

Evaluating Climate Variability of the Canonical Hot-Jupiters HD 189733b and HD 209458b through Multi-epoch Eclipse Observations

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Abstract

Here we present the analysis of multi-epoch secondary eclipse observations of HD 189733b and HD 209458b as a probe of temporal variability in the planetary climate using both *Spitzer* channels 1 and 2 (3.6 and 4.5 μ m). We expect hot-Jupiter atmospheres to be dynamic environments exhibiting time varying weather. However, it is uncertain to what extent temporal variability will be observable when considering disk integrated observations. We do not detect statistically significant variability and are able to place useful upper limits on the infrared variability amplitudes in these atmospheres. There are very few planets with multi-epoch observations at the required precision to probe variability in dayside emission. The observations considered in this study span several years, providing insight into temporal variability at multiple timescales. In the case of HD 189733b, the best-fit eclipse depths for the channel 2 observations exhibit a scatter of 102 ppm about a median depth of 1827 ppm and in channel 1 exhibit a scatter of 88 ppm about a median depth of 1481 ppm. For HD 209458b, the best-fit eclipse depths for the channel 2 observations exhibit a scatter of 22 ppm about a median depth of 1406 ppm, and in channel 1 exhibit a scatter of 131 ppm about a median depth of 1092 ppm. The precision and scatter in these observations allow us to constrain variability to less than (5.6% and 6.0%) and (12% and 1.6%) for channels (1, 2) of HD 189733b and HD 209458b, respectively.

Unified Astronomy Thesaurus concepts: Exoplanet atmospheres (487); Exoplanet atmospheric variability (2020); Exoplanet astronomy (486); Exoplanet structure (495)

1. Introduction

Studying exoplanet atmospheres is challenging since we often are not able to spatially resolve them. They are typically too faint to disentangle their light from that of their much brighter host star. Transiting exoplanets provide a unique opportunity to study exoplanet atmospheres in spite of this challenge. Disk integrated secondary eclipse observations provide valuable information on temperature, albedo, and chemical composition averaged over the entire hemisphere. Primary transits give a limb averaged atmospheric molecular spectrum and pressure-temperature profile. However, we must employ other novel techniques to begin to probe physical and chemical processes and structures at smaller scales. Temporal variability is one way to probe weather features and their movements without spatially resolving them. Variability is also a tool to study portions of the atmosphere inaccessible via other observational techniques. Transmission spectroscopy observations in the near-infrared typically probe millibar pressure levels high in the atmosphere. Processes deeper in the atmosphere are obscured due to the long path lengths of the transit geometry. Time varying changes in emission may be indicative of processes occurring deeper in the atmosphere that are, otherwise, unobservable with current methods and instruments.

Close-in giant planets (hot Jupiters) are interesting objects with which to study atmospheric dynamics. They are assumed to be tidally locked based on their short orbital periods (<5 days) and minimal separation from their host stars. As a result, they experience a constant radiative forcing on their permanent dayside. The combination of the rotation rate and radiative forcing of these planets are predicted to produce large-scale weather structures unlike anything in our solar system.

There have been many efforts to model the circulation and temperature structure of hot Jupiters with many of these efforts based on the properties of the two most well-studied targets, HD 189733b and HD 209458b (HD 189733b and HD 209). Simulations by Showman & Guillot (2002), Cho et al. (2003), and Menou et al. (2003) predicted that the Rossby deformation radius and Rhines scale of hot Jupiters should be comparable to the planetary radius resulting in atmospheric dynamics comprised of a few jets and large-scale polar vortices. They predicted that vortices would be large enough that their migration could have an affect on the observed eclipse depth. Rauscher et al. (2007) demonstrated that, based on those model predictions, changes in eclipse depth as great as 20% could be observed. Later simulations by Showman et al. (2009) predicted far more stable atmospheric structures. Variability was predicted to be less than several percent for HD 189733b at

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 $8 \mu m$ and the result of wave dynamics deep in the atmosphere rather than migrating vortices.

Agol et al. (2010) observationally probed model predictions with a multi-epoch set of transit and eclipse observations of HD 189733b at 8 μ m. The results of that work placed an upper limit on eclipse depth variability at 2.7%, effectively ruling out larger predictions. There have been few other attempts to study temporal variability due to the lack of multiple observations over a sufficient temporal baseline.

We choose as our targets for this study, HD 189733b and HD 209458b, both because of their suitability for observations with the *Spitzer* observatory and because they are the only targets with a large number of observations with a single instrument spanning a number of years. These two planets are the most well-studied and characterized exoplanets to date. Both orbit bright stars, $K_{\rm mag}$ of 5.5 and 6.3 for HD 189733b and HD 209458b, respectively, making them ideal targets for characterization and have previously observed secondary eclipse depths >1000 ppm in both warm *Spitzer* channels 1 and 2.

HD 189733b is arguably the most thoroughly studied exoplanet. It has been observed with photometric (e.g., Ehrenreich et al. 2007; Désert et al. 2009, 2011b) and spectroscopic (e.g., Gibson et al. 2012) transits as well as secondary eclipse (e.g., Charbonneau et al. 2008; Agol et al. 2010) and phase curve (Knutson et al. 2007, 2009, 2012) observations across a multitude of wavelengths. In addition to full orbit phase curves at multiple wavelengths, it is the only planet to have been mapped via the eclipse mapping technique (de Wit et al. 2012; Majeau et al. 2012; Rauscher et al. 2018). HD 209458b was the first transiting exoplanet discovered (Charbonneau et al. 2000). It has also been observed in both transit and eclipse geometries photometrically (e.g., Charbonneau et al. 2008; Diamond-Lowe et al. 2014) and spectroscopically (e.g., Deming et al. 2013; Line et al. 2016), as well as full orbit phase curve observations (Zellem et al. 2014).

The large amount of observational and theoretical effort invested into these two canonical hot Jupiters make them perfect choices for a study of this nature. There are eclipse observations from multiple programs spanning years from which to build the necessary temporal baseline. Additionally, their orbital properties are well studied and well constrained allowing for the detection of small signals in their light curves due to planetary thermal structure that can be clearly distinguished from other potential sources such as orbital eccentricity.

Understanding variability will be essential in current and future attempts to leverage multiple epoch observations to build precision for high resolution techniques. When stacking observations, whether it be transmission spectroscopy or emission photometry, one makes the assumption that each observation is an independent measurement of a constant signal. Showing that any temporal variability is below the level of precision of your observations allows them to be combined in analysis. If this set of *Spitzer* observations are not sensitive to temporal variability they can be combined to achieve the precision necessary to perform eclipse mapping.

Eclipse mapping (de Wit et al. 2012; Majeau et al. 2012) uses the deviations to the shape of ingress and egress caused by a nonuniform dayside temperature distribution to create two-dimensional thermal maps. In general, one needs ~ 10 points over the ingress/egress with a precision of at least a tenth of the

Table 1
Summary of Observations of HD 209458b

Program	AOR	Channel	Date
60021	41629440	1	2011 Jan 12
60021	41628416	1	2011 Jan 15
90186	48013824	1	2013 Aug 28
10103	50496512	1	2014 Jan 19
10103	50496256	1	2014 Feb 27
10103	50496000	1	2014 Feb 6
10103	50495744	1	2014 Aug 22
10103	50495488	1	2014 Aug 29
10103	50494976	1	2014 Sep 5
10103	50494208	1	2014 Sep 27
10103	50493440	1	2015 Jan 24
10103	50492928	1	2015 Jan 28
10103	50490880	2	2014 Jan 26
10103	50490624	2	2014 Feb 2
10103	50490368	2	2014 Aug 19
10103	50490112	2	2014 Aug 26
10103	50489856	2	2014 Sep 12
10103	50489088	2	2014 Jan 7
90186	48014336	2	2013 Aug 31
60021	38703616	2	2010 Jan 21

eclipse depth to achieve the necessary resolution to map hot Jupiters. The only way to achieve that precision with current observatories is to stack multiple observations. In the *James Webb Space Telescope* (*JWST*) era, observing time will be expensive and full orbit phase curves may prove too costly. However, mapping may be done much more efficiently with as little as two eclipse observations. Understanding temporal variability then is crucial in knowing if stacking multi-epoch observations is justifiable in that context. The observations considered here give the best current insight into orbit to orbit changes in hot-Jupiter atmospheres.

2. Observations

Here we consider all existing secondary eclipse observations of HD 189733b and HD 209458b in channels 1 and 2 (3.6 or 4.5 μ m bandpass). The observations analyzed here are part of Programs 60021 (PI: H. Knutson), 10103 (PI: N. Lewis), 90186 (PI: K. Todorov), and 70100 (PI: M. Swain). The details of each astronomical observing request (AOR) are displayed in Tables 1 and 2. All of the observations were carried out in subarray mode (32 \times 32 pixels, 39" \times 39"). Observations in Program 10103 utilize a 30 minute peak-up observation preceding them to stabilize the image on the detector "sweet spot" and decreases the likelihood of a ramp in the data (Ingalls et al. 2012). Program 60021 observations are full orbit phase curves from which we extract the AORs containing the eclipse from the larger data set. Both HD 189733 and HD 209458 are bright targets with a K_{mag} of 5.5 and 6.3 respectively. As a result, frame times for all of the observations are 0.1 s. The two exceptions are the observations of HD 209458b in channel 2 that were conducted with a 0.4 s frame time and the observations of HD 189733b from Program 70100 that were conducted such that the stellar centroid was near the corner of the pixel so that a longer (0.4 s) exposure time could be used. This technique proved problematic in that the systematics were not easily corrected with existing techniques and, as a result, several of these observations were discarded from this study.

Table 2
Summary of Observations of HD 189733b

Program	AOR	Channel	Date
10103	50495232	1	2014 Jan 7
10103	50494464	1	2014 Jan 14
10103	50493696	1	2014 Jan 25
10103	50493184	1	2014 Jul 15
60021	41592320	1	2010 Dec 28
60021	41591296	1	2010 Dec 30
70100	40150528	1	2010 Nov 24
70100	40151040	1	2011 Jan 3
70100	40151296	1	2011 Jun 23
70100	40152064	1	2011 Jun 27
10103	50489344	2	2014 Jan 12
10103	50488832	2	2014 Jan 18
10103	50488576	2	2014 Jul 13
10103	50488320	2	2014 Jul 26
10103	50488064	2	2014 Aug 11
60021	38390784	2	2009 Dec 22
60021	38390016	2	2009 Dec 24

3. Data Analysis Methods

3.1. Photometric Extraction

For each AOR we began with basic calibrated data (BCD) available on the *Spitzer* Heritage Archive. Each BCD file contains a cube of 64 frames of 64×64 pixels. Each set of 64 images comes as a single FITS file with a time stamp corresponding to the start of the first image. We determine the time of each frame in the set by adding the appropriate multiple of the frame time to the time stamp of the first image. Each frame was corrected for bad pixels or unrepresentable (NaN) values by masking the invalid pixels. Each frame is background subtracted based on the median pixel value outside of a 10×10 pixel box around the stellar centroid. Pixel values in the background region that deviate from the mean by more than 5σ are clipped and the median value remaining is taken to be the background. Stellar centroid positions for each frame are determined by a first moment center of mass calculation

$$x_{\text{cen}} = \frac{\sum_{j,k} (I_{jk}j)}{\sum_{i,k} I_{jk}}; \qquad y_{\text{cen}} = \frac{\sum_{j,k} (I_{jk}k)}{\sum_{i,k} I_{jk}}.$$
 (1)

We perform two-dimensional Gaussian centroiding as well but find the first moment calculation to be more stable and it provides less scatter in the extracted photometry.

The noise pixel parameter ($\tilde{\beta}$; Lewis et al. 2013; Kilpatrick et al. 2017) is calculated for each frame as

$$\tilde{\beta} = \frac{(\sum P_i)^2}{\sum (P_i^2)},\tag{2}$$

where each P_i is the response measured in each pixel across the frame. We also save the 5 \times 5 array of the background subtracted pixel values about the stellar centroid for each frame. Each array is normalized such that they sum to one. We then perform aperture photometry about the stellar centroid using the aperture_photometry function from the Astropy package Photutils. Circular apertures of fixed radii range from 1.8 to 2.8 pixels and variable radii apertures range from $\beta_{\rm pix} \times \{0.7...1.2\}$ and $\beta_{\rm pix} + \{-0.6...1.4\}$. The resultant timeseries photometry is then filtered by removing any points that

deviate by more than 3σ from the median values of flux or x,y position.

3.2. Systematics Correction and Model Fitting

The intrapixel sensitivity variation (Ingalls et al. 2012), the change in measured flux as a function of stellar centroid position, and methods of correction are well documented (e.g., Ingalls et al. 2016; Kilpatrick et al. 2017). Here, we employ two independent methods of correction for this systematic variation: the nearest neighbors method, otherwise known as Gaussian kernel regression with data (Lewis et al. 2013) and pixel level decorrelation (PLD; Deming et al. 2015).

Each eclipse fit was based on the model of Mandel & Agol (2002) for a uniform occultation implemented in python by the BATMAN package (Kreidberg 2015). The orbital, stellar, and planetary parameters listed in Table 3 were used as input fixed parameters to the model. *Spitzer* IRAC data is known to have an exponential ramp in flux over the first 30–60 minutes of observing, however the peak-up technique has alleviated this problem to some extent (Ingalls et al. 2012; Kilpatrick et al. 2017). As a precaution, each data set was fit in several ways: without alteration, trimmed at 20 minutes from the beginning of the observation, and with an exponential ramp model of the form

$$R_{\text{model}} = 1 - a_1 \times e^{\left(-\frac{t}{a_2}\right)}. \tag{3}$$

PLD has a quadratic visit long temporal variation included in all cases rather than the exponential ramp and combines the systematics and astrophysical models by a linear expression

$$\Delta S^{t} = \sum_{i=1}^{n} c_{i} \hat{P}_{i}^{t} + DE(t) + ft + gt^{2} + h, \tag{4}$$

where the \hat{P}_i^t 's are the response of the *i*th pixel in a 3 × 3 grid around the centroid of the image and DE(t) is the eclipse model and ΔS^t is the total flux, including the astrophysical signal and all systematics, at each time t.

For each AOR the eclipse model and systematics model were combined and best-fit values for all free parameters were determined using a nonlinear, least-squares fitting algorithm. The standard deviation of the normalized residuals (SDNR) was used as a metric for selecting the best fit out of the 30 different apertures for each AOR. The Bayesian information criterion (BIC) was used to determine the appropriate treatment between various trimming and ramp model options. We find that no trimming or exponential ramp are necessary in all cases of channel 2 observations and the quadratic ramp with PLD is favored in all channel 1 observations. The results from the bestfit aperture were passed to a Markov Chain Monte Carlo implemented by emcee (Foreman-Mackey et al. 2013) to derive uncertainties of each free parameter. We use a number of walkers at least twice the number of free parameters and run for 10⁵ steps per walker before testing for convergence using Gelman Rubin statistics with a threshold for acceptance of 1.01 (Gelman & Rubin 1992).

4. Results

Here we present the best-fit eclipse depths and center of eclipse times, along with their corresponding uncertainty, for each of the observations. The results presented in Table 4 are derived using the PLD method with a quadratic temporal term.

Table 3 Ephemerides

Parameter	HD 189733b	HD 209458b 6065 ± 50	
$T_{\star}(K)$	5040 ± 50		
$M_{\star} (M_{\rm Sun})$	0.806 ± 0.048	1.131 ± 0.026	
$R_{\star} (R_{\mathrm{Sun}})$	0.756 ± 0.018	1.155 ± 0.015	
$M_p (M_{\rm Jup})$	1.144 ± 0.056	0.690 ± 0.024	
$R_p (R_{\text{Jup}})$	1.138 ± 0.027	1.359 ± 0.015	
R_p/R_{\star}	$0.024122 \pm 5.8 \times 10^{-5}$	$0.014607 \pm 2.4 \times 10^{-5}$	
$\log(g) (\log(c s^{-2}))$	3.339 ± 0.03	2.969 ± 0.0187	
Period (days)	$2.21857567 \pm 1.5 \times 10^{-7}$	$3.52474859 \pm 3.8 \times 10^{-7}$	
<i>i</i> (°)	85.7100 ± 0.0023	86.710 ± 0.05	
$m \sin i (M_{\text{Jup}})$	1.140 ± 0.056	0.689 ± 0.024	
a/R_{\star}	8.84 ± 0.27	8.81 ± 0.186	

Table 4
Results of the Best-fit Eclipse Depth and Time

$\begin{array}{c ccccccccccccccccccccccccccccccccccc$		Results of the Be	est-fit Eclipse Depth a	nd Time			
38703616	AOR		1	SDNR	$\beta_{\rm red}$		
48014336		HI	209458b Ch 2				
50489088 1424 ± 60 3.03 ± 0.90 0.003085 1.16 50490880 1380 ± 58 1.62 ± 0.79 0.003053 1.27 50490624 1443 ± 56 3.14 ± 0.82 0.003060 1.27 50490368 1417 ± 45 2.60 ± 0.96 0.003151 1.05 50490112 1420 ± 52 2.81 ± 0.72 0.003125 1.18 50489856 1424 ± 47 1.57 ± 0.65 0.003116 1.05 HD 209458b Ch 1 48013824 1050 ± 73 4.37 ± 1.61 0.004995 2.55 50496512 909 ± 60 1.48 ± 1.27 0.004873 1.95 50496000 1162 ± 77 3.38 ± 1.39 0.004805 1.95 50495744 845 ± 92 4.21 ± 1.84 0.005055 2.25 50495488 1008 ± 76 1.81 ± 1.37 0.004996 1.03 50494976 1049 ± 78 2.48 ± 1.30 0.004898 2.03 50493440 1301 ± 76 2.20 ± 1.15 0.0049966 2.03 50492928 <td>38703616</td> <td>1370 ± 37</td> <td>2.22 ± 1.04</td> <td>0.003240</td> <td>1.43</td>	38703616	1370 ± 37	2.22 ± 1.04	0.003240	1.43		
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	48014336	1401 ± 42	1.44 ± 0.83	0.003085	1.17		
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	50489088	1424 ± 60	3.03 ± 0.90	0.003085	1.16		
50490368 1417 ± 45 2.60 ± 0.96 0.003151 1.05 50490112 1420 ± 52 2.81 ± 0.72 0.003125 1.18 50489856 1424 ± 47 1.57 ± 0.65 0.003116 1.05 HD 209458b Ch 1 48013824 1050 ± 73 4.37 ± 1.61 0.004995 2.59 50496512 909 ± 60 1.48 ± 1.27 0.004873 1.96 50496000 1162 ± 77 3.38 ± 1.39 0.004834 1.96 50496256 1209 ± 67 2.81 ± 1.13 0.004805 1.95 50495744 845 ± 92 4.21 ± 1.84 0.005055 2.25 50494976 1049 ± 78 2.48 ± 1.30 0.004898 2.03 50494208 1209 ± 72 1.61 ± 1.36 0.0049606 2.03 50493440 1301 ± 76 2.20 ± 1.15 0.004983 1.87 50492928 994 ± 105 6.82 ± 2.61 0.004939 2.74 41628416 1128 ± 72 1.99 ± 2.72 0.006168 3.68 <td <="" colspan="2" td=""><td>50490880</td><td>1380 ± 58</td><td>1.62 ± 0.79</td><td>0.003053</td><td>1.27</td></td>	<td>50490880</td> <td>1380 ± 58</td> <td>1.62 ± 0.79</td> <td>0.003053</td> <td>1.27</td>		50490880	1380 ± 58	1.62 ± 0.79	0.003053	1.27
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	50490624	1443 ± 56	3.14 ± 0.82	0.003060	1.27		
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	50490368	1417 ± 45	2.60 ± 0.96	0.003151	1.05		
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	50490112	1420 ± 52	2.81 ± 0.72	0.003125	1.18		
$\begin{array}{c} 48013824 & 1050 \pm 73 & 4.37 \pm 1.61 & 0.004995 & 2.59 \\ 50496512 & 909 \pm 60 & 1.48 \pm 1.27 & 0.004873 & 1.99 \\ 50496000 & 1162 \pm 77 & 3.38 \pm 1.39 & 0.004834 & 1.96 \\ 50496256 & 1209 \pm 67 & 2.81 \pm 1.13 & 0.004805 & 1.95 \\ 50495744 & 845 \pm 92 & 4.21 \pm 1.84 & 0.005055 & 2.29 \\ 50495488 & 1008 \pm 76 & 1.81 \pm 1.37 & 0.004946 & 1.78 \\ 50494976 & 1049 \pm 78 & 2.48 \pm 1.30 & 0.004898 & 2.03 \\ 50494208 & 1209 \pm 72 & 1.61 \pm 1.36 & 0.0049606 & 2.03 \\ 50493440 & 1301 \pm 76 & 2.20 \pm 1.15 & 0.004983 & 1.87 \\ 5049228 & 994 \pm 105 & 6.82 \pm 2.61 & 0.004939 & 2.74 \\ 41629440 & 1216 \pm 77 & 1.28 \pm 2.32 & 0.006171 & 4.14 \\ 41628416 & 1128 \pm 72 & 1.99 \pm 2.72 & 0.006168 & 3.68 \\ \hline & & & & & & & & & & & \\ \hline & & & & &$	50489856	1424 ± 47	1.57 ± 0.65	0.003116	1.09		
$\begin{array}{cccccccccccccccccccccccccccccccccccc$		Н	209458b Ch 1				
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	48013824	1050 ± 73	4.37 ± 1.61	0.004995	2.59		
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	50496512	909 ± 60	1.48 ± 1.27	0.004873	1.99		
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	50496000	1162 ± 77	3.38 ± 1.39	0.004834	1.96		
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	50496256	1209 ± 67	2.81 ± 1.13	0.004805	1.95		
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	50495744	845 ± 92	4.21 ± 1.84	0.005055	2.29		
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	50495488	1008 ± 76	1.81 ± 1.37	0.004946	1.78		
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	50494976	1049 ± 78	2.48 ± 1.30	0.004898	2.03		
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	50494208	1209 ± 72	1.61 ± 1.36	0.0049606	2.03		
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	50493440	1301 ± 76	2.20 ± 1.15	0.004983	1.87		
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	50492928	994 ± 105	6.82 ± 2.61	0.004939	2.74		
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	41629440	1216 ± 77	1.28 ± 2.32	0.006171	4.14		
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	41628416	1128 ± 72	1.99 ± 2.72	0.006168	3.68		
$\begin{array}{cccccccccccccccccccccccccccccccccccc$		HI	D 189733b Ch 2				
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	38390784	1812 ± 50	1.52 ± 0.69	0.004596	1.65		
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	38390016	1806 ± 64	0.31 ± 0.97	0.004698	1.74		
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	50489344	1716 ± 55	0.96 ± 0.45	0.004631	1.06		
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	50488832	1815 ± 61	-0.37 ± 0.61	0.004606	1.41		
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	50488576	1984 ± 75	0.31 ± 0.64	0.004630	1.31		
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	50488320	1774 ± 50	0.24 ± 0.55	0.004572	1.12		
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	50488064	2016 ± 65	-0.02 ± 0.48	0.004654	1.00		
$\begin{array}{cccccccccccccccccccccccccccccccccccc$		HI	D 189733b Ch 1				
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	41592320	1574 ± 305	1.40 ± 6.0	0.004228	4.55		
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	41591296	1431 ± 86	0.29 ± 1.74	0.003382	2.13		
50494464 1473 ± 73 0.81 ± 0.93 0.003298 1.50 50493696 1498 ± 53 0.80 ± 0.67 0.003266 1.54	40152064	1271 ± 310	0.16 ± 4.08	0.001708	3.76		
50493696 1498 ± 53 0.80 ± 0.67 0.003266 1.54	50495232	1514 ± 105	-0.37 ± 1.35	0.003370	1.51		
	50494464	1473 ± 73	0.81 ± 0.93	0.003298	1.50		
	50493696	1498 ± 53	0.80 ± 0.67	0.003266	1.54		
		1491 ± 115	-0.74 ± 1.37	0.003306	1.85		

No additional trimming or ramps are modeled. The best-fit aperture was consistently a fixed radius aperture between 2.2 and 2.4 pixels. We include in Table 4 the SDNR and the $\beta_{\rm red}$

factor, as defined in Gillon et al. (2010), as a measure of correlated noise remaining in the data after systematic corrections. Included in Figure 1 are representative fits for each of the two targets in each of the two channels with the systematics removed and binned at two minute intervals. In the case of HD 189733b, the best-fit eclipse depths for the channel 2 observations exhibit a scatter of 102 ppm about a median depth of 1827 ppm and in channel 1 exhibit a scatter of 88 ppm about a median depth of 1481 ppm. For HD 209458b, the best-fit eclipse depths for the channel 2 observations exhibit a scatter of 22 ppm about a median depth of 1406 ppm and in channel 1 exhibit a scatter of 131 ppm about a median depth of 1092 ppm.

As shown in Figures 2 and 3, the scatter in the data is consistent with the uncertainty in each measurement in all cases except for the channel 1 HD 209 data. Given the number of observations at the achieved precision, we would expect the resultant eclipse depths to represent a sampling of a distribution represented by the shaded areas in Figures 2 and 3. The channel 1 observations of HD 209, which exhibit more scatter than indicated by the error bars, is thought to be due to unresolved systematics. This is further supported by the larger values of $\beta_{\rm red}$ in the channel 1 observations in comparison to channel 2.

4.1. Constraints on Temporal Variability

As a probe of periodic variability in the eclipse depths we calculate the absolute difference in eclipse depths for each pair of observations. The absolute difference is plotted against the time between observations. Small numbers of observations do not lend themselves to more thorough methods of detecting power at certain timescales such as Lomb-Scargle periodograms, however, this simple approach would show a spike in absolute difference at any relevant timescale. The apparent random scatter of the data points in Figure 4 does not indicate any periodic structure in any of the observations. Given that we find no evidence for variability in our observations we compare the standard deviation and the magnitude of the eclipse depths to constrain variability to less than (5.6% and 6.0%) and (12% and 1.6%) for channels (1, 2) of HD 189733b and HD 209458b, respectively. We synthesized a periodic signal over a grid of varying periods and amplitudes to demonstrate that our observations would be sensitive to variability above the levels of our constraint. We then simulated measurements using the relevant uncertainty at each of the observation times. We evaluate the delta BIC for a constant signal versus a periodic signal at each grid point averaged over 100 trials. We find that the detection threshold is not sensitive to period over the timescales probed by these observations, only amplitude. The

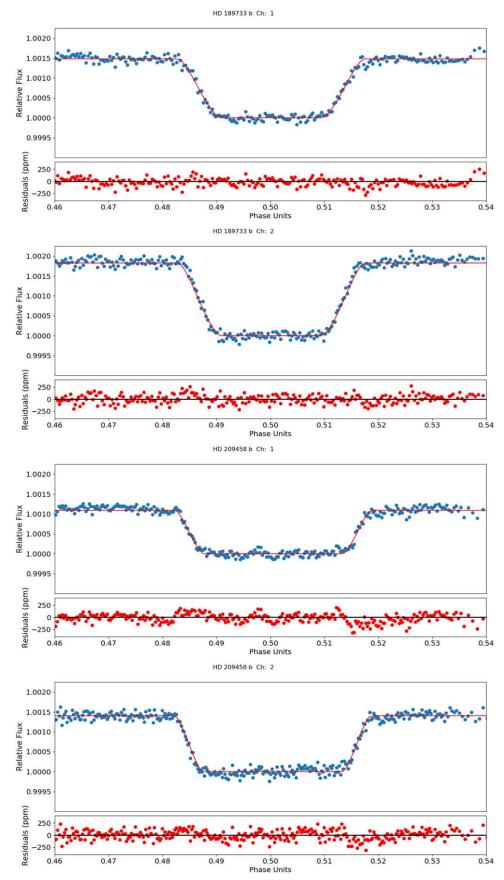


Figure 1. Each of the above panels shows the light curve after all data points for each planet/channel are binned to \sim 1 minute bins with systematics removed. The best-fit model based on the weighted averages as stated in Section 4 is plotted in red. The residuals from each individual fit are combined and binned at the same interval.

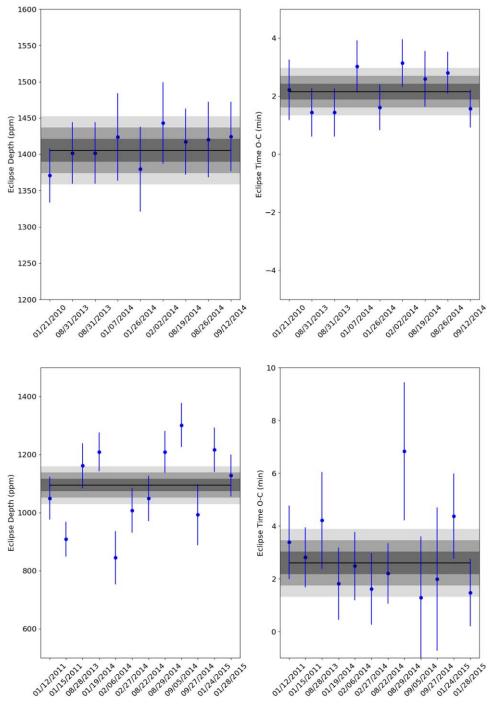


Figure 2. Eclipse depths and timing for the 9 channel 2 eclipses (top) and the 12 channel 1 eclipses (bottom) of HD 209458b with multiple methodologies. The shaded gray areas represent the 1, 2, and 3σ areas of a distribution derived from the mean and uncertainty of the measurements as a whole.

delta BIC is noisy and insignificant until amplitudes equivalent to our previously stated constraints after which it increases rapidly with signal amplitude. This metric provides evidence that if a signal were present our observations would be sensitive to it.

4.2. Stellar Variability

Stellar variability in the form of spots or plages can affect the measured planetary transit signal, potentially altering one's interpretation of its atmospheric composition, particularly for bright targets with large transit signals (Pont et al. 2008;

Silva-Valio 2008; Czesla et al. 2009; Wolter et al. 2009; Agol et al. 2010; Berta et al. 2011; Carter et al. 2011; Désert et al. 2011a; Sing et al. 2011; Fraine et al. 2014; McCullough et al. 2014; Oshagh et al. 2014; Barstow et al. 2015; Damasso et al. 2015; Zellem et al. 2015, 2017; Cauley et al. 2017, 2018; Rackham et al. 2017, 2018, 2019; Morris et al. 2018). HD 189733 is an active K0 star, which has been observed to vary by as much as $\pm 1.5\%$ at visible wavelengths with a rotation period of 11.95 days (Knutson et al. 2012 and references within), whose variability potentially impacts the observed transit depth of the planet (Knutson et al. 2012; McCullough et al. 2014). Although the amplitudes of these variations are

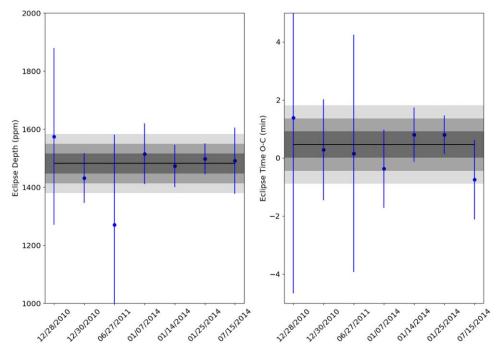


Figure 3. Eclipse depths and timing for the seven channel 2 eclipses (top) and the seven channel 1 eclipses (bottom) of HD 189733b with multiple methodologies. The shaded gray areas represent the 1, 2, and 3σ areas of a distribution derived from the mean and uncertainty of the measurements as a whole.

reduced as our *Spitzer*/IRAC observations are in the infrared (Oshagh et al. 2014; Rackham et al. 2017; Morris et al. 2018) and of eclipses (Zellem et al. 2017), we examine the amplitude of these changes in comparison to the scatter and uncertainty in our eclipse depth measurements.

We employ ground-based monitoring spanning the 2009 to 2014 observing seasons with the Tennessee State University 0.8 m Automated Photoelectric Telescope (APT) at Fairborn Observatory in southern Arizona (e.g., Henry 1999; Eaton et al. 2003, Figure 5). However, most of our Spitzer/IRAC observations occur outside the APT observing season (Figure 5). While previous studies have interpolated APT monitoring to their Spitzer observations (Knutson et al. 2012) using an activity model (Aigrain et al. 2012) to fit the APT data and interpolated it to their Spitzer observations, we conservatively take the peak-totrough Strömgren b+y variability observed by APT from 2009 to 2014 (4.7%) and interpolate it to the infrared using the scaling presented in Knutson et al. (2012; 1.6%). Using Equation (7) in Zellem et al. (2017), we estimate the effect of HD 189733's variability on the observed eclipse depths and find that variability does not statistically impact the eclipse depths of HD 189733b as the changes in its measured eclipse depths induced by variability are less than the measurement uncertainties of the eclipses themselves (Figure 5).

5. Discussion

5.1. Model Predictions

Given that our assessment of atmospheric variability is in direct relation to the planet's atmospheric dynamics, we compare our *Spitzer* variability estimates to predictions from three-dimensional general circulation models (GCMs). In particular, we use GCM simulations of HD 189733b from Showman et al. (2009) and HD 209458b from Kataria et al. (2016), respectively, which utilize the Substellar and Planetary

Radiation and Circulation (SPARC) model (Showman et al. 2009). The SPARC model couples the GCM maintained at the Massachusetts Institute of Technology (the MITgcm; Adcroft et al. 2004) with a plane-parallel, two-stream version of the multistream radiation code developed by Marley & McKay (1999). Further details on these models are provided in Showman et al. (2009), Kataria et al. (2016), and references therein.

Using the prescription described in Fortney et al. (2006) and Showman et al. (2009), we compute simulated eclipse depths derived from our GCM results for each planet over a period of 1–2 Earth years (Figure 6). At each *Spitzer* bandpass, the simulations, on average, exhibit a periodic variation in eclipse depth of 1%–1.5% over a period of \sim 43 days for HD 189733b and a variation of 0.5%–1% over a period of \sim 40 days for HD 209458b. This predicted variability is the result of a global sloshing mode or wave dynamics deep in the planetary atmosphere that leave only a small measurable effect at observable pressures (Showman et al. 2009). Therefore, hot Jupiters such as these should exhibit low (\sim 1%) variability over timescales much longer than the planet's orbital period and smaller than the typical uncertainty in eclipse depth with current instruments.

The low observed atmospheric variability of HD 189733b and HD 209458b with *Spitzer* is in contrast to observations of brown dwarfs and solar system gas giants where temporal variability at infrared wavelengths has been observed at the 10%–50% level (see a review by Artigau 2018). The low level of observable infrared variability for hot Jupiters like HD 189733b and HD 209458b compared with brown dwarfs and solar system gas giants likely arises from differences in the relative strengths in radiative and advective processes taking place in their atmospheres. Because brown dwarfs are self-luminous and comparatively fast rotators ($T_{\rm orb} \sim hr$), their circulation is dominated by multiple bands of jets and vortices (Showman et al. 2009). In contrast, the high stellar insolation and synchronous (and hence slower) rotation of hot

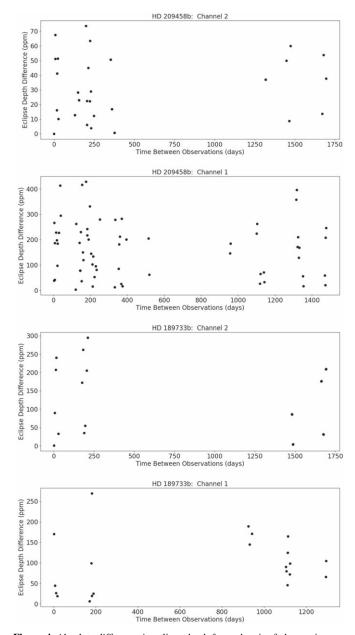


Figure 4. Absolute difference in eclipse depth for each pair of observations are plotted as a function of the time between observations. Any periodic variability would manifest as peaks in this plot. The data appears to be randomly scattered suggesting that any variability in the eclipse depths is likely due to precision limitations rather than any periodic variability in the astrophysical signal.

Jupiters results in the emergence of strong day—night forcing that produces fast (~1 km s⁻¹) planetary-scale jets. The strong radiative forcing and global-scale circulation patterns in the observable portion of hot-Jupiter atmospheres suppress small-scale variations in the planet's thermochemical structure that would contribute to large-amplitude variations in the dayside flux from the planet.

5.2. Further Observational Probes of Variability

Our ability to probe variability in exoplanet atmospheres is currently limited by the available targets and observational facilities. It is important to remember that facilities like *Spitzer* were not originally designed for high-precision time-series observations. With hot-Jupiter targets that orbit bright nearby host stars like HD 209458b and HD 189733b, per eclipse

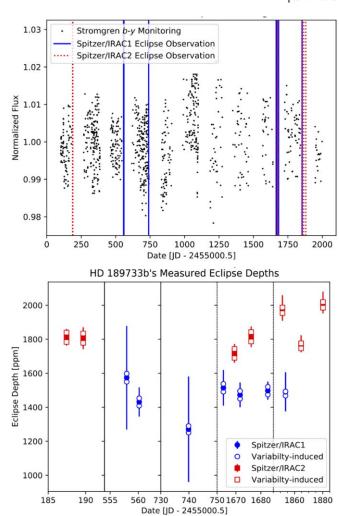


Figure 5. Top: HD 189733's stellar variability from the 2009–2014 observing seasons with our *Spitzer*/IRAC observations also indicated (IRAC1 in solid blue and IRAC2 in dotted red). Bottom: conservatively using HD 189733's overall peak-to-trough variability (top), we estimate its impact on the planet's eclipse depth using the prescriptions described in Knutson et al. (2012) and Zellem et al. (2017). We find that any variability-induced changes to HD 189733b's eclipse depths (empty blue diamonds for IRAC2 and empty red squares for IRAC2) fall within our measurement uncertainties. Therefore, the stellar variability of HD 189733 does not statistically impact our measured eclipse depths.

precisions on the order of 100 ppm can be achieved with Spitzer. Future observational facilities, such as JWST, will both improve the achievable precision on eclipse depth measurements and greatly expand the wavelengths over which they can be obtained (Beichman et al. 2014). Hot-Jupiter models predict significant variations in temperature, chemistry, and circulation patterns as a function of pressure level in the atmosphere (e.g., Showman et al. 2009), which translates into a strong wavelength dependence in the predicted levels of observable variability (e.g., Lewis et al. 2014). The observations presented here at 3.6 and 4.5 μ m for HD 209458b and HD 189733b are predicted to probe a fairly limited pressure range in the \sim 1–100 mbar level of these planets atmospheres (e.g., Showman et al. 2009). Future observations of hot Jupiters at higher precision spanning a larger range of wavelengths as well as observations of cooler exoplanets will be critical for expanding our understanding of the physical processes driving variability, or the lack thereof, in exoplanet atmospheres.

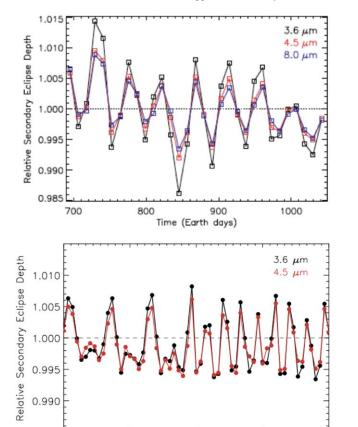


Figure 6. Model predictions of variability in eclipse depth orbit to orbit. The top panel is taken from Showman et al. (2009) and shows the predicted change in eclipse depth orbit to orbit for HD 189733b at 3.6, 4.5, and 8.0 μ m. The bottom panel shows the predicted variation for HD 209458b at 3.6 and 4.5 μ m. In both cases the eclipse depths are scaled by the mean eclipse depth to illustrate only the relative change.

2000

Earth days

1850

1700

5.3. Nonuniform Disk

There is prior evidence of nonuniform thermal distributions in both of the targets studied here. The analysis of the full orbit phase curves of HD 189733b (Knutson et al. 2012) provides evidence for an eastward shift of the hottest portion of the planetary atmosphere with respect to the substellar point of 5.29 \pm 0.59 and 2.98 \pm 0.82 hr in channels 1 and 2, respectively. These offsets correspond to longitudinal offsets of 35° \pm 4° and 20° \pm 6°. Similarly, phase curve analysis of HD 209458b at 4.5 μm by Zellem et al. (2014) indicates an offset of 41° \pm 6°.

Williams et al. (2006) and Rauscher et al. (2007) predicted that a nonuniform dayside temperature distribution will change the shape of ingress/egress in comparison to a uniformly bright model. Also, as Williams et al. (2006) predicted and Agol et al. (2010) observed, fitting the eclipse of a planet with a nonuniform dayside temperature distribution with a uniform occultation model will result in an apparent delay in the eclipse time as a result of these changes to the shape of ingress/egress when the timing of the eclipse is a free parameter. In Figures 2 and 3 we plot the difference between the center of eclipse time and what would be expected by assuming that the eclipse would occur at exactly one-half of a period from the transit. HD 209458b consistently shows an offset in the eclipse time of $155\pm25\,\mathrm{s}$ in channel 1 and $129\pm16\,\mathrm{s}$ in channel 2. HD

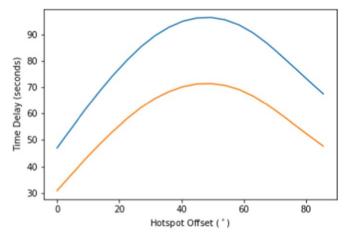


Figure 7. Apparent delay in the center of eclipse time as a function of the offset of the hot spot for HD 209458b (blue) and HD 189733b (orange) at 4.5 μ m. An offset hot spot causes changes to the shape of ingress/egress that will manifest as a delay in the eclipse timing when being fit with a uniform occultation model

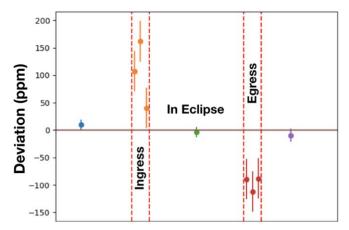


Figure 8. Here we stack the residuals from the best fit of each HD 209458b channel 2 observation with the time of mid eclipse fixed to coincide with phase 0.5 plus the transit time of light across the system. We bin them into nine separate bins: one each for pre-eclipse, during eclipse, and post-eclipse and three each for ingress and egress. The structure shown in ingress/egress is similar to model predictions illustrated in Williams et al. (2006) and Rauscher et al. (2007) resulting from fitting a nonuniform dayside temperature distribution with a uniform occultation model.

189733b shows an offset of 28 \pm 27 s in channel 1 and 35 \pm 13 s in channel 2.

Figure 7 shows the magnitude of the effect of the longitudinal offset on the observed center of eclipse time. We create a model planet with a hot spot of a radius of $0.5 R_{planet}$ utilizing the python package SPIDERMAN (Louden & Kreidberg 2017). The global (out of hot spot) temperature is set to 1200 K and the hot spot temperature to 1700 K. Starting with the hot spot centered at the substellar point, we move the hot spot longitudinally in 1° increments and fit at each iteration with a uniform brightness model with the center of eclipse time as a free parameter. We plot in Figure 7 the delay in eclipse time relative to the predicted time exactly one-half of a period from transit. Note that some portion of apparent delay is present even in the 0° offset case. This is due to light travel time across the solar system (\sim 45 s for HD 209). The offset of the maximum brightness observed in the phase curves would suggest that eclipse observations fit with a uniform model

2300

2150

should exhibit an offset in eclipse timing of 40 and 60 s (channel 1 and 2) for HD 189733b and 90 s for HD 209458b channel 2 observations. The secondary eclipse fits presented here show strong agreement with the phase curve observations of HD 209458b. We are unable to confirm the phase curve offsets for HD 189733b with the precision attained with this set of observations.

As a further probe of non-uniformity, we refit the data while fixing the eclipse time to the expected value based on previous observations of the epoch of transit and assuming a circular orbit. We combine the residuals of all the fits of each target in each channel to probe for any coherent deviations from the uniform model. Here we see strong evidence for deviations in the shape of ingress/egress that could be caused by an eastward shifted hot spot. There are other factors that could also mimic this effect. The effect of eccentricity and shape of planet are explored in detail by de Wit et al. (2012). However, the precision with which the orbital properties of both of these canonical hot Jupiters have been characterized allow many of factors to be ruled out or tight enough constraints to be placed on them to make a significant detection of non-uniformity likely in future eclipse mapping studies (Rauscher et al. 2018).

6. Conclusion

This analysis of multi-epoch secondary eclipse observations of the canonical hot Jupiters, HD 189733b and HD 209458b, finds no evidence for temporal variability greater than the precision of our observations. We expect variability in secondary eclipse depth to be driven by the dynamics of the atmosphere thus motivating comparison of observations to GCM predictions. The simulations, on average, exhibit a periodic variation in eclipse depth of 1%-1.5% for both planets at both 3.6 and 4.5 μ m. Based on the uncertainty in each measurement of secondary eclipse depth, we are able to constrain variability to less than (5.6% and 6.0%) and (12% and 1.6%) for channels (1, 2) of HD 189733b and HD 209458b, respectively. The lack of evidence of variability provides motivation and justification to combine multi-epoch observations to achieve the precision necessary to perform high spatial resolution techniques such as eclipse mapping. The apparent offset of the center of eclipse time evident in these observations provides further evidence for a nonuniform dayside temperature distribution for the planet HD 209458b. We compare the evidence for non-uniformity to previous analyses of full phase curve observations and find agreement with HD 209458b observations at $4.5 \mu m$. The precision achieved by these observations when phase folding and stacking all like observations is enough to resolve deviations to ingress/egress caused by a nonuniform temperature distribution in at least the case of HD 209458b at 4.5 μ m. This level of precision meets the requirements to utilize the eclipse mapping technique to produce spatially resolved, twodimensional maps of the planetary dayside thermal distribution.

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