \sin indicate normal, uniform, and sinusoidal distributions.

Appendix J: Corner plot of the joint modeling SOPHIE+ RVs and TESS sector 21 photometry

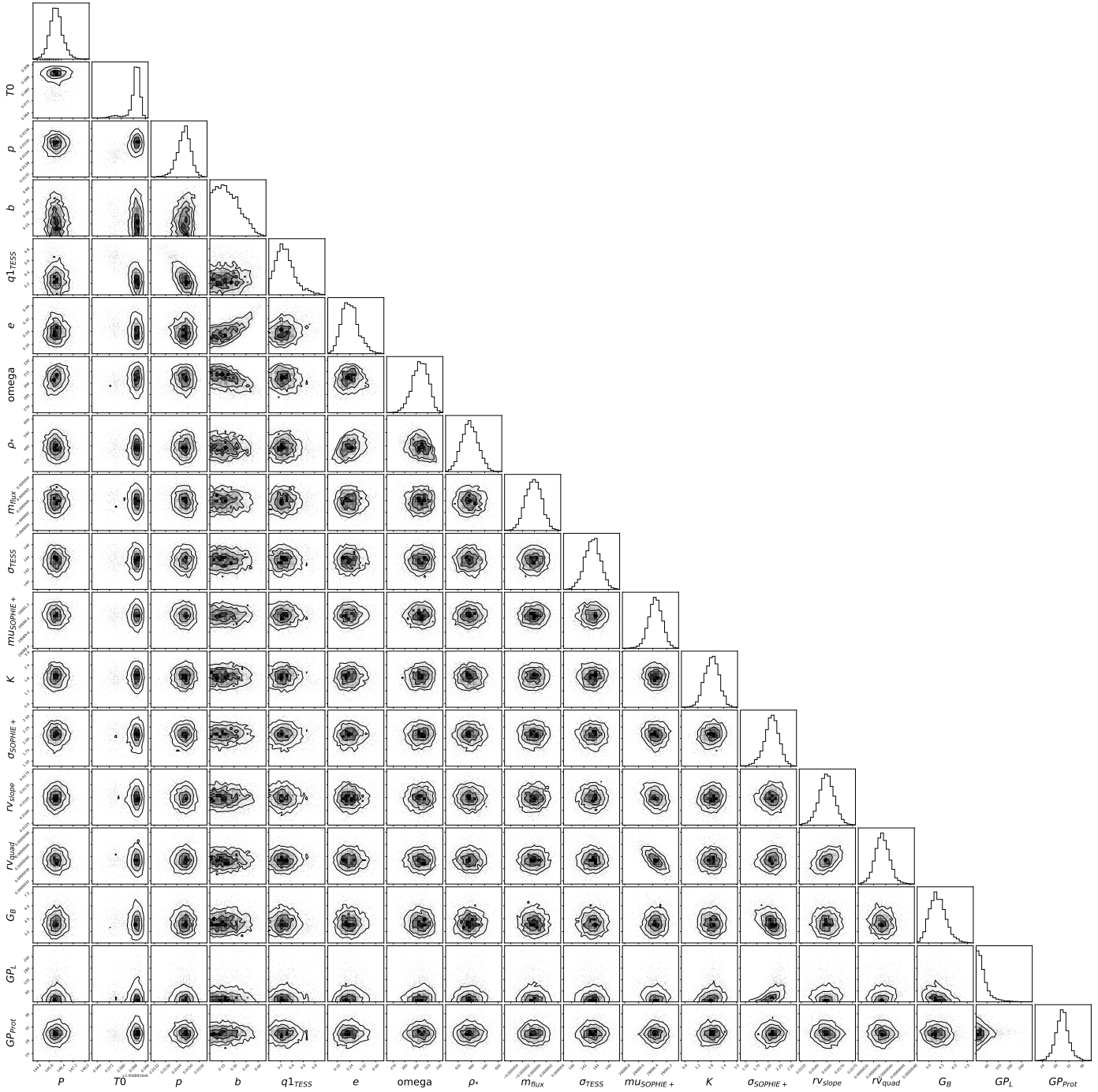


Fig. J.1. Nested samples distribution of fitted parameters of HD88986 b on joint modeling of SOPHIE+ RVs and TESS sector 21 light curve. The 1, 2, and 3 σ confidence levels of the posterior samples are shown by the contours.

Appendix K: Corner plot of the joint modeling of combined HD88986 RVs, Hipparcos and Gaia astrometry

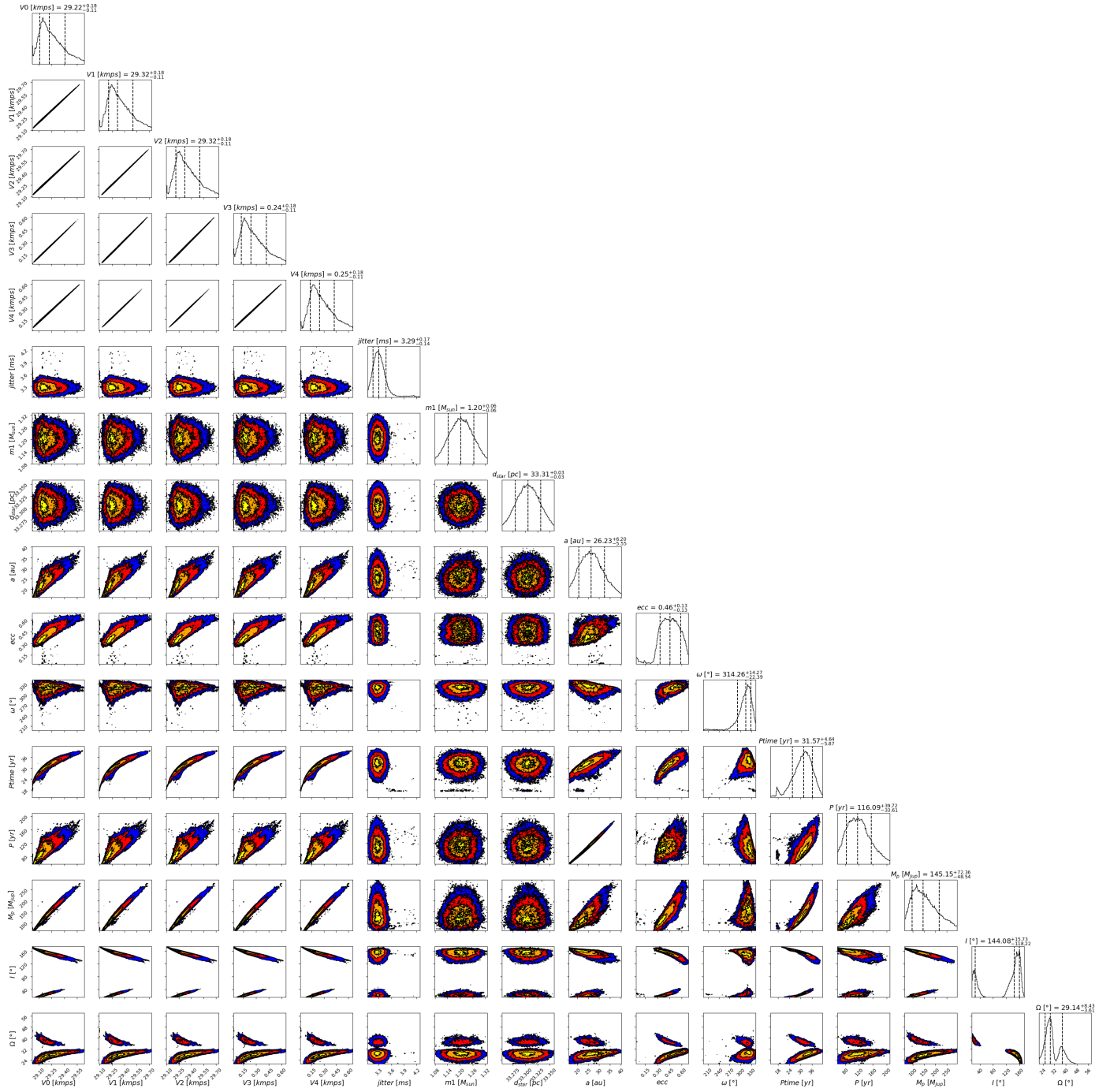


Fig. K.1. MCMC samples distribution of fitted parameters of HD88986 outer massive companion on joint modeling of HD88986 RVs and Hipparcos/Gaia astrometry. V0, V1, V2, V3, and V4 correspond to the ELODIE, SOPHIE, SOPHIE+, HIRES, and HIRES+ RV dataset, respectively.

Appendix L: APT photometric data

Table L.1: Summary of APT photometric observation for HD88986

Observing Season	N_{obs}	Date Range (HJD - 2,400,000)	σ (mag)	Seasonal Mean (mag)
1995-96	18	50192-50235	0.00129	-1.16507(30)
1996-97	46	50395-50597	0.00083	-1.16476(12)
1997-98	68	50755-50978	0.00140	-1.16513(17)
1998-99	72	51115-51339	0.00146	-1.16529(17)
1999-00	60	51480-51706	0.00116	-1.16500(15)
2000-01	43	51862-52051	0.00104	-1.16486(16)
2001-02	60	52202-52445	0.00114	-1.16421(15)
2002-03	75	52572-52805	0.00108	-1.16476(13)
2003-04	78	52930-53171	0.00099	-1.16492(11)
2004-05	104	53308-53529	0.00132	-1.16491(13)
2005-06	109	53663-53904	0.00138	-1.16509(13)
2006-07	99	54032-54259	0.00119	-1.16453(12)
2007-08	62	54391-54630	0.00101	-1.16479(13)
2008-09	44	54774-54983	0.00086	-1.16511(13)
2009-10	75	55139-55351	0.00116	-1.16494(13)
2010-11	71	55513-55709	0.00105	-1.16474(12)
2011-12	61	55893-56069	0.00109	-1.16472(14)
2012-13	38	56236-56447	0.00068	-1.16502(11)
2013-14	51	56607-56809	0.00097	-1.16539(14)
2014-15	67	56967-57176	0.00118	-1.16532(14)
2019-20	34	58856-58975	0.00117	-1.16518(20)